



# Evidence for $D^0$ - $\bar{D}^0$ mixing: finding the (small) crack in the Standard Model

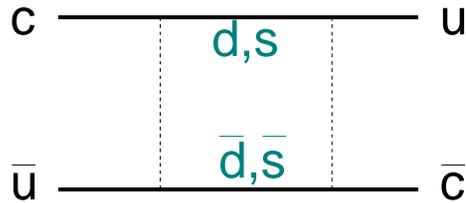


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*University of Cincinnati*

**Joint Experiment/Theory Seminar**  
*Fermilab*  
**April 27th, 2007**

- neutral meson mixing
- $D^0$  meson mixing
- 3 new  $D^0$  measurements
- summary of knowledge; what have we learned?

# Neutral meson mixing I:



Flavor eigenstates are  
not mass eigenstates:

$$i\frac{\partial}{\partial t} \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix} = \left( M - \frac{i}{2}\Gamma \right) \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix}$$

$$\begin{aligned} |D_1\rangle &= p|D^0\rangle + q|\bar{D}^0\rangle \\ |D_2\rangle &= p|D^0\rangle - q|\bar{D}^0\rangle \end{aligned}$$

$$\begin{aligned} |D_1(t)\rangle &= |D_1\rangle e^{-(\Gamma_1/2 + im_1)t} \\ |D_2(t)\rangle &= |D_2\rangle e^{-(\Gamma_2/2 + im_2)t} \end{aligned}$$

$$|D^0\rangle = \frac{1}{2p} (|D_1\rangle + |D_2\rangle)$$

$$|\bar{D}^0\rangle = \frac{1}{2q} (|D_1\rangle - |D_2\rangle)$$

$$\begin{aligned} |D^0(t)\rangle &= e^{-(\bar{\Gamma}/2 + i\bar{m})t} \left\{ \cosh [(\Delta\gamma/4 + i\Delta m/2)t] |D^0\rangle + \left(\frac{q}{p}\right) \sinh [(\Delta\gamma/4 + i\Delta m/2)t] |\bar{D}^0\rangle \right\} \\ |\bar{D}^0(t)\rangle &= e^{-(\bar{\Gamma}/2 + i\bar{m})t} \left\{ \left(\frac{p}{q}\right) \sinh [(\Delta\gamma/4 + i\Delta m/2)t] |D^0\rangle + \cosh [(\Delta\gamma/4 + i\Delta m/2)t] |\bar{D}^0\rangle \right\} \end{aligned}$$

$$\bar{m} \equiv \frac{1}{2} (m_1 + m_2) \quad \bar{\Gamma} \equiv \frac{1}{2} (\Gamma_1 + \Gamma_2) \quad \Delta m \equiv m_2 - m_1 \quad \Delta\gamma \equiv \Gamma_2 - \Gamma_1$$

# Neutral meson mixing II

$$\langle f|H|D^0(t)\rangle = e^{-(\bar{\Gamma}/2+i\bar{m})t} \left\{ \cosh [(\Delta\gamma/4 + i\Delta m/2)t] \mathcal{A}_f + \left(\frac{q}{p}\right) \sinh [(\Delta\gamma/4 + i\Delta m/2)t] \bar{\mathcal{A}}_f \right\}$$

$$\langle \bar{f}|H|\bar{D}^0(t)\rangle = e^{-(\bar{\Gamma}/2+i\bar{m})t} \left\{ \left(\frac{p}{q}\right) \sinh [(\Delta\gamma/4 + i\Delta m/2)t] \mathcal{A}_{\bar{f}} + \cosh [(\Delta\gamma/4 + i\Delta m/2)t] \bar{\mathcal{A}}_{\bar{f}} \right\}$$

$$\begin{aligned} \mathcal{A}_f &\equiv \langle f|H|D^0\rangle & \bar{\mathcal{A}}_f &\equiv \langle f|H|\bar{D}^0\rangle \\ \mathcal{A}_{\bar{f}} &\equiv \langle \bar{f}|H|D^0\rangle & \bar{\mathcal{A}}_{\bar{f}} &\equiv \langle \bar{f}|H|\bar{D}^0\rangle \end{aligned}$$

Since  $\Delta m t \ll 1$  and  $\Delta\gamma t \ll 1$ , expand  $\cos(\Delta m t)$ ,  $\cosh(\Delta\gamma/2)t$ ,  $\sin(\Delta m t)$ ,  $\sinh(\Delta\gamma/2)t$ :

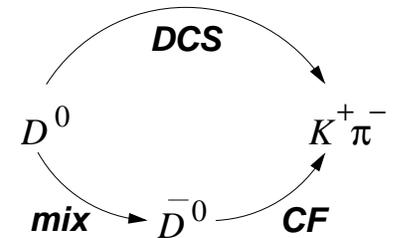
$$\begin{aligned} R(D^0(t) \rightarrow f) &\propto e^{-\bar{\Gamma}t} \left\{ 1 + [y \operatorname{Re}(\lambda) - x \operatorname{Im}(\lambda)] (\bar{\Gamma}t) + |\lambda|^2 \frac{(x^2 + y^2)}{4} (\bar{\Gamma}t)^2 \right\} \\ R(\bar{D}^0(t) \rightarrow \bar{f}) &\propto e^{-\bar{\Gamma}t} \left\{ 1 + [y \operatorname{Re}(\bar{\lambda}) - x \operatorname{Im}(\bar{\lambda})] (\bar{\Gamma}t) + |\bar{\lambda}|^2 \frac{(x^2 + y^2)}{4} (\bar{\Gamma}t)^2 \right\} \end{aligned}$$

Direct	Interference	Direct	Mixing
$x \equiv \frac{\Delta m}{\bar{\Gamma}}$	$y \equiv \frac{\Delta\Gamma}{2\bar{\Gamma}}$	$\lambda \equiv \frac{q}{p} \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f}$	$\bar{\lambda} \equiv \frac{p}{q} \frac{\mathcal{A}_{\bar{f}}}{\bar{\mathcal{A}}_{\bar{f}}}$

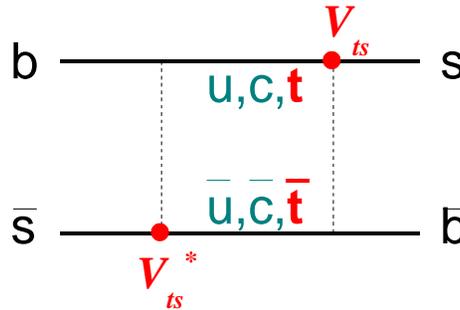
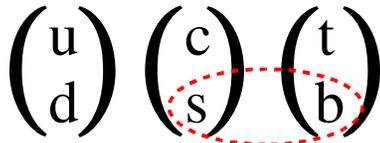
**MIXING PARAM.**

**CPV enters here**

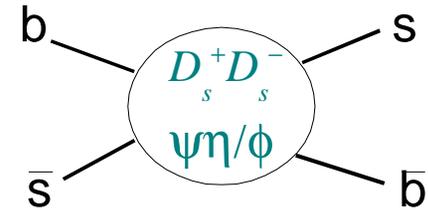
Note:  $\tau = \Gamma^{-1}$



# Neutral meson mixing III:



off-shell (“virtual”) states:  $\Delta m$



on-shell states:  $\Delta\Gamma$

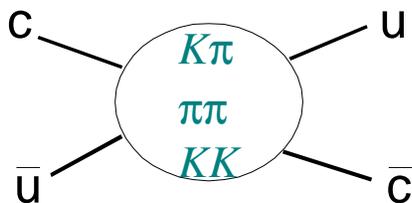
Meson	flavors	$\Delta m/\Gamma$	$\Delta\Gamma/2\Gamma$	mixing observed?
$K^0$	$\bar{s}d$	0.474	0.997	yes (1958)
$B^0$	$\bar{b}d$	0.77	< 1%	yes (1987)
$B_s^0$	$\bar{b}s$	27	$0.15 \pm 0.07$	yes (2006)
$D^0$	$\bar{c}u$	< 0.029	$0.011 \pm 0.005$	before March'07: no after March 13: yes

- small because:
- doubly-Cabibbo-suppressed with respect to  $\Gamma_D$
  - GIM mechanism cancellation:  $V_{cd}^* V_{ud} + V_{cs}^* V_{us} + V_{cb}^* V_{ub} = 0$

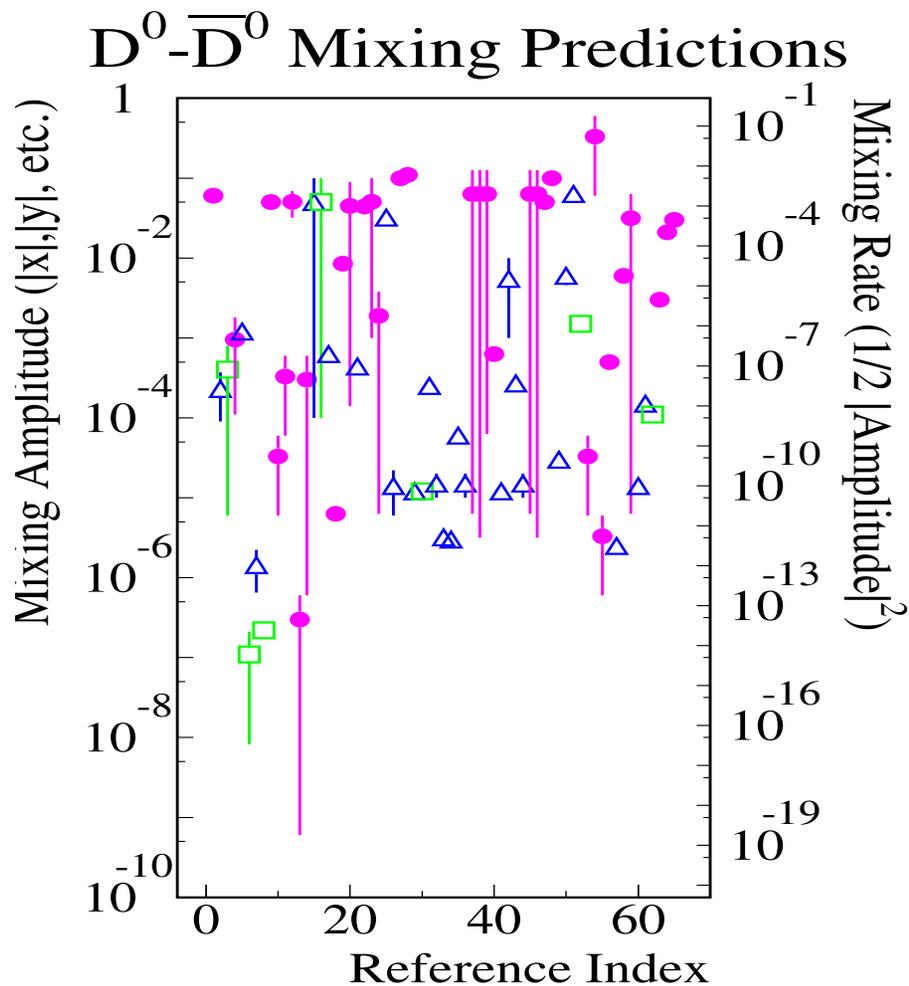
# $D^0$ meson mixing:

Nelson, hep-ex/9908021  
 Golowich, Petrov, PLB 625 (2005) 53  
 Bianco *et al.*, Riv.Nuov.Cim.26N7-8 (2003)

**Expect in SM:** mixing is dominated by “long-distance” (non-perturbative) contributors



$x \rightsquigarrow y \sim$	$10^{-6} - 10^{-3}$	(short distance)
	$10^{-3} - 10^{-2}$	(long distance)



# $D^0$ mixing measurements

- **Wrong-sign semileptonic  $D^0(t) \rightarrow K^+ l^- \nu$  decays**  
measures  $x^2 + y^2$ , no DCS contamination



- **Wrong-sign hadronic  $D^0(t) \rightarrow K^+ \pi^-$  decays**  
measures  $x' = x \cos \delta + y \sin \delta$ ,  $y' = y \cos \delta - x \sin \delta$ ,  
where  $\delta$  is a strong phase difference



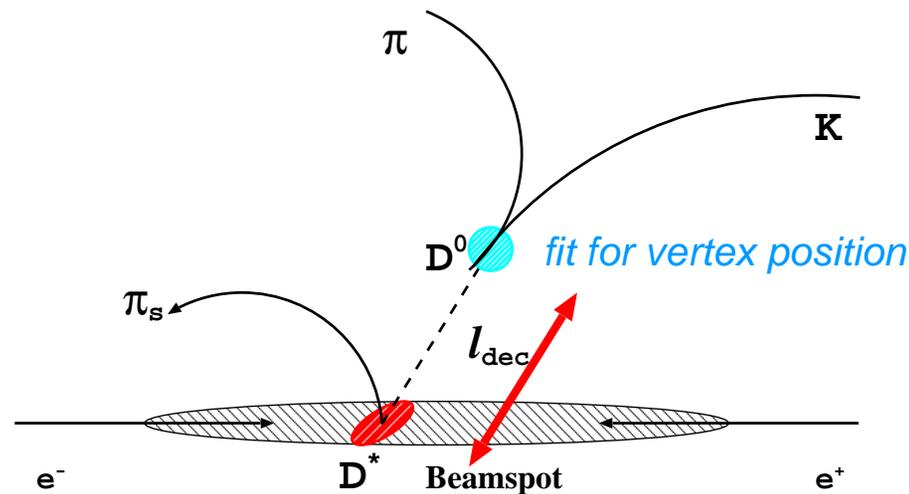
- **Decays to CP eigenstates:  $D^0(t) \rightarrow K^+ K^-, \pi^+ \pi^-$**   
measures  $y \cos \phi$ , where  $\phi$  is a weak phase difference



- **Dalitz plot analysis of  $D^0(t) \rightarrow K^0 \pi^+ \pi^-$  decays**  
measures  $x, y$
- **Wrong-sign hadronic  $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-, K^+ \pi^- \pi^0$  decays**  
measures  $x^2 + y^2$
- **Quantum correlations in  $e^+ e^- \rightarrow D^0 \bar{D}^0(n\pi^0), D^0 \bar{D}^0 \gamma(n\pi^0)$**   
measures  $y, \cos \delta$

# Experimental Method

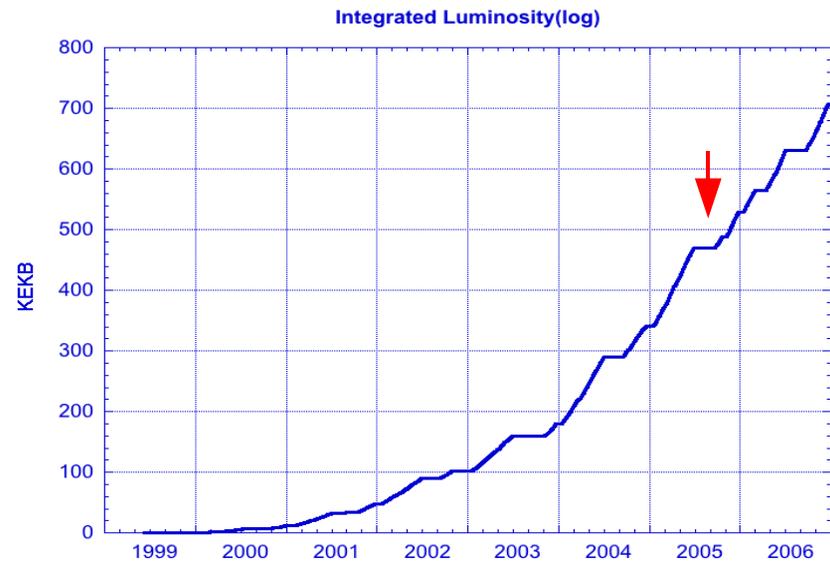
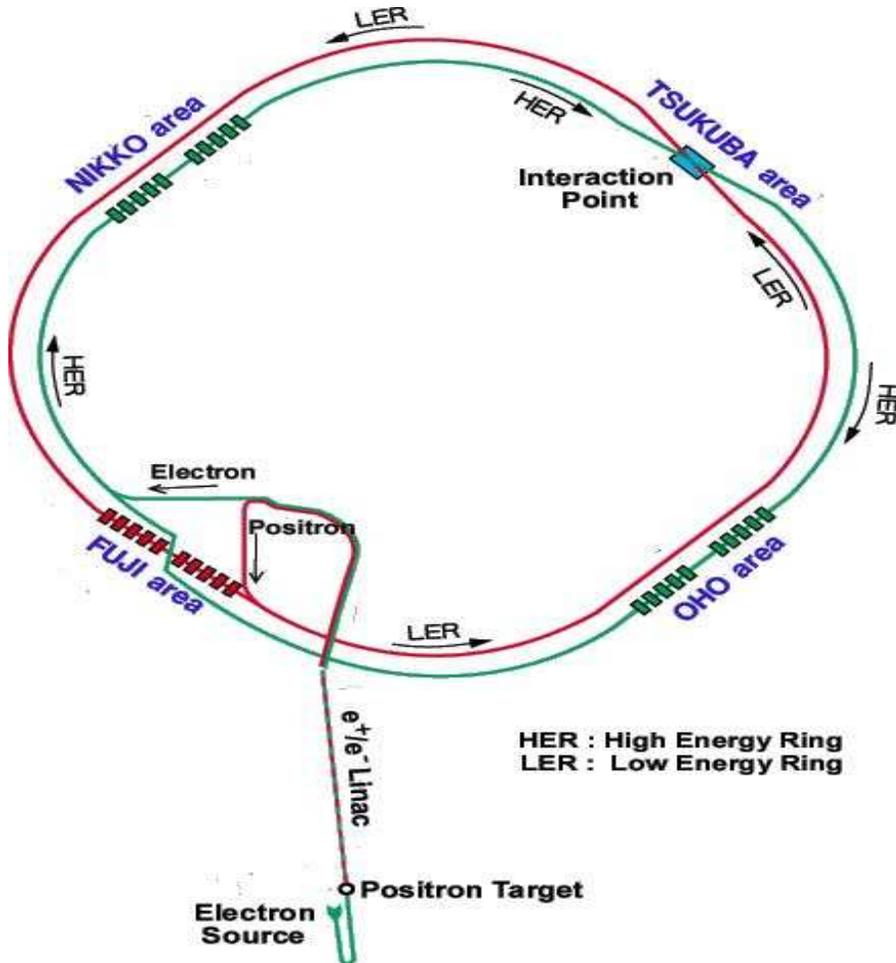
- Initial flavor of  $D^0(t)$  is determined from  $D^{*+} \rightarrow D^0\pi^+$  or  $D^{*-} \rightarrow D^0\pi^-$   
 This also greatly reduces background:  $Q = m_{K\pi\pi} - m_{K\pi} - m_\pi$  only 6 MeV/c  
 (very near threshold)
- $D^0$  proper decay time  $\Delta t = (l_{dec}/p) \times (m/c)$  measurement:



- $p(D^*) > 2.5$  GeV to eliminate  $D^0$ 's from  $B$  meson decay  
 (at  $e^+e^- \rightarrow Y(4S)$  resonance,  $\sigma(bb)/\sigma(\text{all}) = 1/3$ )

# KEKB accelerator (Tsukuba, Japan)

$e^+e^- \rightarrow Y(4S) \rightarrow BB$   
 3.5 GeV on 8.0 GeV

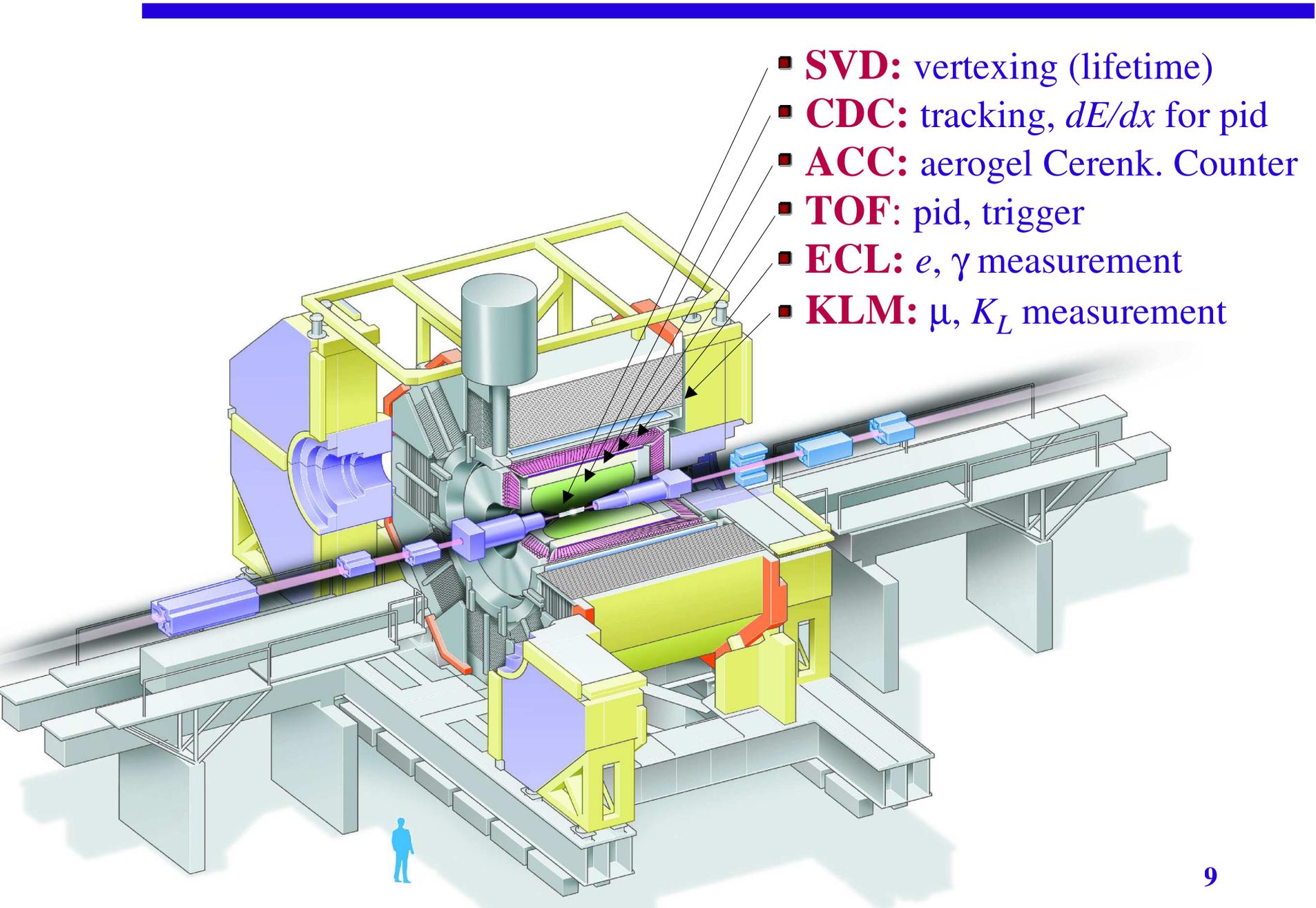


$$\int L dt = 710 \text{ fb}^{-1} \quad (25 \text{ Dec } 2006)$$

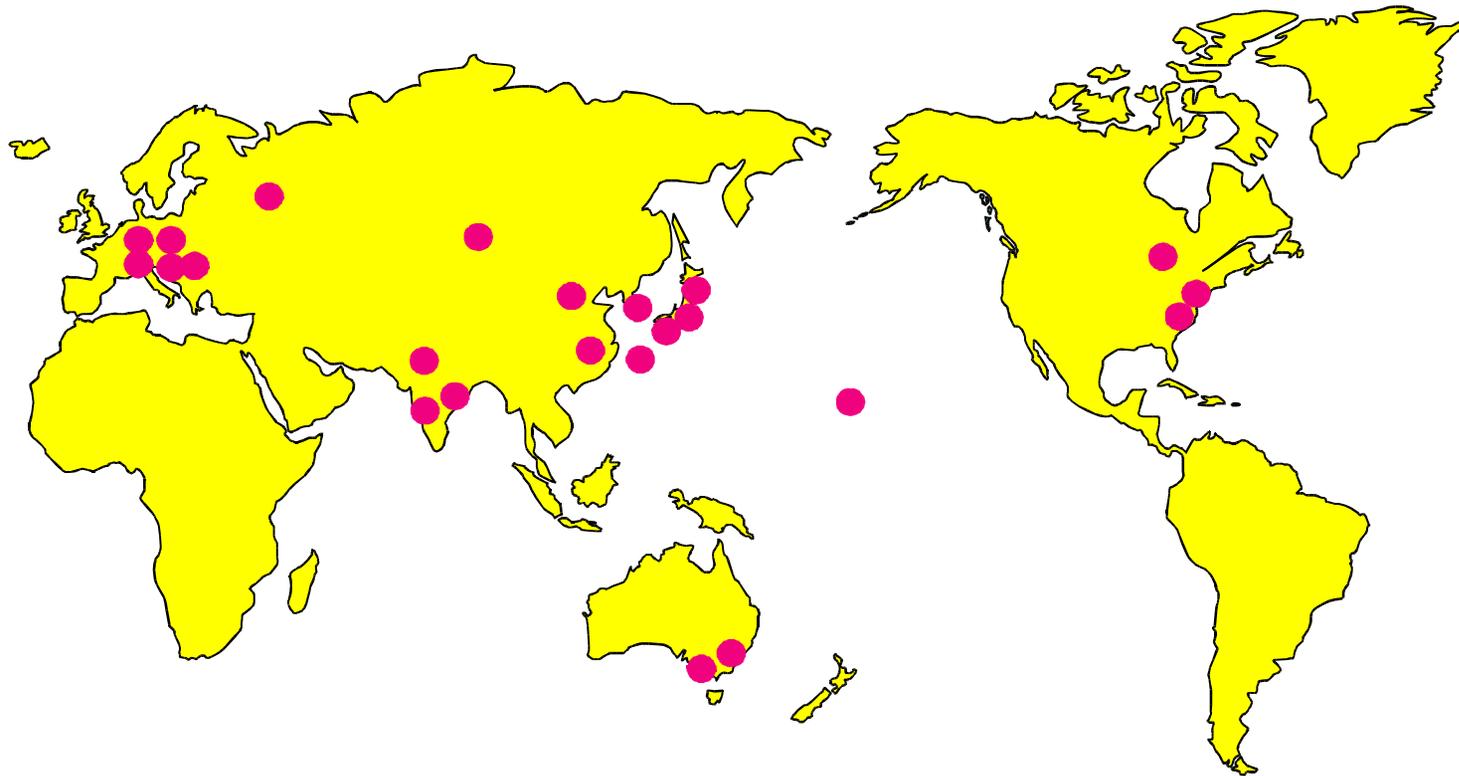
$$L_{\text{peak}} (\text{max}) = 1.5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

540 fb<sup>-1</sup> reported here

# The Belle Detector



# *The Belle Collaboration*



About 400 people from 59 institutions, many nations

USA: Cincinnati  
Hawaii  
Princeton  
Virginia Tech

# CP eigenstates: $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$

Master formula:

$$R(D^0(t) \rightarrow f) \propto e^{-\bar{\Gamma}t} \{1 + [y \operatorname{Re}(\lambda) - x \operatorname{Im}(\lambda)] (\bar{\Gamma}t)\}$$

CP violation parameters:

$$\lambda \equiv \frac{q \bar{\mathcal{A}}_f}{p \mathcal{A}_f} = \left| \frac{q}{p} \right| e^{i\phi} \quad \bar{\lambda} \equiv \frac{p \mathcal{A}_{\bar{f}}}{q \bar{\mathcal{A}}_{\bar{f}}} = \left| \frac{p}{q} \right| e^{-i\phi}$$

$$\boxed{D^0(t) \rightarrow K^- \pi^+} \quad 50\% D_1 \text{ and } 50\% D_2 \quad |\lambda| \ll 1 \Rightarrow \mathbf{R} \sim e^{-\Gamma t}$$

$$\boxed{D^0(t) \rightarrow K^+K^- \text{ (or } \pi^+\pi^-)} \quad \text{pure } D_1 \Rightarrow \mathbf{R} = e^{-\Gamma_1 t} = e^{-\Gamma(1+y)t}$$

$$(\lambda \sim 1 \Rightarrow \mathbf{R} \sim e^{-\Gamma t}(1+y\Gamma t) \sim e^{-\Gamma t} e^{y\Gamma t} = e^{-\Gamma(1+y)t})$$

$$\Rightarrow \tau(K^- \pi^+) / \tau(K^+ K^-) = 1 + y$$

more accurate:  $y \cos\phi = \tau_{K\pi} / \tau_{KK} - 1 = y_{CP}$

E791, PRL 83, 32 (1999)

FOCUS, PLB 485, 62 (2000)

CLEO, PRD 65, 092001 (2002)

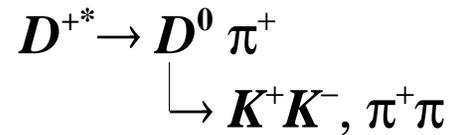
Belle, PRL 88, 162001 (2002)

Babar, PRL 91, 121801 (2003)

$$\left. \begin{array}{l} \text{E791, PRL 83, 32 (1999)} \\ \text{FOCUS, PLB 485, 62 (2000)} \\ \text{CLEO, PRD 65, 092001 (2002)} \\ \text{Belle, PRL 88, 162001 (2002)} \\ \text{Babar, PRL 91, 121801 (2003)} \end{array} \right\} y_{CP} = (1.09 \pm 0.46)\%$$

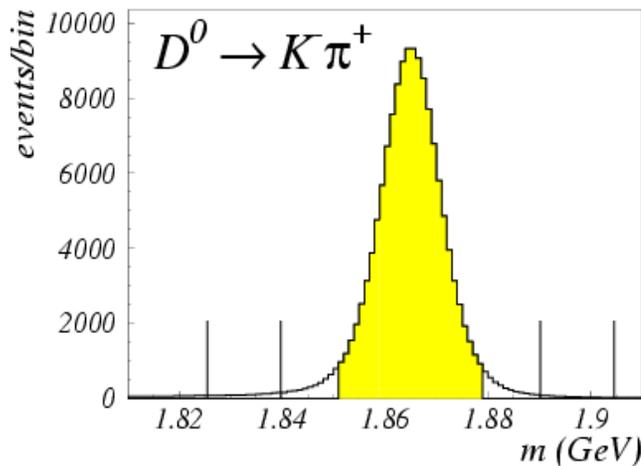
(world average)

# Belle: $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$ with $540 \text{ fb}^{-1}$

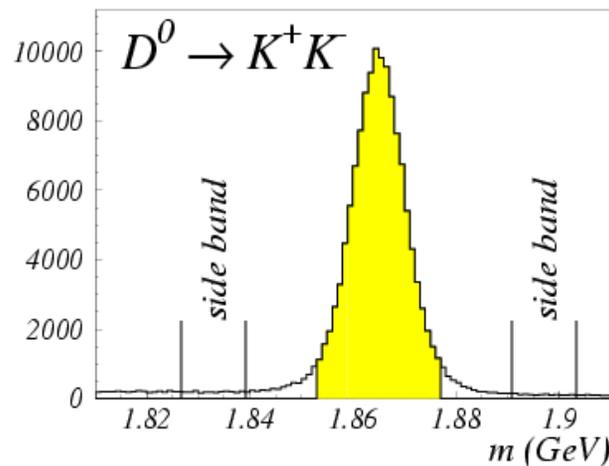


$$\left. \begin{aligned} m(D^0) &= 1865 \text{ MeV} \\ m(\pi^+) &= 139 \\ m(D^{*+}) &= 2010 \end{aligned} \right\} 2004 \text{ MeV}$$

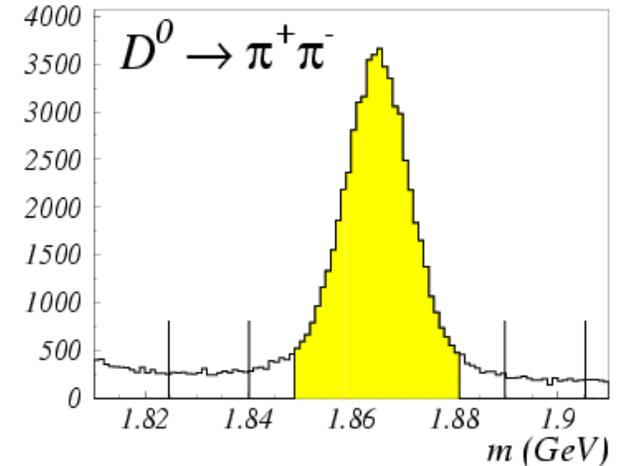
Select candidate events: require  $q = m(KK\pi) - m(D^0) - m(\pi)$  to be very small:



**1200k events**  
**99% pure**



**110k events**  
**98% pure**



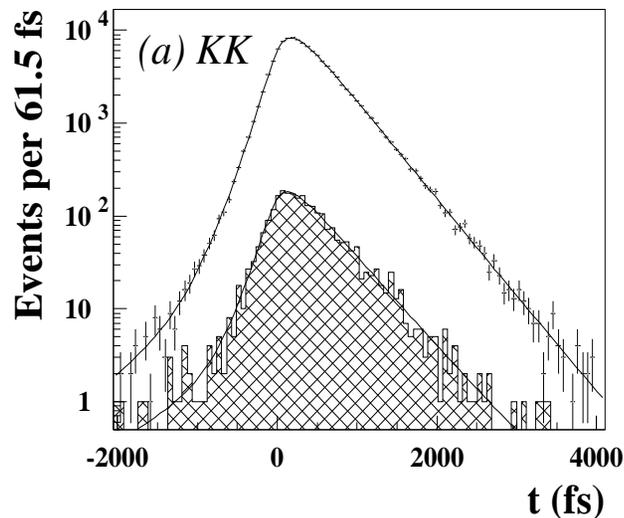
**50k events**  
**92% pure**

# *Belle: $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$ with $540 \text{ fb}^{-1}$*

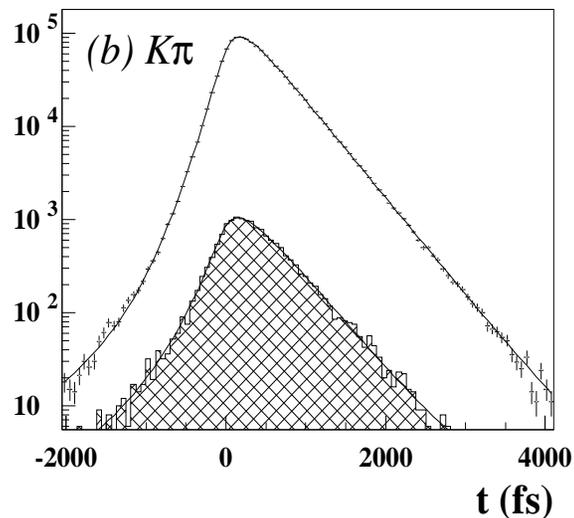
## Maximum likelihood fit to decay time spectrum:

$$\frac{dN}{dt} = \frac{N}{\tau} e^{-t/\tau} \otimes R(t) + B(t)$$

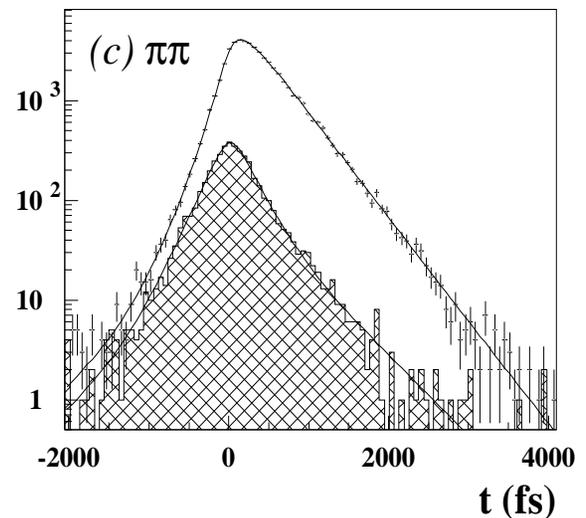
*resolution function background distribution*



$\tau = 404.0 \pm 2.2 \text{ fs}$   
(110k events)



$\tau = 408.7 \pm 0.6 \text{ fs}$   
(1200k events)

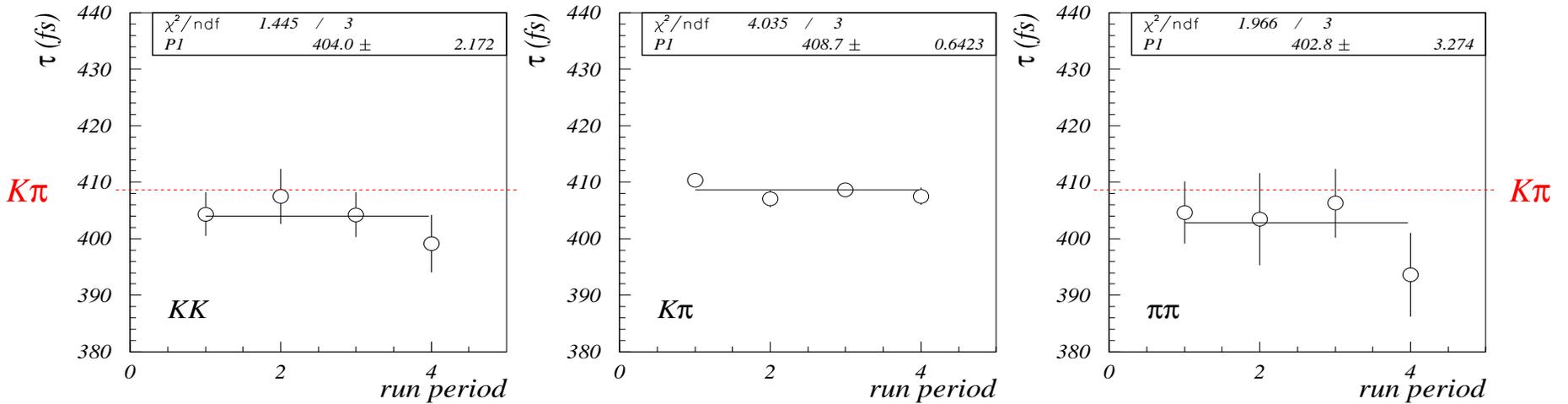


$\tau = 402.8 \pm 3.3 \text{ fs}$   
(50k events)

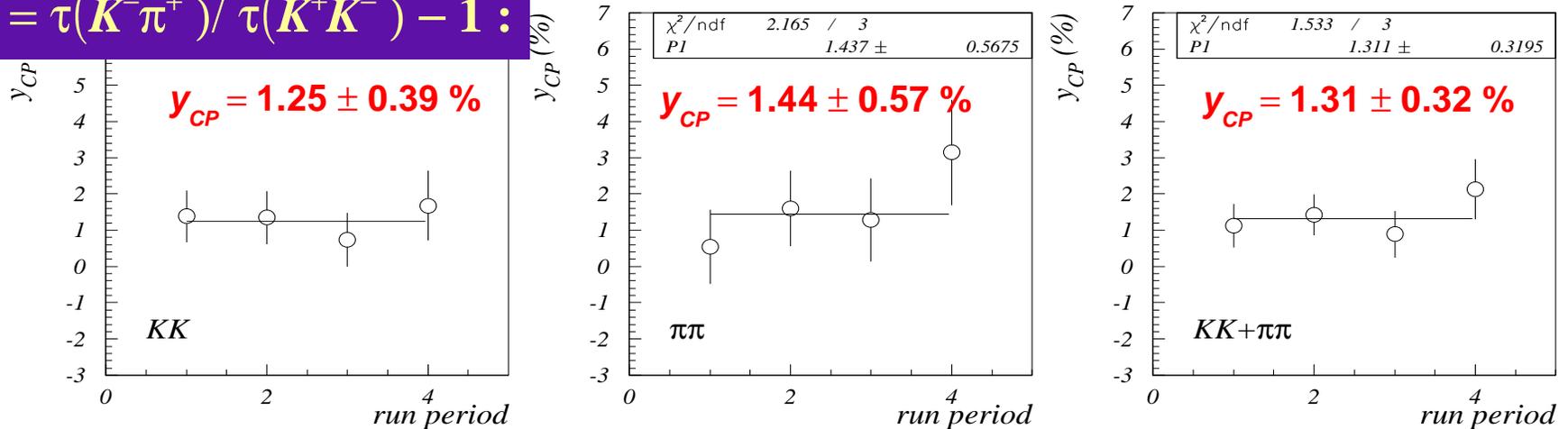
$\Rightarrow$  there is a difference between  $KK$  and  $K\pi$   
(here,  $t_0$  is free for each final state)

# Belle: $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$ with $540 \text{ fb}^{-1}$

A cross-check: divide the data into sub-samples



$$y_{CP} = \tau(K^-\pi^+) / \tau(K^+K^-) - 1 :$$



# Belle: $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$ with $540 \text{ fb}^{-1}$

## Systematic errors:

	$y_{CP}$	$A_\Gamma$
acceptance	0.12%	0.07%
equal $t_0$ assumption	0.14%	0.08%
mass window position	0.04%	0.003%
difference btw background and sidebands	0.09%	0.06%
difference btw final states opening angles	0.02%	
background parameterization	0.07%	0.07%
resolution function	0.01%	0.01%
analysis cuts	0.11%	0.05%
binning	0.01%	0.01%
<b>TOTAL</b>	<b>0.25%</b>	<b>0.15%</b>

## Final result:

$$y_{CP} = 1.31 \pm 0.32 \pm 0.25 \%$$

$> 3 \sigma$  above zero  
(first evidence for  $D^0$ - $\bar{D}^0$  mixing)

## Search for CP violation:

$$A_\Gamma = \frac{\Gamma(D^0 \rightarrow K^+K^-) - \Gamma(\bar{D}^0 \rightarrow K^+K^-)}{\Gamma(D^0 \rightarrow K^+K^-) + \Gamma(\bar{D}^0 \rightarrow K^+K^-)}$$

$$A_\Gamma = 0.01 \pm 0.30 \pm 0.15 \%$$

no evidence for CP violation

# Dalitz plot analysis of $D^0(t) \rightarrow K^0 \pi^+ \pi^-$

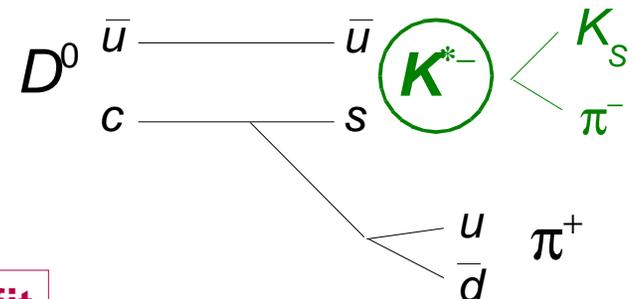
$$\begin{aligned} \langle K_S^0 \pi^+ \pi^- | H | D^0(t) \rangle &= \frac{1}{2p} \left( \langle K_S^0 \pi^+ \pi^- | H | D_1(t) \rangle + \langle K_S^0 \pi^+ \pi^- | H | D_2(t) \rangle \right) \\ &\equiv A_1 e^{-(\Gamma_1/2 + im_1)t} + A_2 e^{-(\Gamma_2/2 + im_2)t} \end{aligned}$$

$$\begin{aligned} R(D^0(t) \rightarrow K_S^0 \pi^+ \pi^-) &= |A_1|^2 e^{-\bar{\Gamma}(1+y)t} + |A_2|^2 e^{-\bar{\Gamma}(1-y)t} + \\ &2e^{-\bar{\Gamma}t} \left[ \text{Re}(A_1 A_2^*) \cos xt - \text{Im}(A_1 A_2^*) \sin xt \right] \end{aligned}$$

$$A_n \propto \sum_j a_j e^{i\delta_j} \mathcal{A}^j$$

**NOTE:** sign of  $x$  is determined

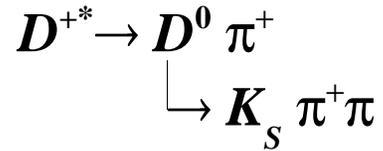
The amplitudes  $A^j$  are functions of  $m^2(K_S \pi^+)$  and  $m^2(K_S \pi^-)$  and account for various intermediate states:



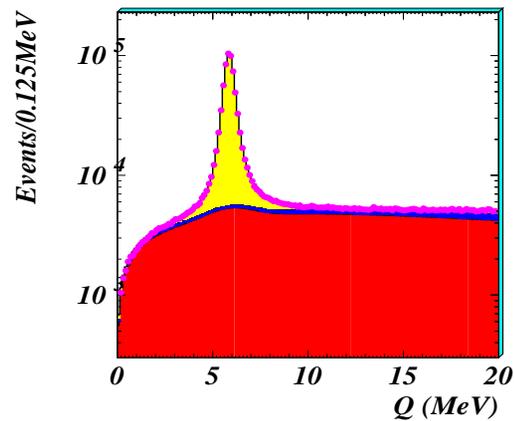
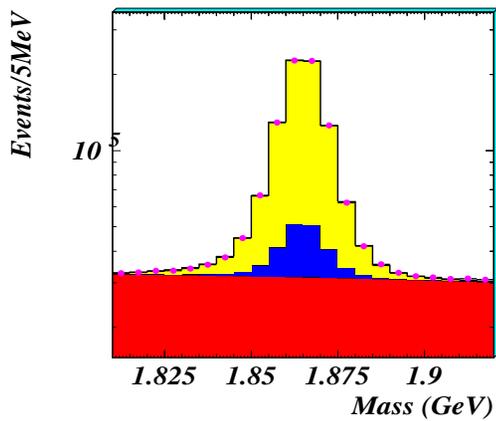
Each amplitude has a magnitude ( $a_j$ ) and phase ( $\delta_j$ )

⇒ must include these parameters (34 of them) in the fit

# Belle: $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$ with $540 \text{ fb}^{-1}$



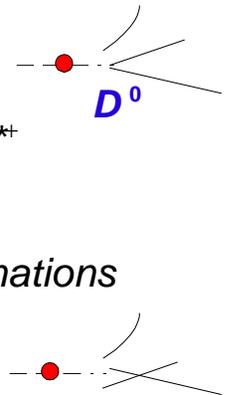
Select candidate events based on  $m(K\pi\pi)$  and  $q = m(K\pi\pi) - m(D^0) - m(\pi)$  :



signal

background #1:  
real  $D^0$ , fake  $D^{*+}$

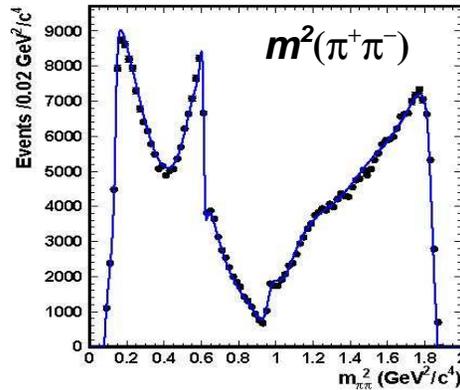
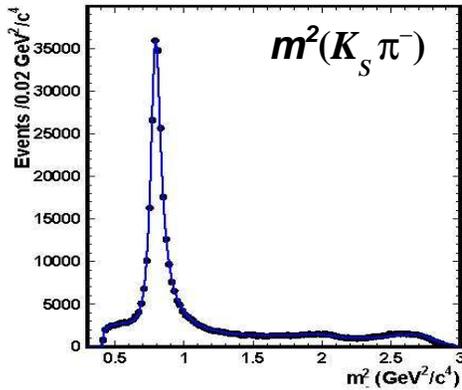
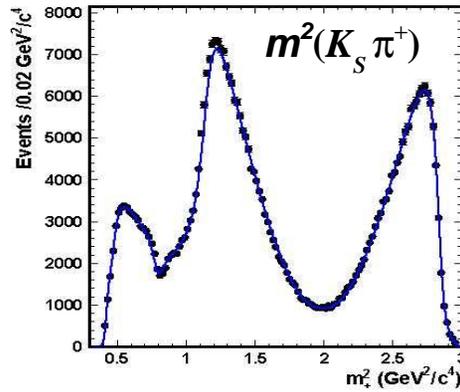
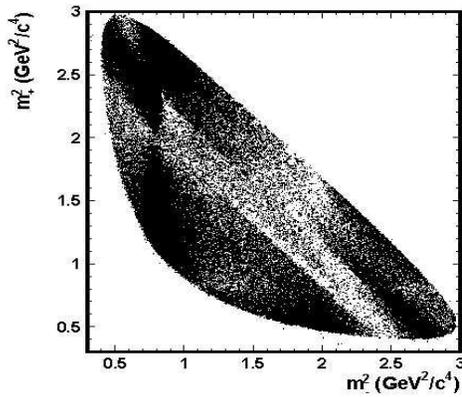
background #2:  
random combinations



534k events

95% pure

# Belle: $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$ with $540 \text{ fb}^{-1}$



Resonance	Amplitude	Phase (deg)	Fit fraction
$K^*(892)^-$	$1.629 \pm 0.005$	$134.3 \pm 0.3$	0.6227
$K_0^*(1430)^-$	$2.12 \pm 0.02$	$-0.9 \pm 0.5$	0.0724
$K_2^*(1430)^-$	$0.87 \pm 0.01$	$-47.3 \pm 0.7$	0.0133
$K^*(1410)^-$	$0.65 \pm 0.02$	$111 \pm 2$	0.0048
$K^*(1680)^-$	$0.60 \pm 0.05$	$147 \pm 5$	0.0002
$K^*(892)^+$	$0.152 \pm 0.003$	$-37.5 \pm 1.1$	0.0054
$K_0^*(1430)^+$	$0.541 \pm 0.013$	$91.8 \pm 1.5$	0.0047
$K_2^*(1430)^+$	$0.276 \pm 0.010$	$-106 \pm 3$	0.0013
$K^*(1410)^+$	$0.333 \pm 0.016$	$-102 \pm 2$	0.0013
$K^*(1680)^+$	$0.73 \pm 0.10$	$103 \pm 6$	0.0004
$\rho(770)$	1 (fixed)	0 (fixed)	0.2111
$\omega(782)$	$0.0380 \pm 0.0006$	$115.1 \pm 0.9$	0.0063
$f_0(980)$	$0.380 \pm 0.002$	$-147.1 \pm 0.9$	0.0452
$f_0(1370)$	$1.46 \pm 0.04$	$98.6 \pm 1.4$	0.0162
$f_2(1270)$	$1.43 \pm 0.02$	$-13.6 \pm 1.1$	0.0180
$\rho(1450)$	$0.72 \pm 0.02$	$40.9 \pm 1.9$	0.0024
$\sigma_1$	$1.387 \pm 0.018$	$-147 \pm 1$	0.0914
$\sigma_2$	$0.267 \pm 0.009$	$-157 \pm 3$	0.0088
NR	$2.36 \pm 0.05$	$155 \pm 2$	0.0615

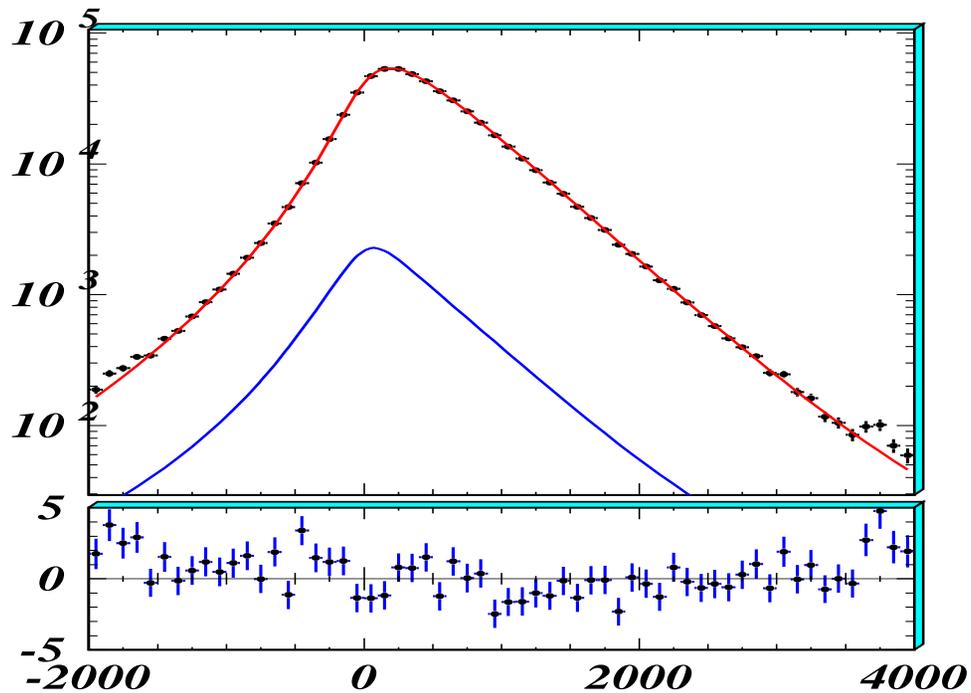
1.19

$$\text{Fit fraction} \equiv \frac{\int |a_r \mathcal{A}_r(m_-^2, m_+^2)|^2 dm_-^2 dm_+^2}{\int \left| \sum_{r=1}^n a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2) \right|^2 dm_-^2 dm_+^2}$$

$\Rightarrow$  destructive interference

# *Belle: $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$ with $540 \text{ fb}^{-1}$*

**Time fit (in projection):**



$$x = (0.80 \pm 0.29)\% \quad \text{positive}$$

$$y = (0.33 \pm 0.24)\%$$

$$t_D = (409.9 \pm 0.9) \text{ fs}$$

*consistent with PDG  
(in fact better precision)*

# Belle: $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$ with $540 \text{ fb}^{-1}$

## Largest systematic errors:

	$\Delta x (\times 10^{-2})$	$\Delta y (\times 10^{-2})$
$\rho(D^*)$ cut	+0.076	-0.078
t dependence of Dalitz background	-0.056	-0.057
background timing parameters	$\pm 0.037$	$\pm 0.063$
decay model (form factors, variation of fixed masses & widths, K-matrix, no non-resonant comp., others)	+0.13 -0.11	+0.051 -0.066
<b>TOTAL</b>	<b>(+0.17, -0.15)</b>	<b>(+0.10, -0.15)</b>

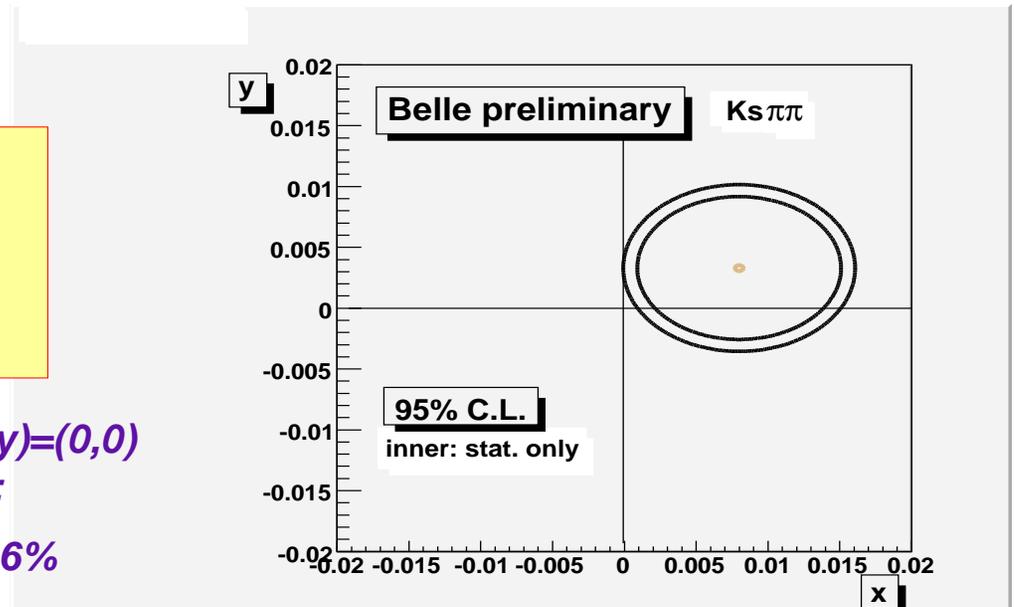
## Final result:

$$x = (0.80 \pm 0.29 \pm 0.17)\%$$

$$y = (0.33 \pm 0.24 \pm 0.15)\%$$

rise of the likelihood function at  $(x,y)=(0,0)$   
which corresponds to no mixing is:

$$-2\Delta \ln \mathcal{L} = 7.33 \Rightarrow \text{CL} = \text{only } 2.6\%$$



# Belle: $D^0(t) \rightarrow K_S^0 \pi^+ \pi^-$ with $540 \text{ fb}^{-1}$

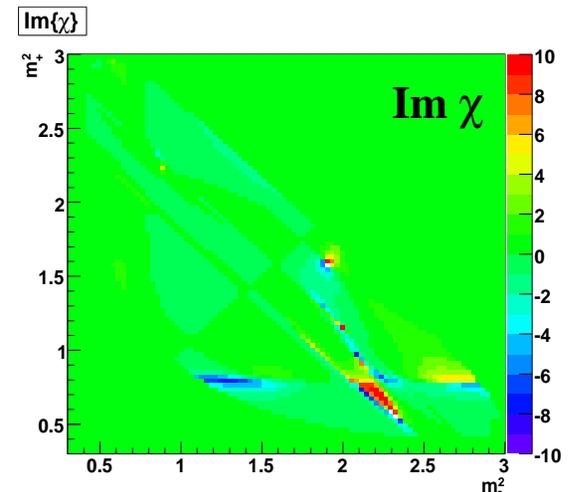
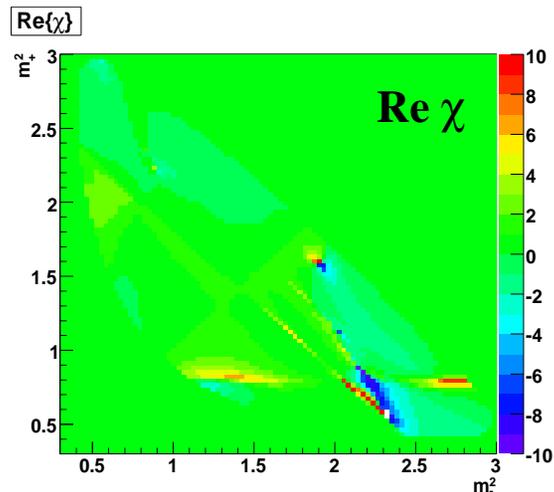
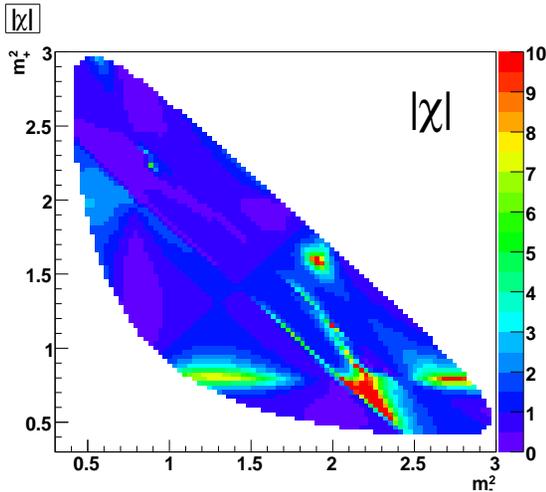
Sensitivity:

$$e_{(1,2)} = e^{-i(m_{(1,2)} - i\Gamma_{(1,2)}/2)t}$$

$$\begin{aligned} \mathcal{M}(m_-^2, m_+^2, t) &= \mathcal{A}(m_-^2, m_+^2) \frac{e_1(t) + e_2(t)}{2} + \frac{q}{p} \overline{\mathcal{A}}(m_-^2, m_+^2) \frac{e_1(t) - e_2(t)}{2} \\ &\rightarrow \mathcal{A}(m_-^2, m_+^2) \frac{e_1(t) + e_2(t)}{2} + \mathcal{A}(m_+^2, m_-^2) \frac{e_1(t) - e_2(t)}{2} \end{aligned}$$

Define  $\chi(m_-^2, m_+^2) \equiv \frac{\mathcal{A}(m_+^2, m_-^2)}{\mathcal{A}(m_-^2, m_+^2)}$ , then

$$|\mathcal{M}|^2 \approx |\mathcal{A}(m_-^2, m_+^2)|^2 \left\{ 1 + [\text{Im}(\chi) x - \text{Re}(\chi) y] t + |\chi|^2 \left( \frac{x^2 + y^2}{4} \right) t^2 \right\} e^{-\Gamma t}$$



$\Rightarrow$  much of sensitivity comes from the  $K^*(890)^+$  region and interference region between  $\rho(770)$  and  $\omega$

# Wrong-sign $D^0(t) \rightarrow K^+\pi^-$ decays

## Master formula:

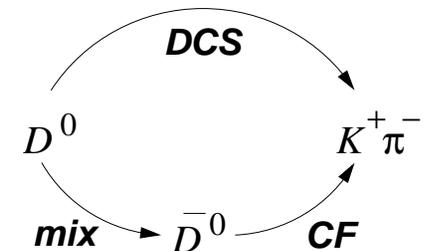
$$R(D^0(t) \rightarrow f) \propto e^{-\bar{\Gamma}t} \left\{ 1 + [y \operatorname{Re}(\lambda) - x \operatorname{Im}(\lambda)] (\bar{\Gamma}t) + |\lambda|^2 \frac{x^2 + y^2}{4} (\bar{\Gamma}t)^2 \right\}$$

$$\text{for } f = K^+\pi^-: \quad \lambda \equiv \frac{q \bar{\mathcal{A}}_f}{p \mathcal{A}_f} = \left| \frac{q}{p} \right| \sqrt{R_D} e^{i(\phi+\delta)}$$

$ q/p $	$CPV$ in mixing
$A_D \equiv (R_D - \bar{R}_D)/(R_D + \bar{R}_D)$	$CPV$ in the decay amplitude (direct $CPV$ )
$\phi$	$CPV$ in mixed/direct interference

$$\begin{aligned} R(D^0 \rightarrow K^+\pi^-) &\propto e^{-\bar{\Gamma}t} \left\{ R_D + \left| \frac{q}{p} \right| \sqrt{R_D} [y \cos(\phi + \delta) - x \sin(\phi + \delta)] (\bar{\Gamma}t) + \left| \frac{q}{p} \right|^2 \frac{(x^2 + y^2)}{4} (\bar{\Gamma}t)^2 \right\} \\ &= e^{-\bar{\Gamma}t} \left\{ R_D + \sqrt{R_D} (y \cos \delta - x \sin \delta) (\bar{\Gamma}t) + \frac{(x^2 + y^2)}{4} (\bar{\Gamma}t)^2 \right\} \quad \left( \begin{array}{l} |q/p| = 1 \\ \phi = 0 \end{array} \right) \text{ no } CPV \\ &= e^{-\bar{\Gamma}t} \left\{ R_D + \sqrt{R_D} y' (\bar{\Gamma}t) + \frac{(x'^2 + y'^2)}{4} (\bar{\Gamma}t)^2 \right\} \end{aligned}$$

$$x' \equiv x \cos \delta + y \sin \delta \quad y' \equiv y \cos \delta - x \sin \delta$$



# Belle $D^0(t) \rightarrow K^+ \pi^-$ with $400 \text{ fb}^{-1}$

R.Barate *et al.* (ALEPH), PLB 436, 211 (1998)

E.M.Aitala *et al.* (E791), PRD 57, 13 (1998)

R.Godang *et al.* (CLEO), PRL 84, 5038 (2000)

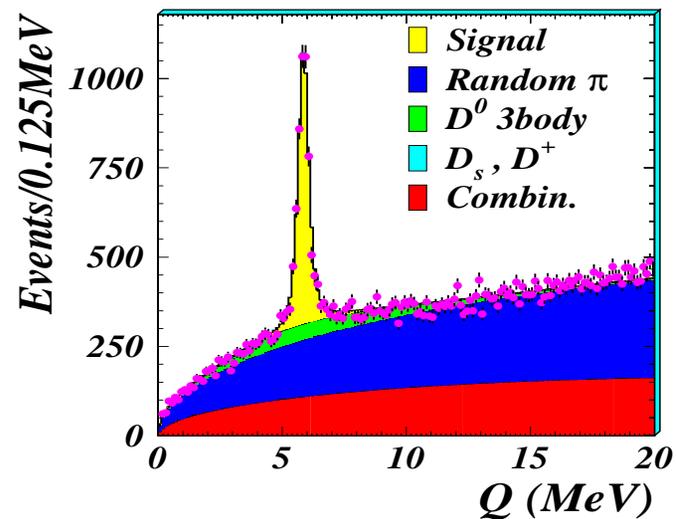
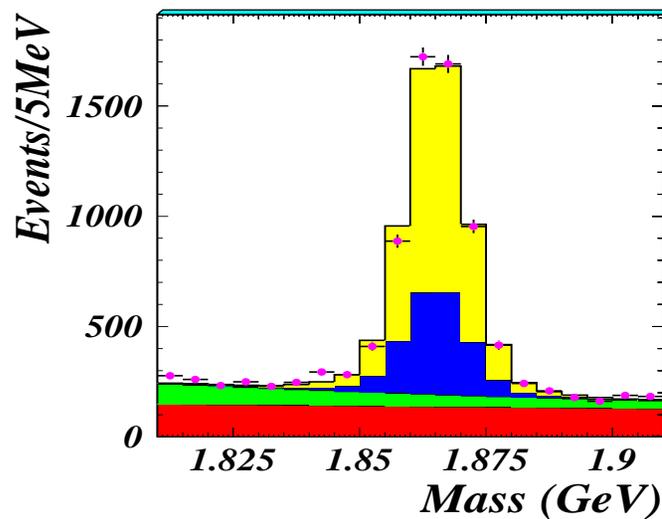
J.M.Link *et al.* (FOCUS), PRL 86, 2955 (2001); PLB 618, 23 (2005)

B. Aubert *et al.* (Babar), PRL 91, 171801 (2003)



→ L.Zhang *et al.* (Belle), PRL 96, 151801 (2006)

new → B. Aubert *et al.* (Babar), hep-ex/0703020

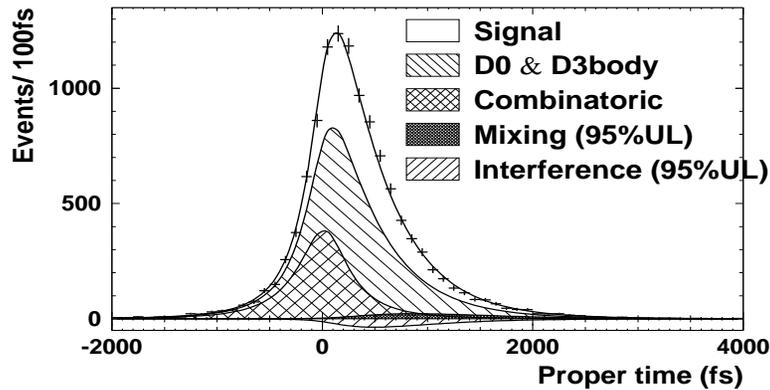


4024 events

52% purity

# $D^0(t) \rightarrow K^+ \pi^-$ (Belle and BaBar)

Time fit:



400 fb<sup>-1</sup>

$$R_D = (0.364 \pm 0.017)\%$$

$$x'^2 = (0.018^{+0.021}_{-0.023})\%$$

$$y' = (0.06^{+0.40}_{-0.39})\%$$

*no CPV*



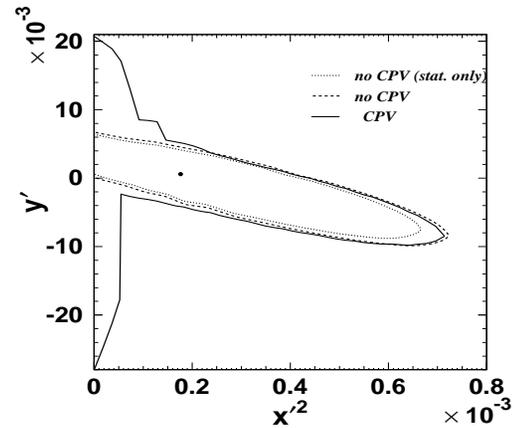
384 fb<sup>-1</sup>  
new

$$R_D = (0.303 \pm 0.019)\%$$

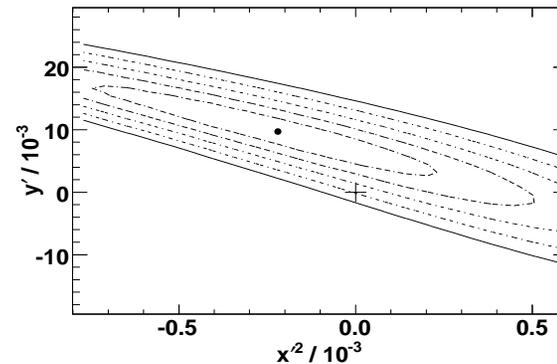
$$x'^2 = (-0.022 \pm 0.037)\%$$

$$y' = (0.97 \pm 0.54)\%$$

*no CPV*



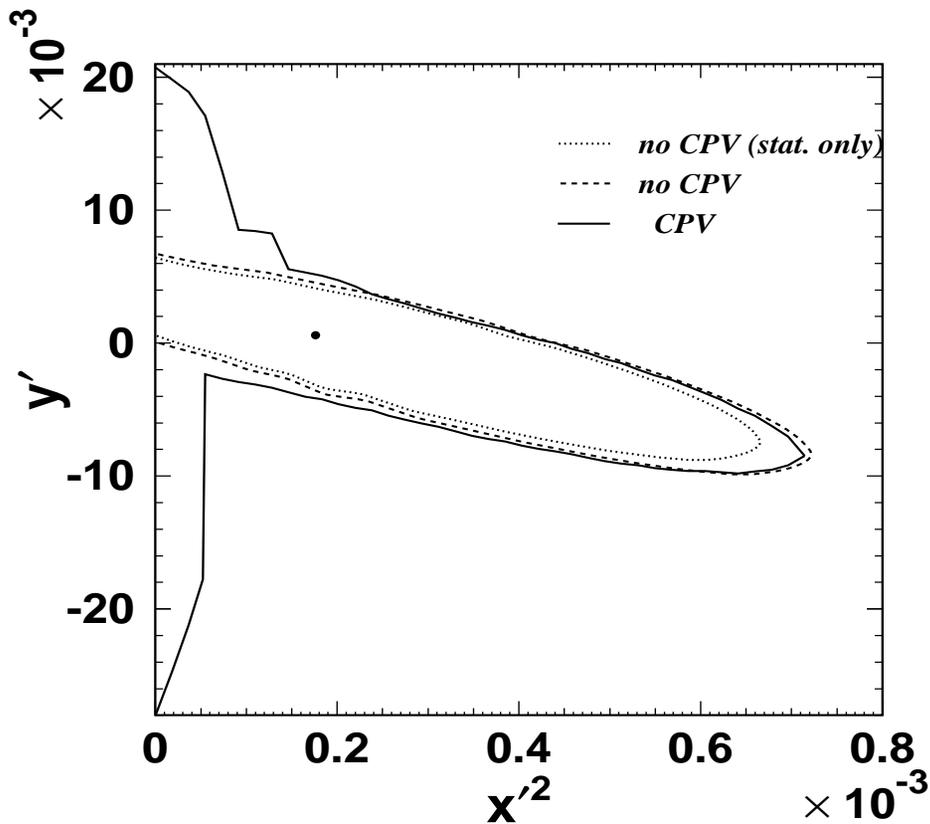
$(x', y') = (0, 0)$   
has CL = 3.9%



$(x', y') = (0, 0)$   
has CL = 0.01%  
evidence  
for mixing

# Belle $D^0(t) \rightarrow K^+ \pi^-$ with $400 \text{ fb}^{-1}$

Use toy MC to obtain frequentist (Feldman-Cousins) confidence region (95% CL):



$$x'^{\pm} = \left( \frac{1 \pm A_M}{1 \mp A_M} \right)^{1/4} (x' \cos \phi \pm y' \sin \phi)$$

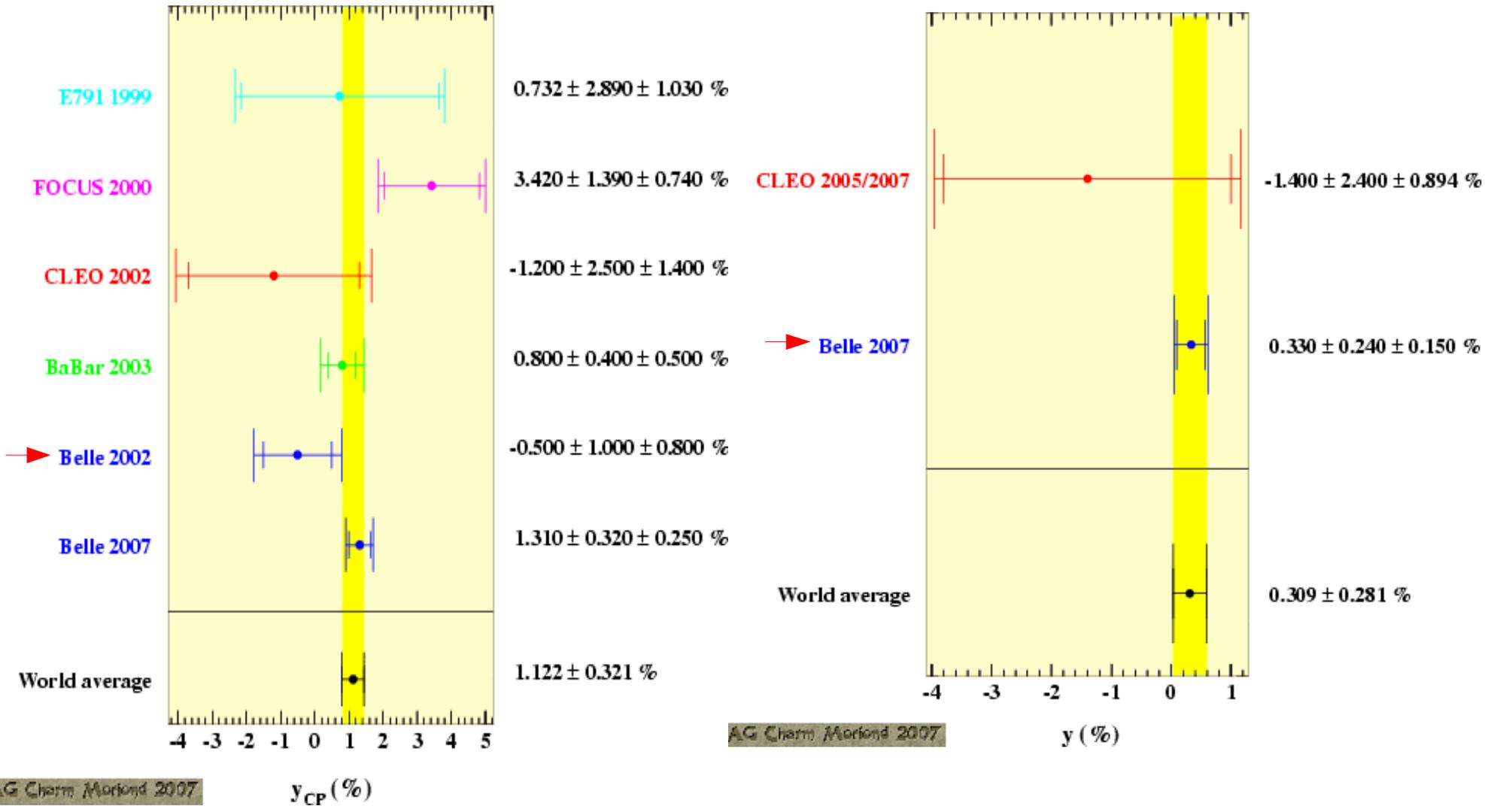
$$y'^{\pm} = \left( \frac{1 \pm A_M}{1 \mp A_M} \right)^{1/4} (y' \cos \phi \mp x' \sin \phi)$$

Fit Case	Parameter	95% CL interval ( $\times 10^{-3}$ )
No <i>CPV</i>	$x'^2$	$x'^2 < 0.72$
	$y'$	$-9.9 < y' < 6.8$
	$R_D$	$3.3 < R_D < 4.0$
	$R_M$	$0.63 \times 10^{-5} < R_M < 0.40$
<i>CPV</i> allowed	$A_D$	$-76 < A_D < 107$
	$A_M$	$-995 < A_M < 1000$
	$x'^2$	$x'^2 < 0.72$
	$y'$	$-28 < y' < 21$
	$R_M$	$R_M < 0.40$

unusual contour shape due to ambiguities

No *CPV*:  $(x'^2, y') = (0, 0)$  has **CL = 3.9%** (outside 95% CL contour)

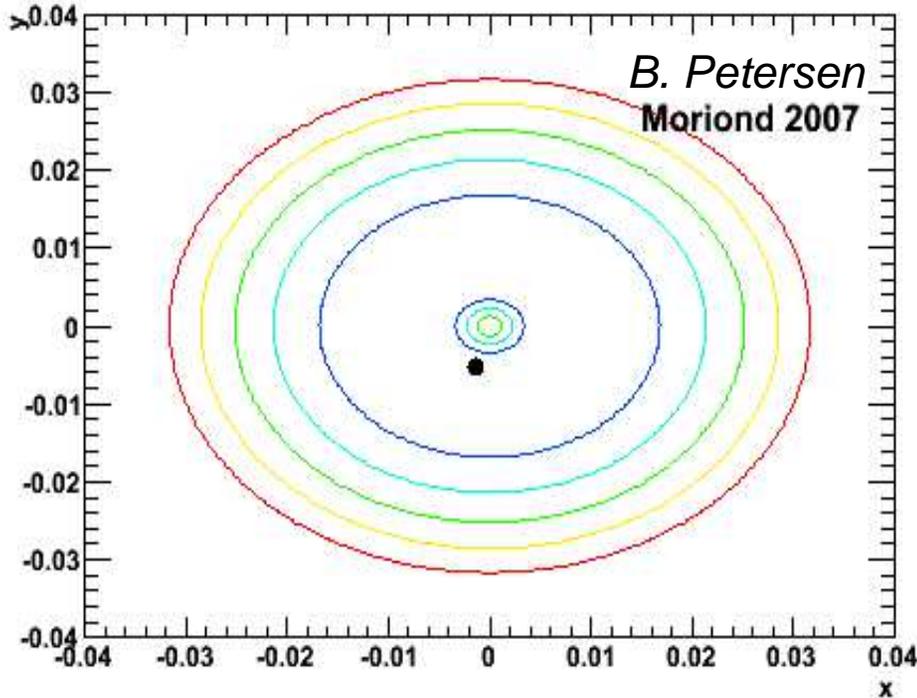
# What have we learned?



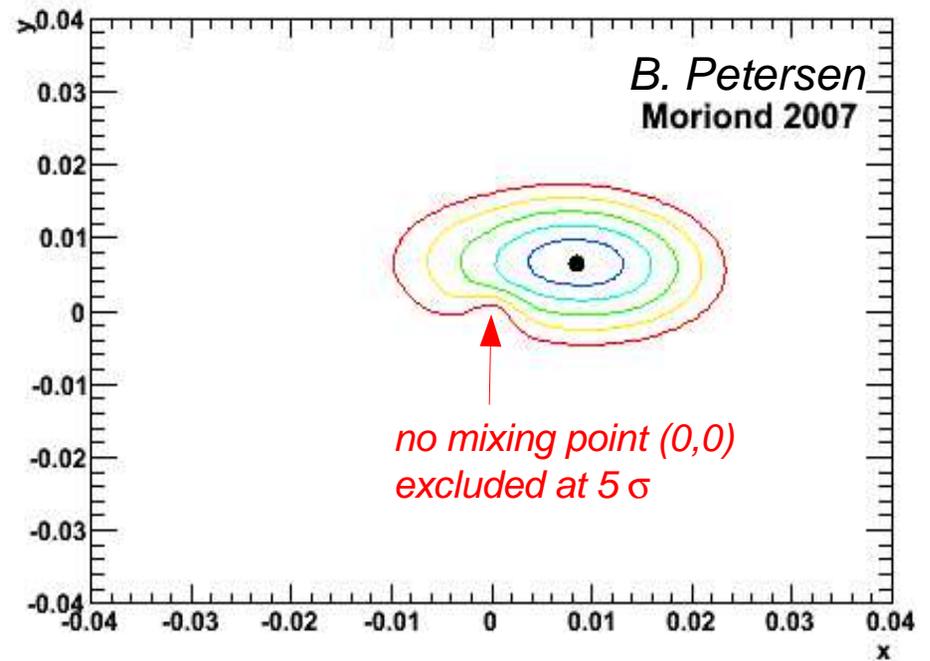
# What have we learned?

All  $D^0(t) \rightarrow K^+ \pi^-$  measurements, allowing strong phase  $\delta$  to always take its preferred value (for a given  $x$  and  $y$ ):

Adding  $-2 \ln \mathcal{L}$  functions from semileptonic decays,  $K^+ \pi^-$ ,  $K_S \pi \pi$ ,  $y_{CP}$ ,  $K^+ \pi^- \pi^0$ ,  $K^+ \pi^- \pi^+ \pi^-$ ,  $\psi(3770)$ :

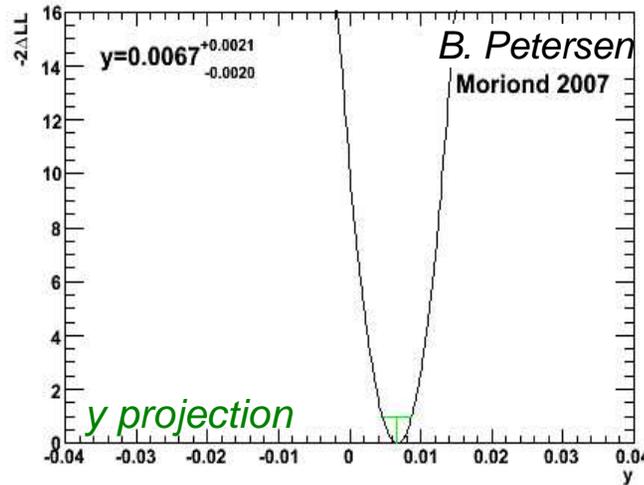
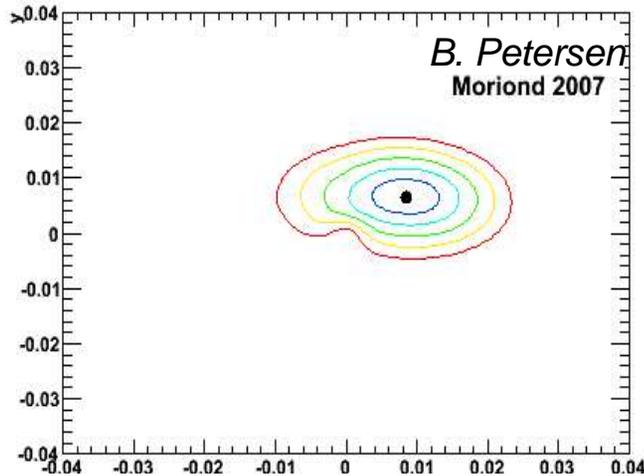


$-2 \ln \mathcal{L}$

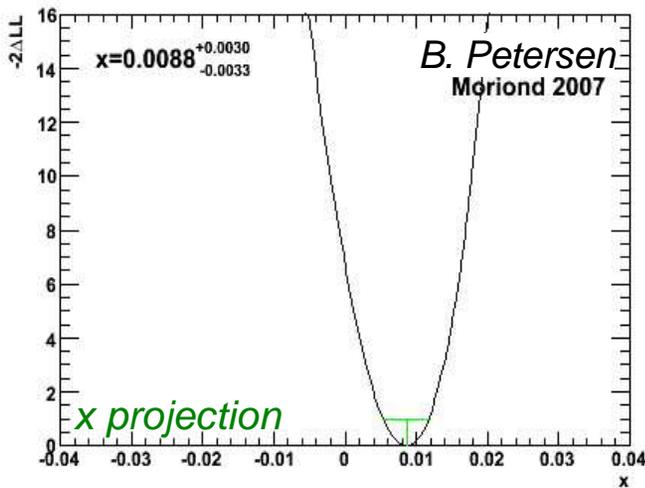


# What have we learned?

All data [semileptonic decays,  $K^+\pi^-$ ,  $K_S\pi\pi$ ,  $y_{CP}$ ,  $K^+\pi^-\pi^0$ ,  $K^+\pi^-\pi^+\pi^-$ ,  $\psi(3770)$ ]:



$x = (0.88 \pm 0.33)\%$   
 (2.7 $\sigma$  above zero)  
 $y = (0.67 \pm 0.20)\%$   
 (3.4 $\sigma$  above zero)



## Conclusions:

Evidence is consistent and convincing that  $D^0$ 's mix; affect is dominated by non-perturbative processes ( $y$ ); may be new physics in  $x$ ; need more data & better theoretical calculations to tell.

Since  $y_{CP}$  is positive, CP-odd state is longer-lived (like other neutral meson systems); but positive  $x/y$  implies CP-odd is lighter