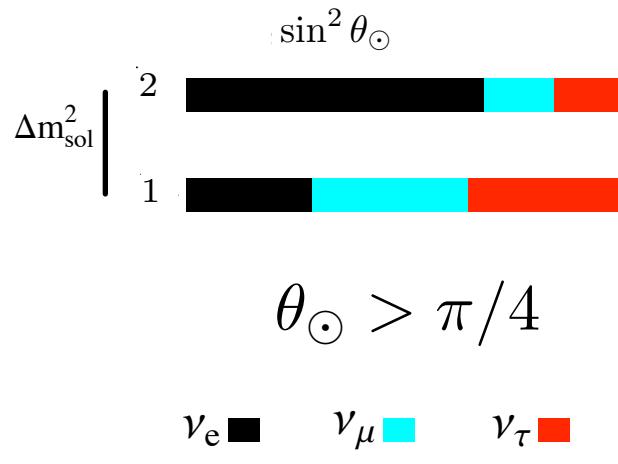


# $\theta_{13}$ & Beyond Nu Worlds

Stephen Parke  
Fermilab  
Feb 23, 2006

## Solar Summary:

- ${}^8\text{Boron}$ : born where  $\nu_e = \nu_2$  remain  $\nu_2$ 's forever (no oscillations)
- pp and  ${}^7\text{Be}$ : full averaged vacuum oscillations  $\Rightarrow 2/3 \nu_1$  and  $1/3 \nu_2$
- Solar hierarchy determined by matter effect.  
( $P_{ee} < 1/2$  impossible for one hierarchy)



Solar matter effects put more of the neutrino into  $\nu_2$ .

This raises the survival probability above vacuum value since  $\nu_2$  has more  $\nu_e$ . But the minimum of  $P_{ee}$  in vacuum is  $1/2$ .

For this hierarchy  $P_{ee}^{\text{matter}} \geq P_{ee}^{\text{vac}} \geq 1/2$

But  $P_{ee}^{SNO} = 0.347 \pm 0.038 < 1/2$

This solar hierarchy EXCLUDED !!!.

<http://theory.fnal.gov/people/parke/TALKS/2006>

What happens to the neutrino oscillation length  
in the semi-classical limit,  $\hbar \rightarrow 0$  ?

- $L_{osc} \rightarrow \infty$
- $L_{osc} \rightarrow 0$
- Other

$$\Delta = \frac{\delta m^2 L}{4 \hbar c E} \quad \Rightarrow \quad L_{osc} = 4\pi \hbar c E / \delta m^2$$

So in the limit  $\hbar \rightarrow 0$  then  $L_{osc} \rightarrow 0$   
same as  $\delta m^2 \rightarrow \text{large} !!!$

and

$W^+ \rightarrow e^+ \nu_1$  with probability  $\cos^2 \theta_\odot$   
 $W^+ \rightarrow e^+ \nu_2$  with probability  $\sin^2 \theta_\odot$

compare quark sector !

## The $\nu$ Standard Model

- 3 light ( $m_i < 1$  eV) Majorana Neutrinos:

$\Rightarrow$  only 2  $\delta m^2$

$$|\delta m_{atm}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2 \text{ and } \delta m_{solar}^2 \sim +8.0 \times 10^{-5} \text{ eV}^2$$

- Only Active flavors (no steriles):

$e, \mu, \tau$

- Unitary Mixing Matrix:

3 angles ( $\theta_{12}, \theta_{23}, \theta_{13}$ ), 1 Dirac phase ( $\delta$ ),

2 Majorana phases ( $\alpha_2, \alpha_3$ )

$$|\nu_\alpha\rangle_{flavor} = U_{\alpha i} |\nu_i\rangle_{mass}.$$

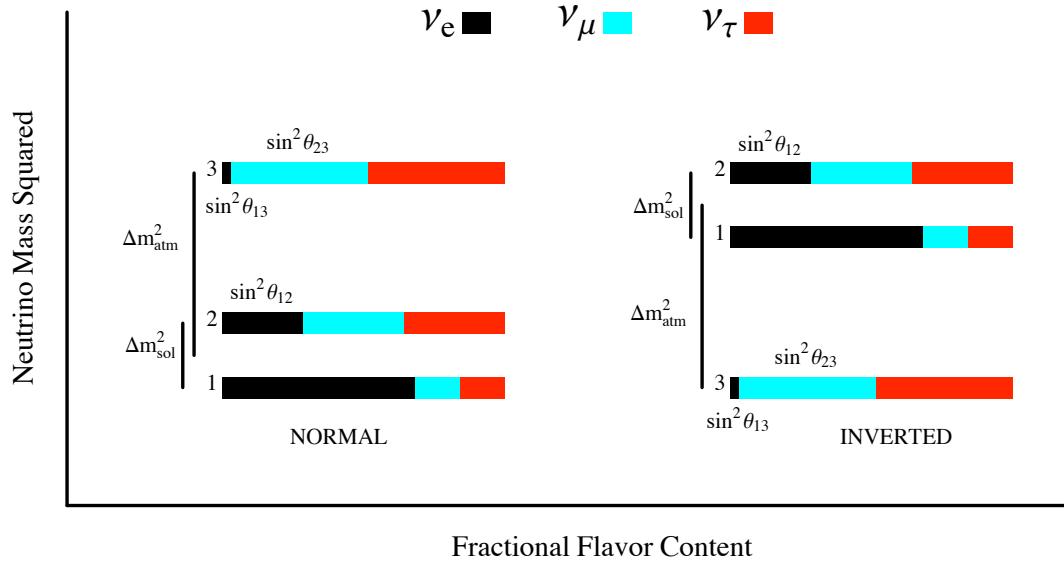
$$\begin{pmatrix} 1 & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & & \\ & 1 & \\ & -s_{13}e^{i\delta} & \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & \\ -s_{12} & c_{12} & \\ & & 1 \end{pmatrix} \begin{pmatrix} 1 & e^{i\alpha} & \\ & e^{i\beta} & \end{pmatrix}$$

In oscillation phenomena,

the phases  $\alpha_2$ ,  $\alpha_3$  are unobservable ( $U_{\alpha i} U_{\beta i}^*$ ) and also the value of  $m_{lite}$  is irrelevant ( $\delta m^2$ )

$$= \begin{pmatrix} c_{13}c_{12} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{13}s_{23}c_{12}e^{i\delta} & c_{23}c_{12} - s_{13}s_{23}s_{12}e^{i\delta} & c_{13}s_{23} \\ s_{23}s_{12} - s_{13}c_{23}c_{12}e^{i\delta} & -s_{23}c_{12} - s_{13}c_{23}s_{12}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

# (12)-Sector:



## (12) Parameters: SNO, KamLAND, SK

$$\delta m_{21}^2 = +8.0 \pm 0.8 \times 10^{-5} \text{ eV}^2$$

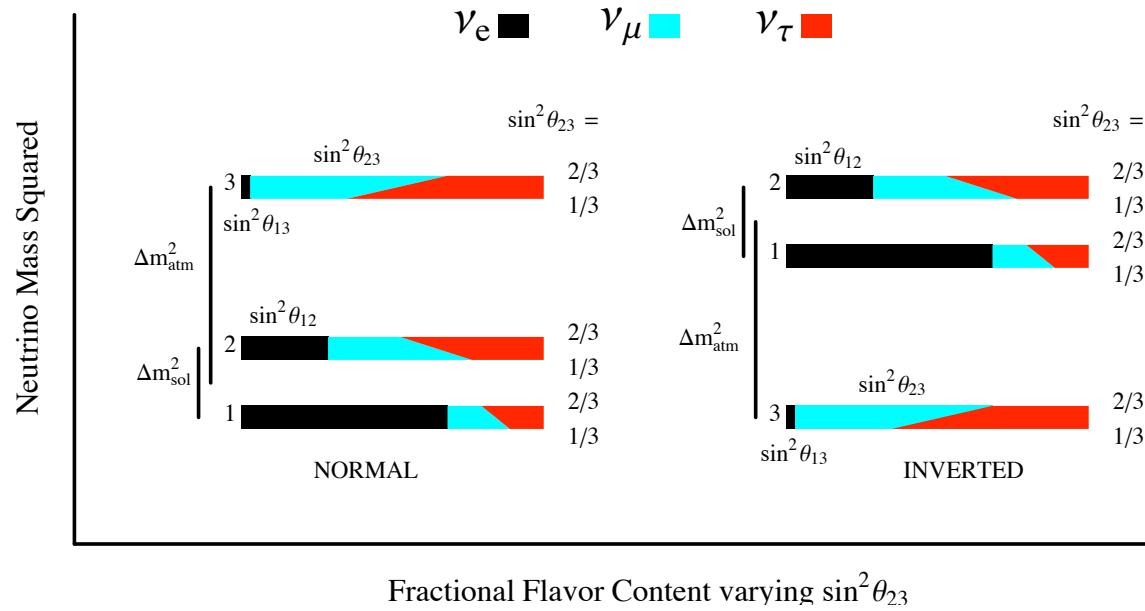
$$0.25 < \sin^2 \theta_{12} < 0.37$$

$\sin^2 \theta_{12} \geq \frac{1}{2}$  excluded at  $> 5 \sigma$ !

sign of  $\delta m_{21}^2$  determined at this C.L.

# (23)-Sector:

Mena + SP hep-ph/0312131



## (23) Parameters: SK, K2K

$$|\delta m_{32}^2| = 1.5 - 3.4 \times 10^{-3} \text{ eV}^2$$

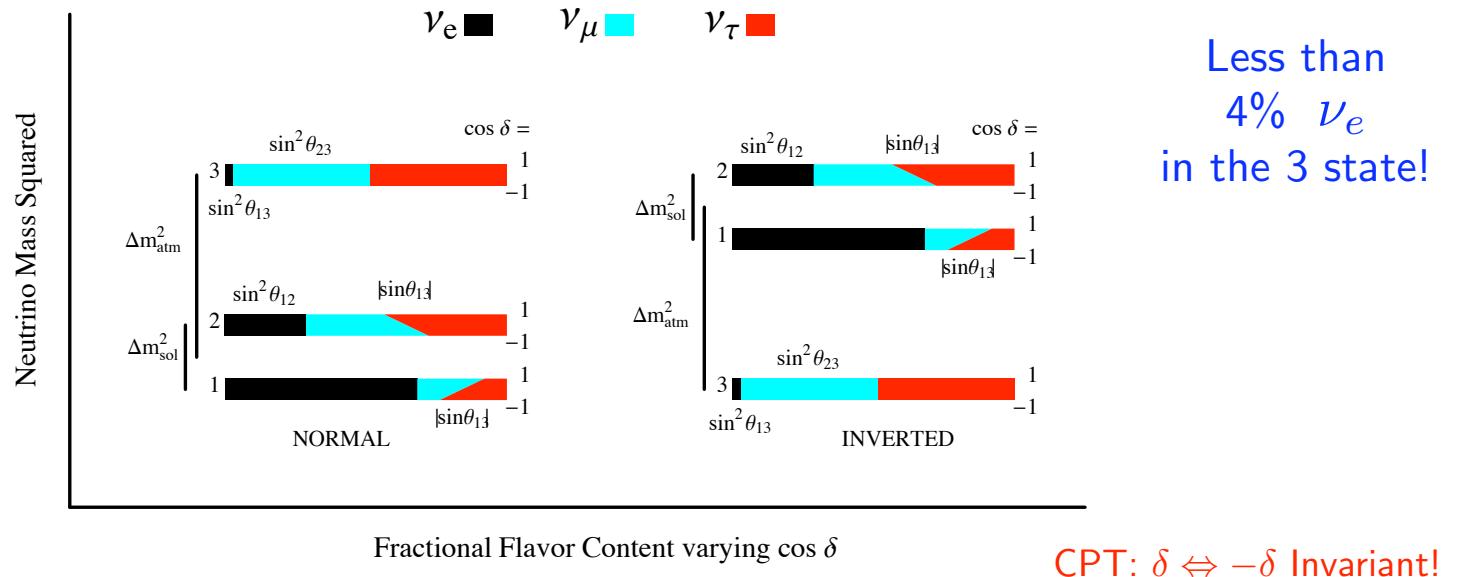
$$0.36 < \sin^2 \theta_{23} < 0.64$$

(obtained from  $\sin^2 2\theta_{23} > 0.91$ )

Magnitude of  $\delta m_{32}^2$  and  $\sin^2 \theta_{23}$  not as well known!

Sign of  $\delta m_{32}^2$  Unknown !!!

# (13)-Sector:



## (13) Parameters: Chooz, SK, K2K

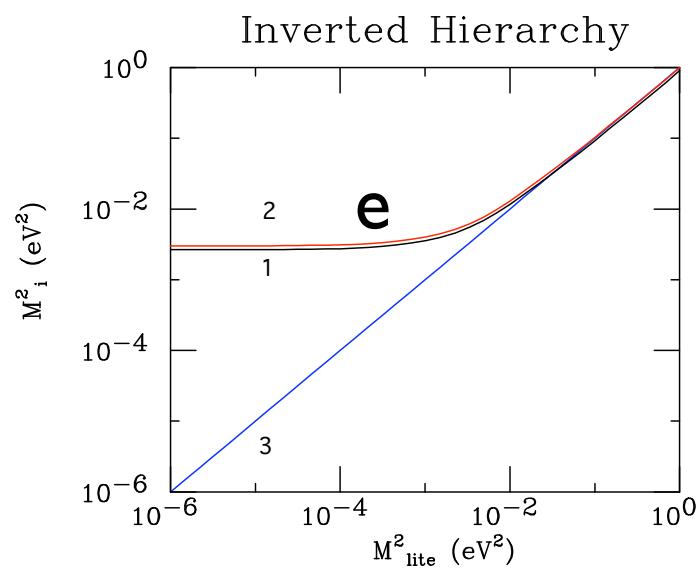
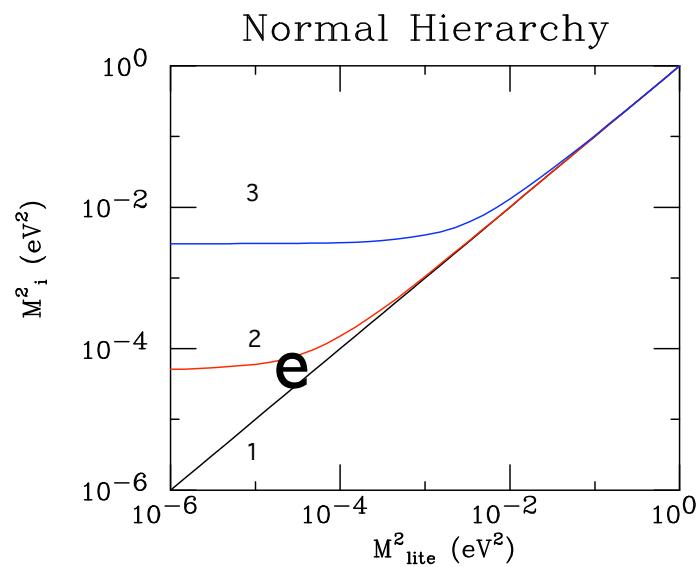
$$\sin^2 \theta_{13} < 0.03 - 0.05$$

limit  $|\delta m_{32}^2|$  dependent

$$0 \leq \delta_{CP} < 2\pi$$

Unknown!

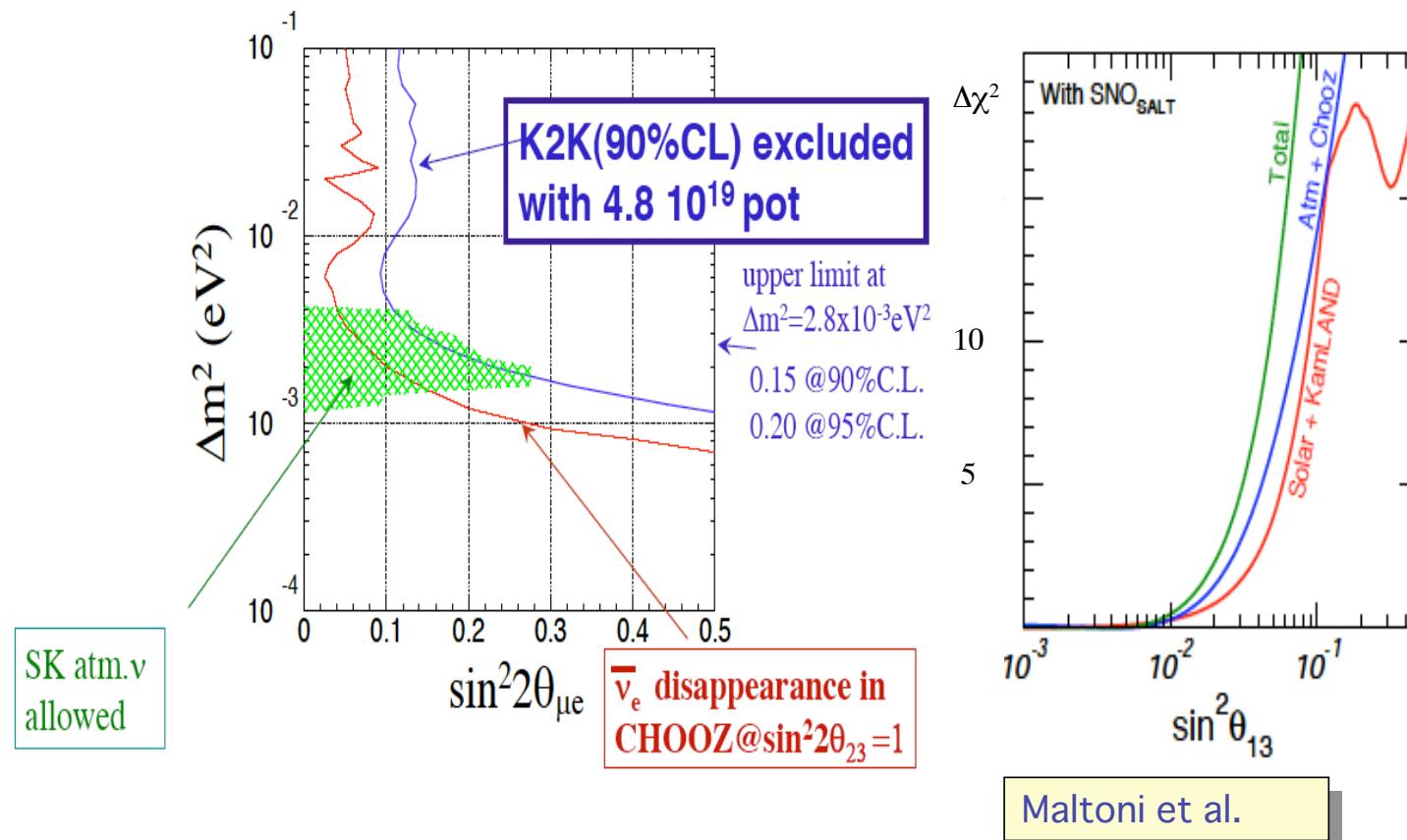
## Masses:



States 1 and 2 are  $\nu_e$  rich.

- $\nu_e$  fraction of  $\nu_3$ :
    - $\sin^2 \theta_{13}$
  - mass hierarchy:
    - sign of  $\delta m_{31}^2$
  - CP violation:
    - $\sin \delta \neq 0$
- observable

# No indication yet of nonzero $\theta_{13}$ from atmospheric, solar and terrestrial $\nu$

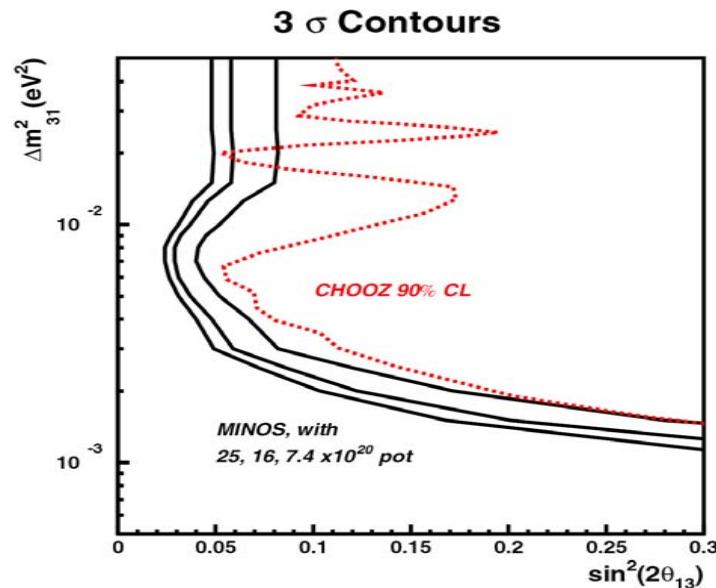


Chooz bound  $\sin^2 \theta_{13} < 0.04$

## Quest for $\nu_e$ fraction in $\nu_3$ : $\sin^2 \theta_{13}$

- Current LBL (MINOS)
- Atmospheric Neutrinos
- Low and High Energy Solar Neutrinos
- Supernova Neutrinos
- Short Baseline Reactor (Double Chooz, ...)
- Future Long Baseline (T2K, NuMI, BNL2?, ...)
- Neutrino Factories
- Beta Beams

# MINOS:



$\nu_e$  appearance  $\Rightarrow$  non-zero  $\theta_{13}$

Can improve CHOOZ limit by  $\sim 2$   
with adequate protons

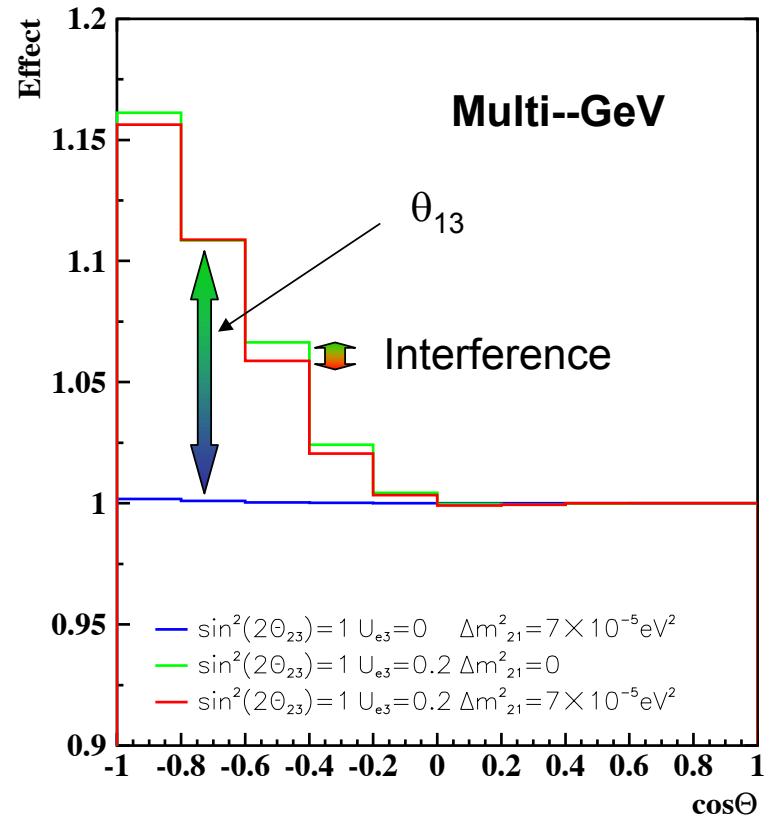
Has some sensitivity to  $\nu_e$  above backgrounds.

Primary goal is to measure  $|\delta m_{32}^2|$  to 10%

## ● Atmospheric Neutrinos

SK - Suzuki

- $|U_{e3}|=0.2$
- $\Delta m_{12}^2=7 \times 10^{-5} \text{ eV}^2$
- Interference



- Low and High Energy Solar Neutrinos

Goswami + Smirnov  
hep-ph/0411359

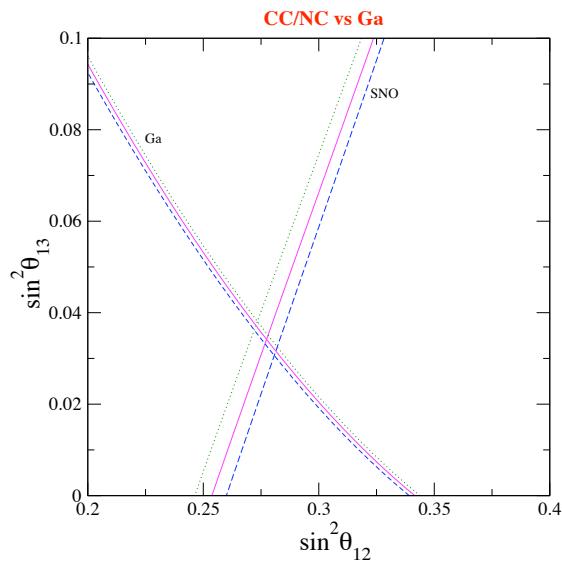


Figure 6: The iso-contours of CC/NC = 0.31 at SNO and  $Q_{Ge} = 68.1$  SNU in Ga experiments in the  $\sin^2 \theta_{12} - \sin^2 \theta_{13}$  plane for different values of  $\Delta m_{21}^2$ :  $\Delta m_{21}^2 = 9 \cdot 10^{-5} \text{ eV}^2$  - the dotted lines;  $\Delta m_{21}^2 = 8 \cdot 10^{-5} \text{ eV}^2$  - the solid lines;  $\Delta m_{21}^2 = 7 \cdot 10^{-5} \text{ eV}^2$  - the dashed lines.

$$\begin{aligned}\sin^2 \theta_{\odot}^{8B} &\approx \sin^2 \theta_{12} - 0.9 \sin^2 \theta_{13} \\ \sin^2 \theta_{\odot}^{8pp} &\approx \sin^2 \theta_{12} + 1.5 \sin^2 \theta_{13}\end{aligned}$$

$$\sin^2 \theta_{\odot}^{8pep} \approx \sin^2 \theta_{12} + (0.5???) \sin^2 \theta_{13}$$

$$\frac{CC}{NC} \sim \cos^2 \theta_{13} \sin^2 \theta_{12} + \dots$$

$$\sin^2 \theta_{13} \uparrow \Rightarrow \sin^2 \theta_{12} \uparrow$$

$$Ga \sim \cos^4 \theta_{13} \cos^4 \theta_{12} + \dots$$

$$\sin^2 \theta_{13} \uparrow \Rightarrow \sin^2 \theta_{12} \downarrow$$

Nunokawa, Zukanovich + SP  
hep-ph/0601198

$\bar{\nu}_e$  (reactor) Disappearance:  $e^{-iE_i t} \Rightarrow e^{-im_i^2 L/2E}$

$$\begin{aligned} P_{ee} &= |U_{e1}^* e^{-im_1^2 L/2E} U_{e1} + U_{e2}^* e^{-im_2^2 L/2E} U_{e2} + U_{e3}^* e^{-im_3^2 L/2E} U_{e3}|^2 \\ &= |U_{e1}|^4 + \dots \\ &\quad + 2|U_{e1}|^2|U_{e2}|^2 \cos 2\Delta_{21} + \dots \end{aligned}$$

$$\cos 2\Delta_{ji} = 1 - 2 \sin^2 \Delta_{ji}$$

$$\begin{aligned} P_{ee} &= 1 - 4|U_{e3}|^2|U_{e1}|^2 \sin^2 \Delta_{31} - 4|U_{e3}|^2|U_{e2}|^2 \sin^2 \Delta_{32} \\ &\quad - 4|U_{e2}|^2|U_{e1}|^2 \sin^2 \Delta_{21} \end{aligned}$$

$$\Delta_{31} \approx \Delta_{atm} \approx \Delta_{32}$$

$$P_{ee} = 1 - 4|U_{e3}|^2(1 - |U_{e3}|^2) \sin^2 \Delta_{atm} - 4|U_{e2}|^2|U_{e1}|^2 \sin^2 \Delta_{\odot}$$

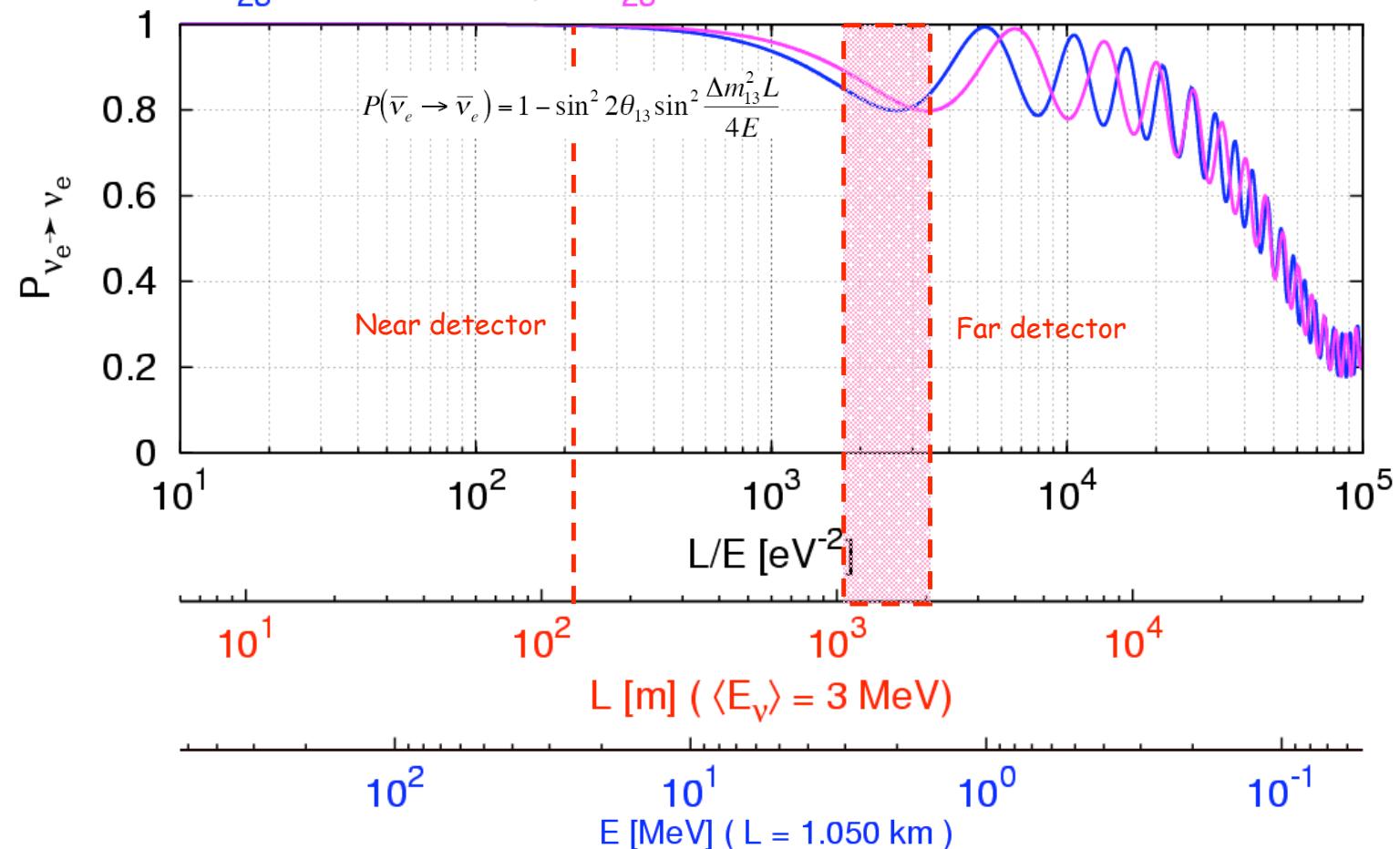
$$\Delta = \frac{\delta m^2 L}{4E}$$

$$P_{ee} = 1 - \sin^2 2\theta_{13} \sin^2 \Delta_{atm} - \cos^4 \theta_{13} \sin^2 2\theta_\odot \sin^2 \Delta_\odot$$

$$\delta m_{atm}^2 \approx \cos^2 \theta_\odot \delta m_{31}^2 + \sin^2 \theta_\odot \delta m_{32}^2$$

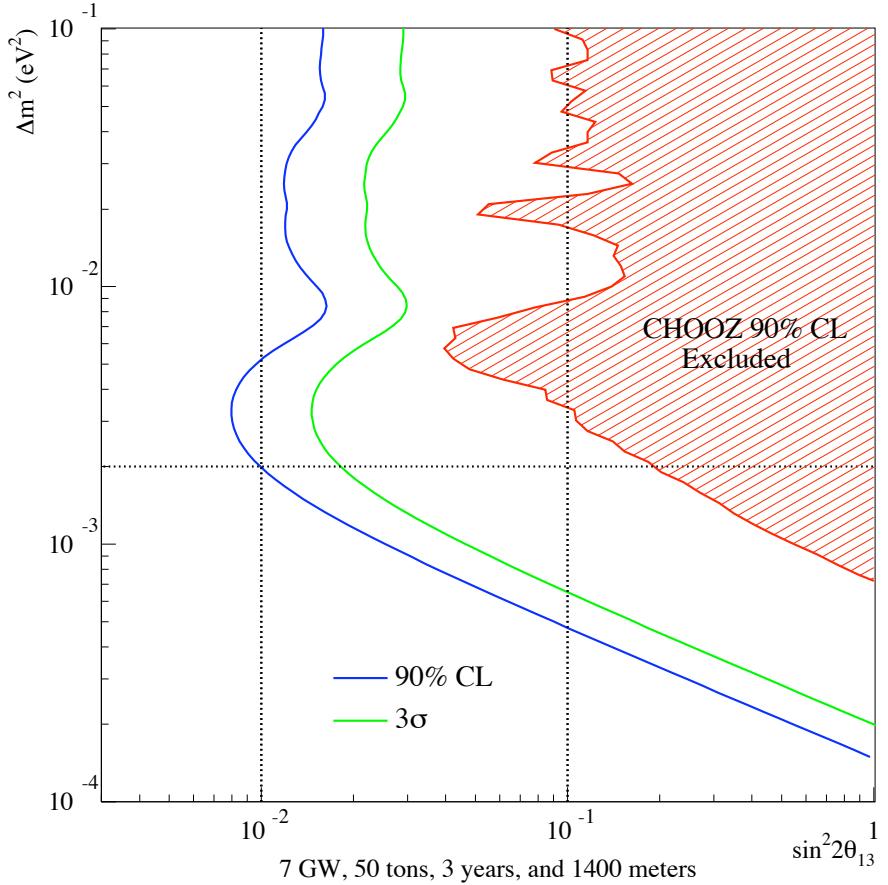
$$\Delta m_{12}^2 = 7.2 \cdot 10^{-5} \text{ eV}^2; \cos \theta_{12} = 0.8; \sin \theta_{13} = 0.23$$

$$\Delta m_{23}^2 = 2.5 \cdot 10^{-3} \text{ eV}^2; \Delta m_{23}^2 = 2.0 \cdot 10^{-3} \text{ eV}^2$$



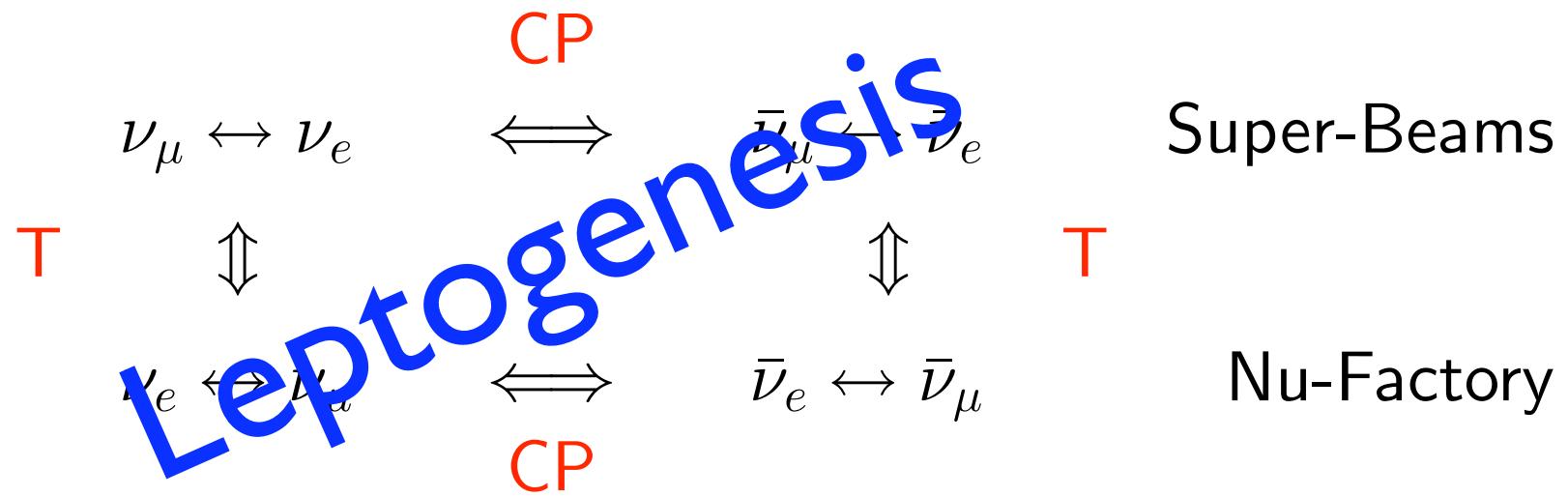
$$P_{ee} = 1 - \sin^2 2\theta_{13} \sin^2 \Delta_{atm} - \cos^4 \theta_{13} \sin^2 2\theta_\odot \sin^2 \Delta_\odot$$

Clean measurement of  
 $\sin^2 2\theta_{13}$  down to 0.01  
 Systematics limit  
 experiment:  
 Could be “quick” and  
 “cheap” but ...



J. Link, Columbia

# Leptonic CP and T Violation in Neutrino Oscillations



Vacuum:

$$\underline{\nu_\mu \rightarrow \nu_e}$$

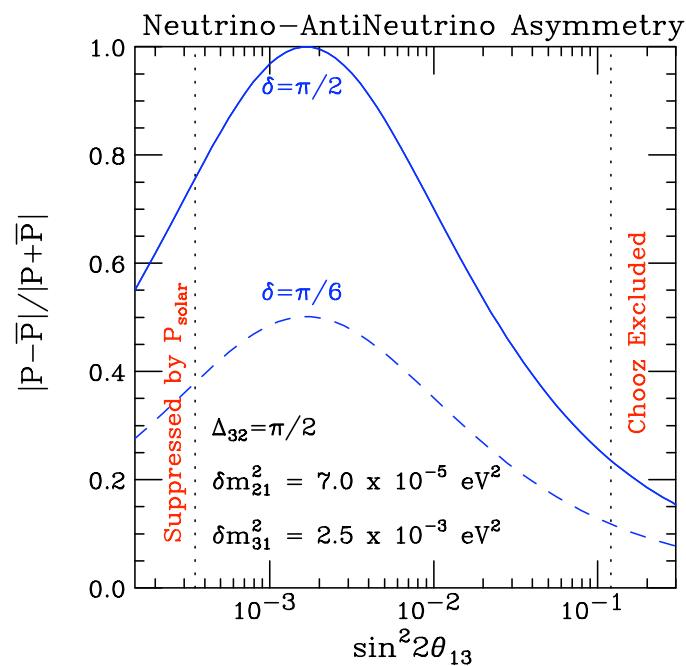
$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &= |U_{\mu 1}^* e^{-im_1^2 L/2E} U_{e 1} + U_{\mu 2}^* e^{-im_2^2 L/2E} U_{e 2} + U_{\mu 3}^* e^{-im_3^2 L/2E} U_{e 3}|^2 \\
 &= |2U_{\mu 3}^* U_{e 3} \sin \Delta_{31} e^{-i\Delta_{32}} + 2U_{\mu 2}^* U_{e 2} \sin \Delta_{21}|^2 \\
 &= |\sqrt{P_{atm}} e^{-i(\Delta_{32} + \delta)} + \sqrt{P_{sol}}|^2 \\
 e^{-iE_i t} \Rightarrow e^{-im_i^2 L/2E} &\quad \text{CP violation !!!} \quad \delta \rightarrow -\delta \text{ for } \bar{\nu}
 \end{aligned}$$

where  $\sqrt{P_{atm}} = \sin \theta_{23} \sin 2\theta_{13} \sin \Delta_{31}$  and  $\sqrt{P_{sol}} \approx \cos \theta_{23} \sin 2\theta_{12} \sin \Delta_{21}$

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &= P_{atm} + 2\sqrt{P_{atm}}\sqrt{P_{sol}} \cos(\Delta_{32} + \delta) + P_{sol} \\
 &\quad \text{CP violation !!!} \quad \delta \rightarrow -\delta \text{ for } \bar{\nu}
 \end{aligned}$$

$$P_{\mu \rightarrow e} \approx | \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} |^2$$

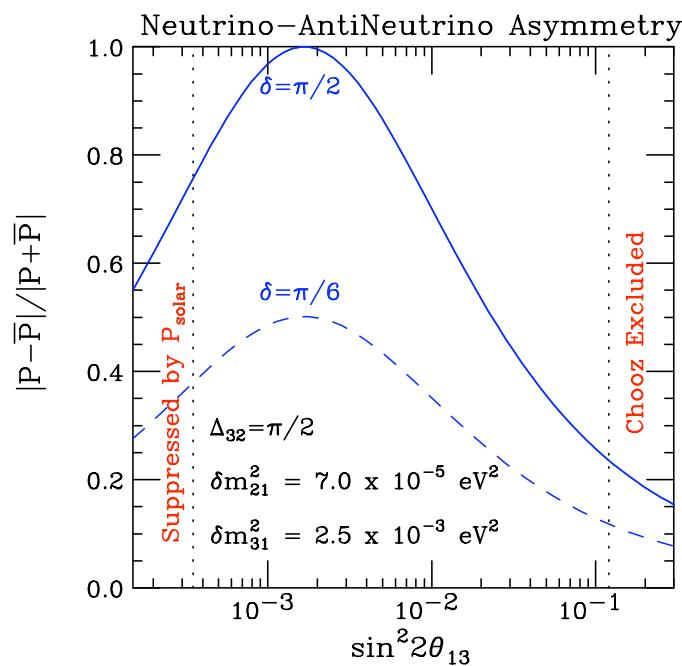
## Asymmetry Peaks:



$$\sqrt{P_{atm}} = \sqrt{P_{sol}}$$

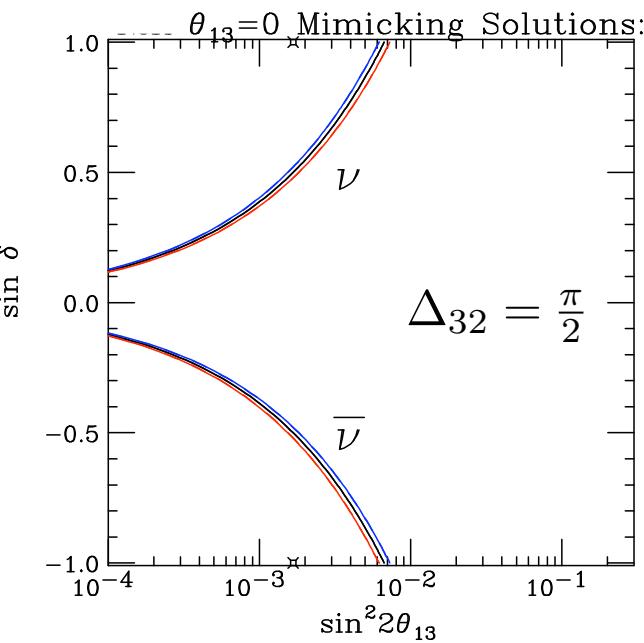
$$P_{\mu \rightarrow e} \approx | \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} |^2$$

## Asymmetry Peaks:



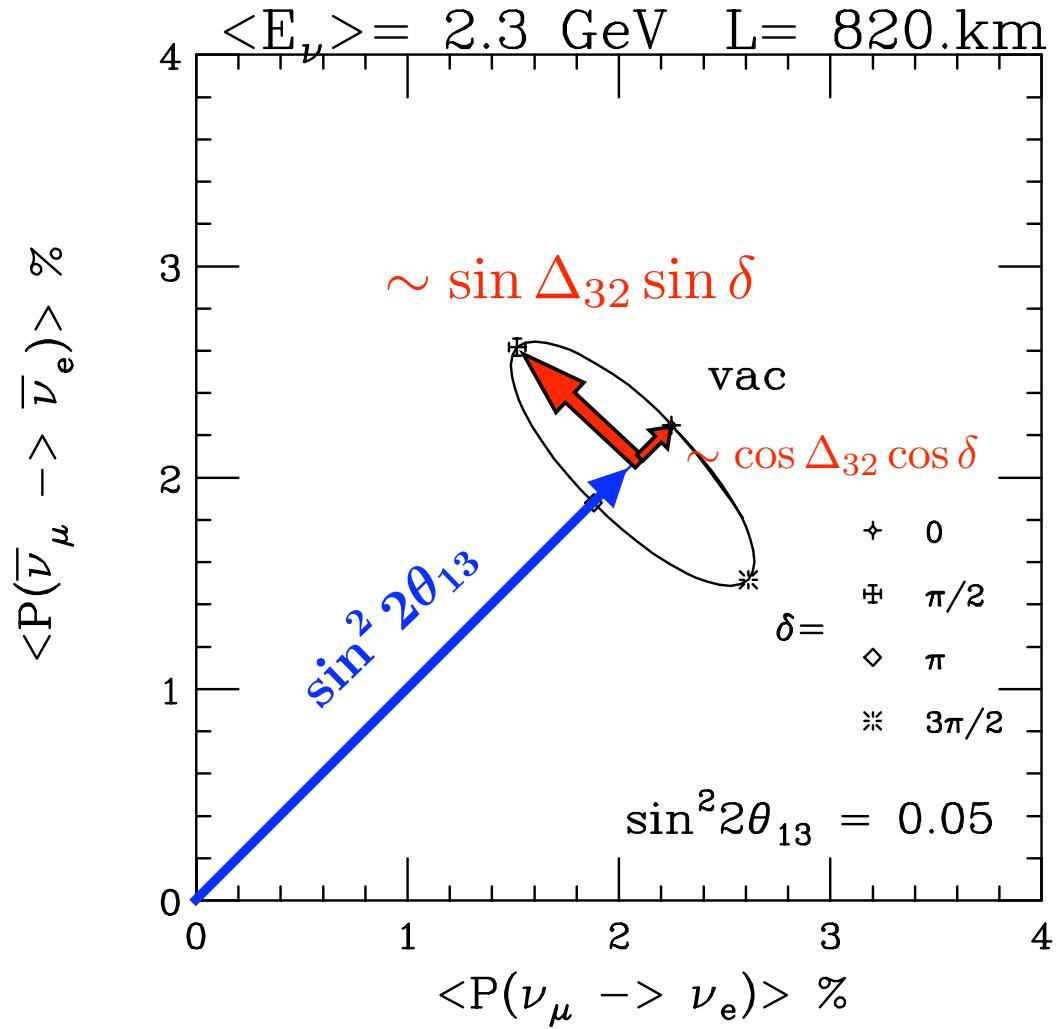
$$\sqrt{P_{atm}} = \sqrt{P_{sol}}$$

## Zero Mimicking Solutions:



$$\sqrt{P_{atm}} = -2\sqrt{P_{sol}} \cos(\Delta_{32} \pm \delta)$$

$$P_{\mu \rightarrow e} \approx | \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} |^2$$



Next Time:

## In Matter:

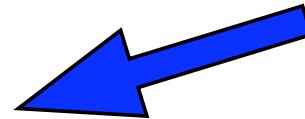
Masses and Mixings in MATTER:  $\delta m_N^2$  and  $\theta^N$

## SUMMARY:

- Majorana or Dirac

- Size  $m_{lite}$

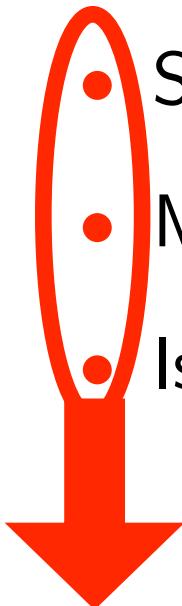
• Size  $\sin^2 \theta_{13}$



Reactor ( $\bar{\nu}_e \rightarrow \bar{\nu}_e$ )

- Mass Hierarchy  $m_3 > or < m_1, m_2$

• Is  $\sin \delta_{CP} \neq 0 ???$  CP violation !!!



Long Baseline ( $\nu_\mu \rightarrow \nu_e$ )

