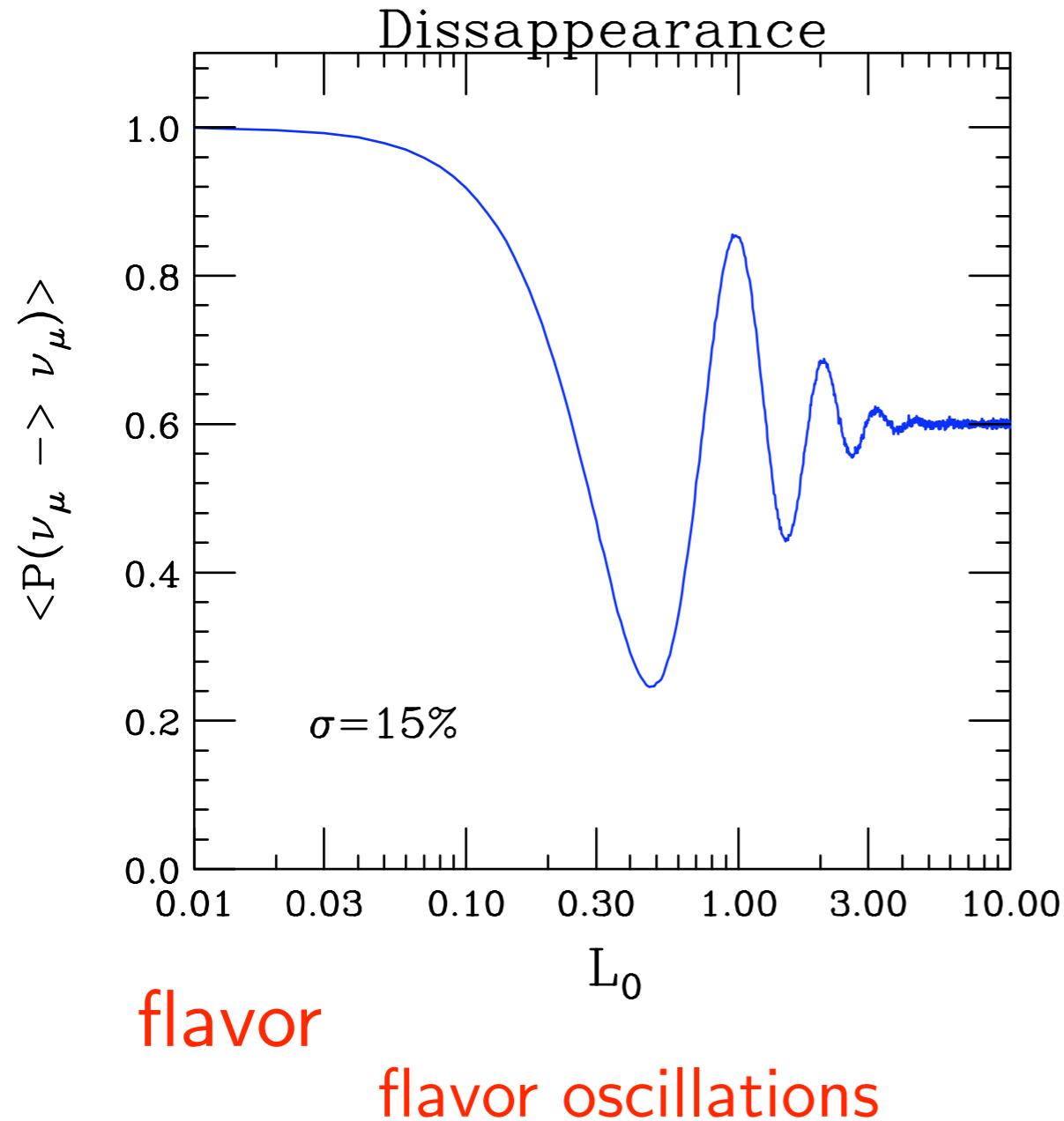


$$\langle P(\nu_\mu \rightarrow \nu_\mu) \rangle = 1 - \sin^2 2\theta \left\langle \sin^2 \frac{\delta m^2 L}{4E} \right\rangle$$

Spread E_ν



$$1 - \sin^2 2\theta \left(\frac{1}{2}\right) = \cos^4 \theta + \sin^4 \theta$$

Understood in terms of probability

$W^+ \rightarrow \mu^+ + \nu_1$ probability $\cos^2 \theta$

$W^+ \rightarrow \mu^+ + \nu_2$ probability $\sin^2 \theta$

probability ν_1 contains ν_μ is $\cos^2 \theta$

probability ν_2 contains ν_μ is $\sin^2 \theta$

effectively incoherent
mass eigenstates

Neutrinos, In and Beyond the Standard Model:

Stephen Parke
Fermilab

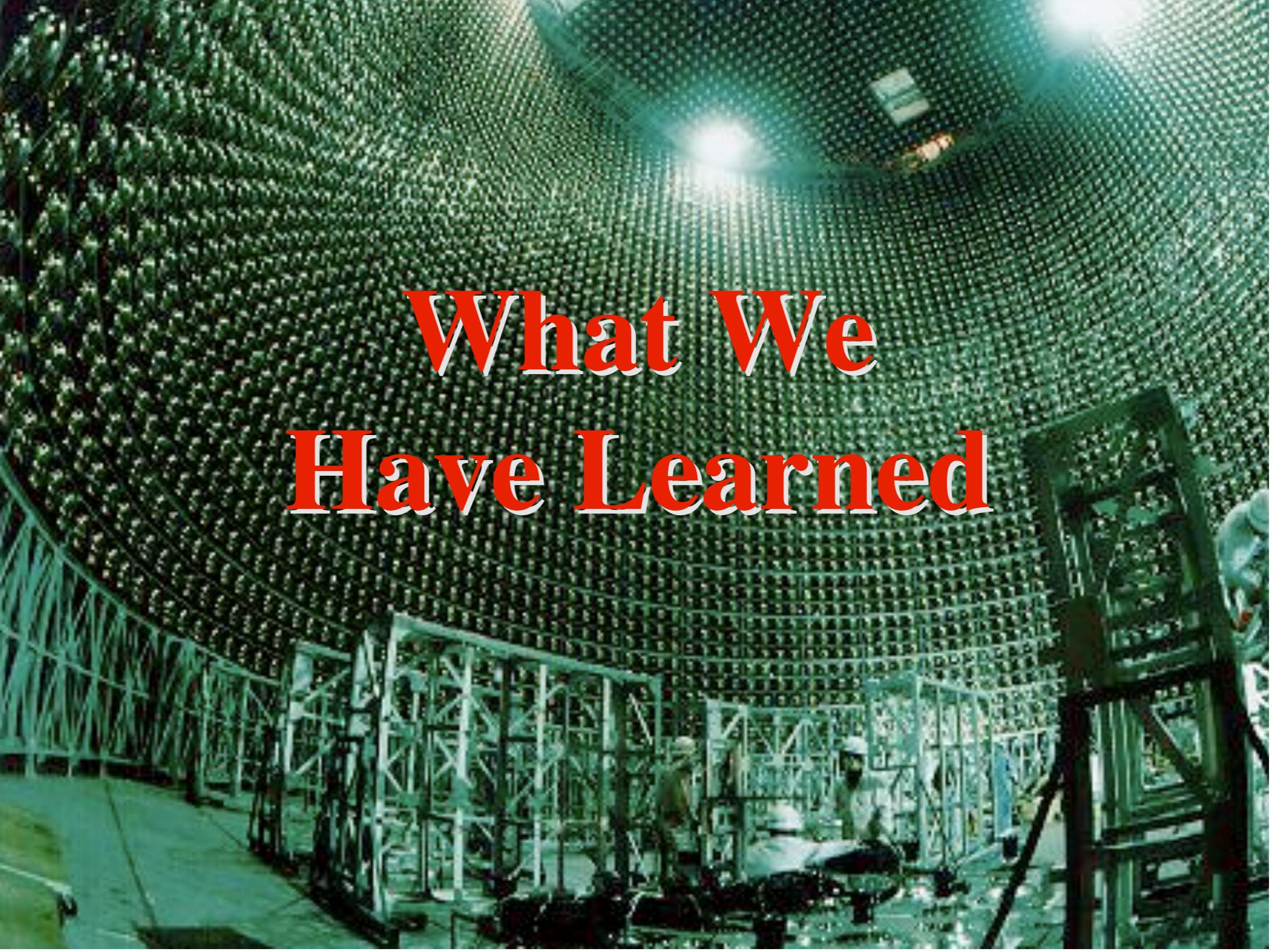
Evidence for Flavor Change:

Evidence for Flavor Change:

*** Atmospheric and Accelerator Neutrinos with $L/E = 500 \text{ km/GeV}$

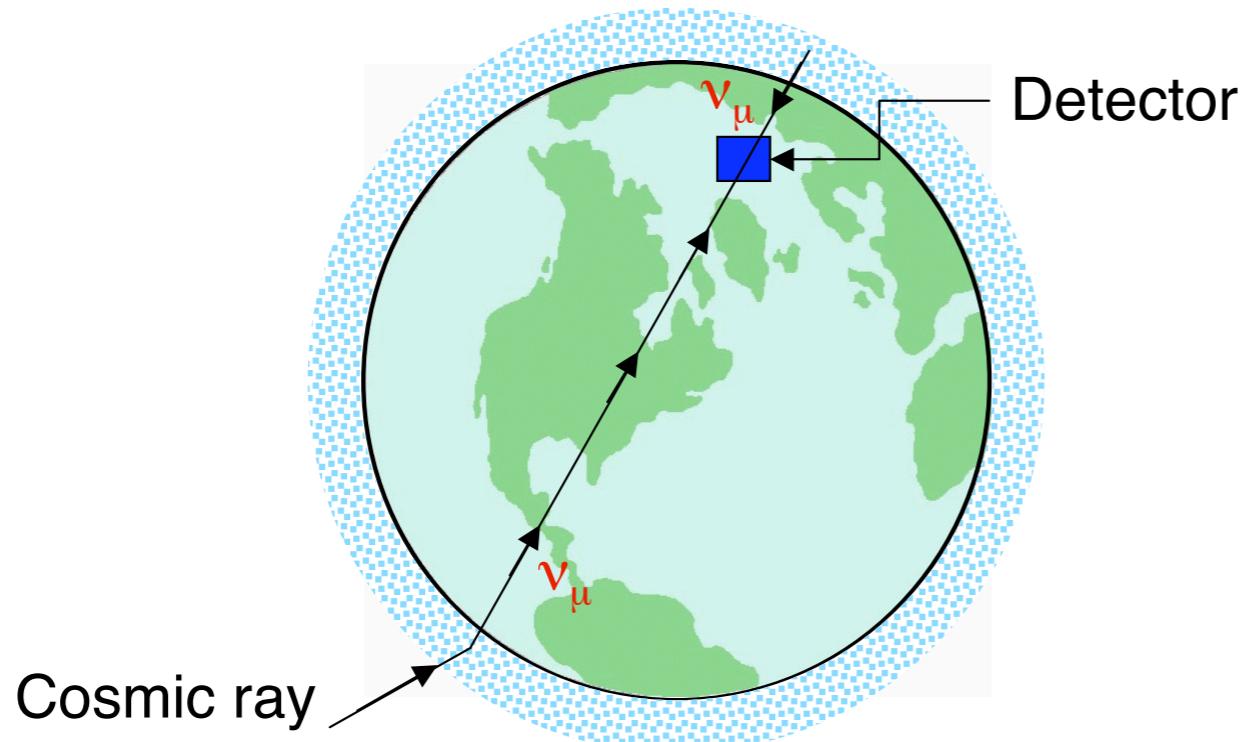
*** Solar and Reactor Neutrinos with $L/E = 15 \text{ km/MeV}$

Neutrinos from Stopped muons $L/E = 2\text{m/MeV}$ (Unconfirmed)



What We Have Learned

Atmospheric Neutrinos

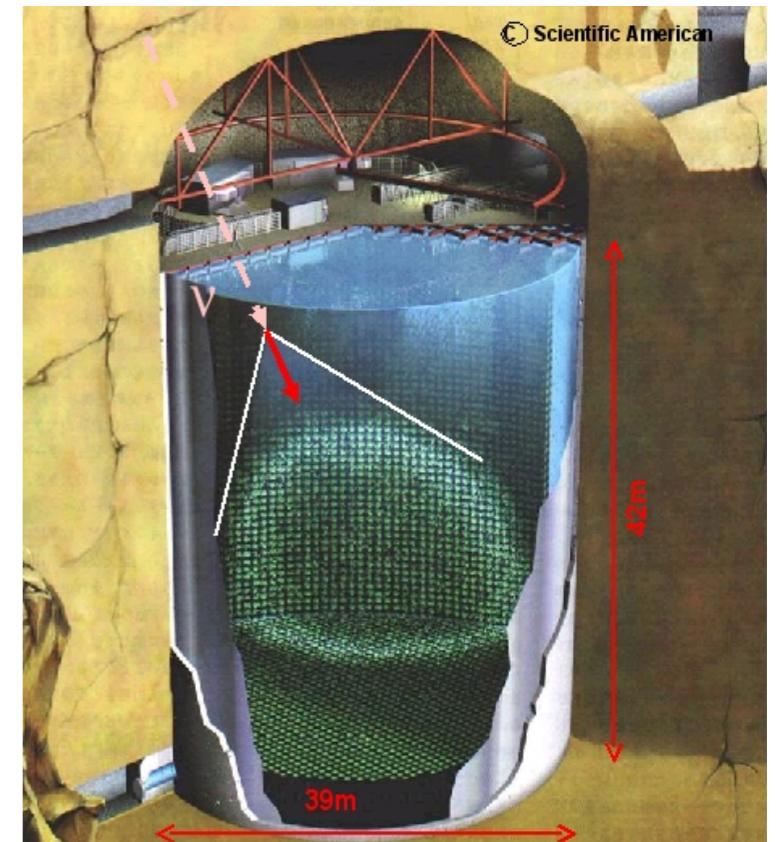


Isotropy of the $\gtrsim 2$ GeV cosmic rays + Gauss' Law + No ν_μ disappearance

$$\Rightarrow \frac{\phi_{\nu_\mu}(\text{Up})}{\phi_{\nu_\mu}(\text{Down})} = 1 .$$

But Super-Kamiokande finds for $E_\nu > 1.3$ GeV

$$\frac{\phi_{\nu_\mu}(\text{Up})}{\phi_{\nu_\mu}(\text{Down})} = 0.54 \pm 0.04 .$$



Half of the upward-going, long-distance-traveling ν_μ are disappearing.

Voluminous atmospheric neutrino data are well described by —

$$\nu_\mu \longrightarrow \nu_\tau$$

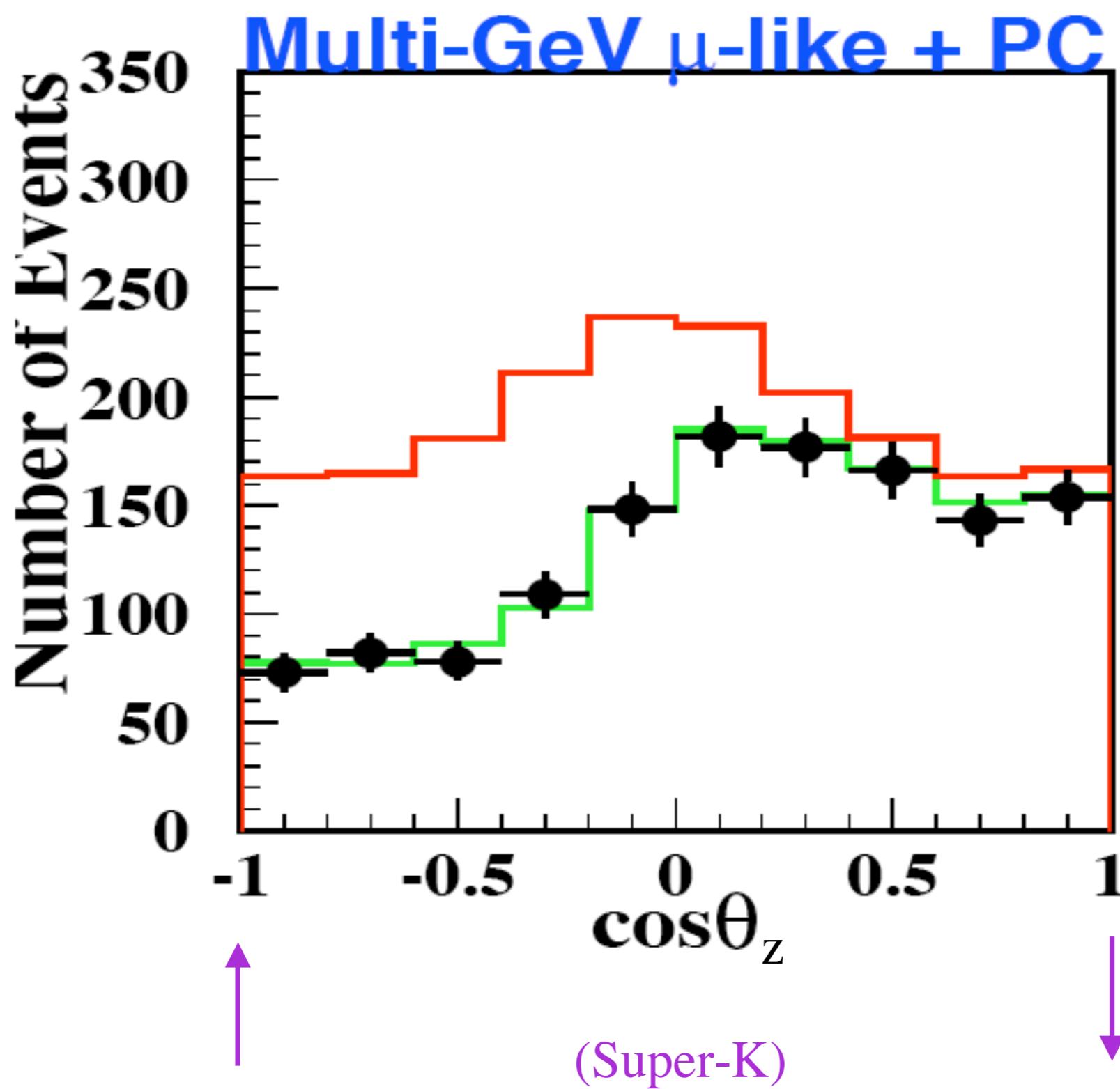
with —

$$1.9 \times 10^{-3} < \Delta m_{\text{atm}}^2 < 3.0 \times 10^{-3} \text{ eV}^2$$

and —

$$\sin^2 2\theta_{\text{atm}} > 0.92$$

(
Super-K
90%CL)



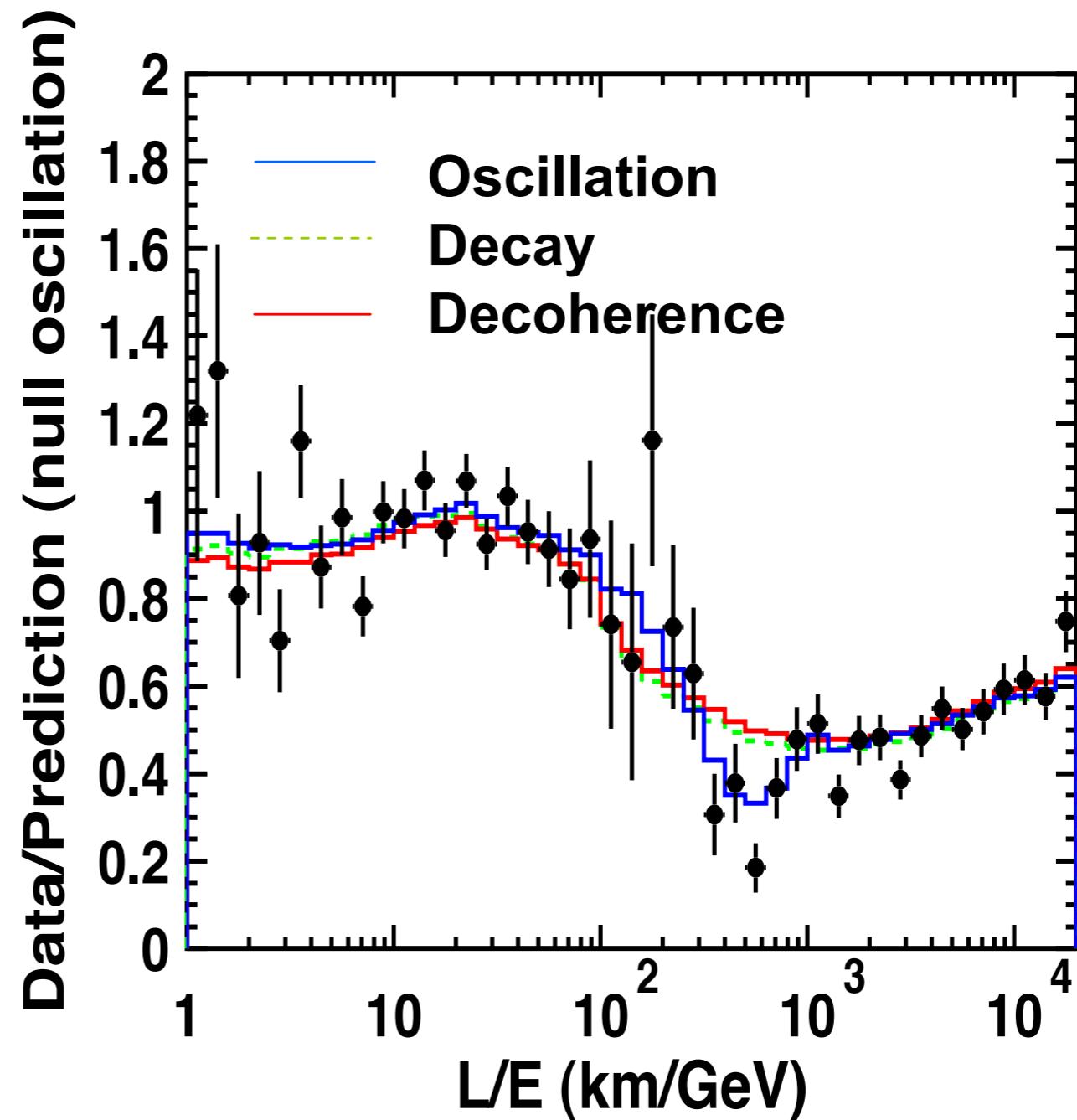
L/E Analysis

❖ Oscillation, decay and decoherence models tested

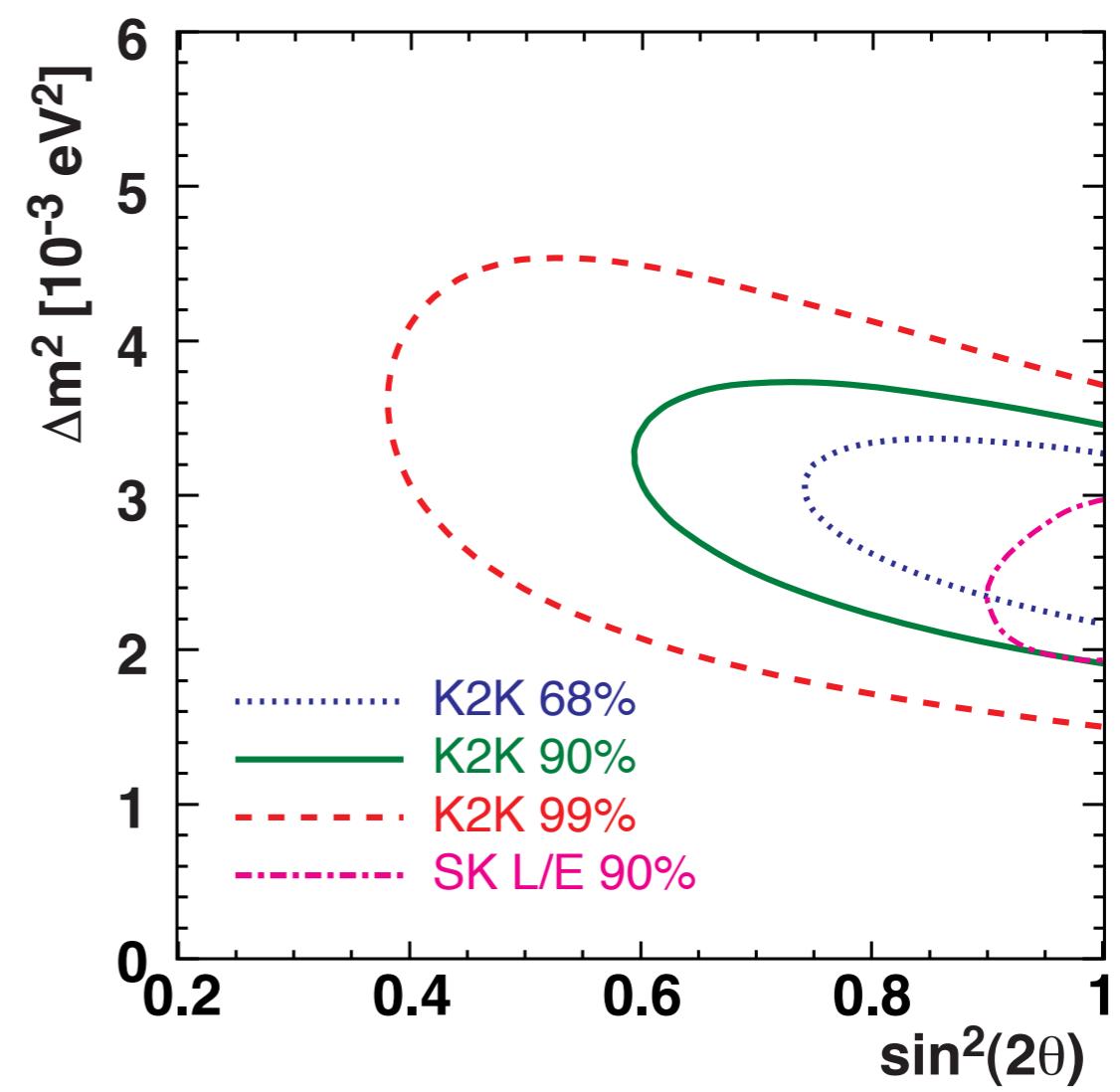
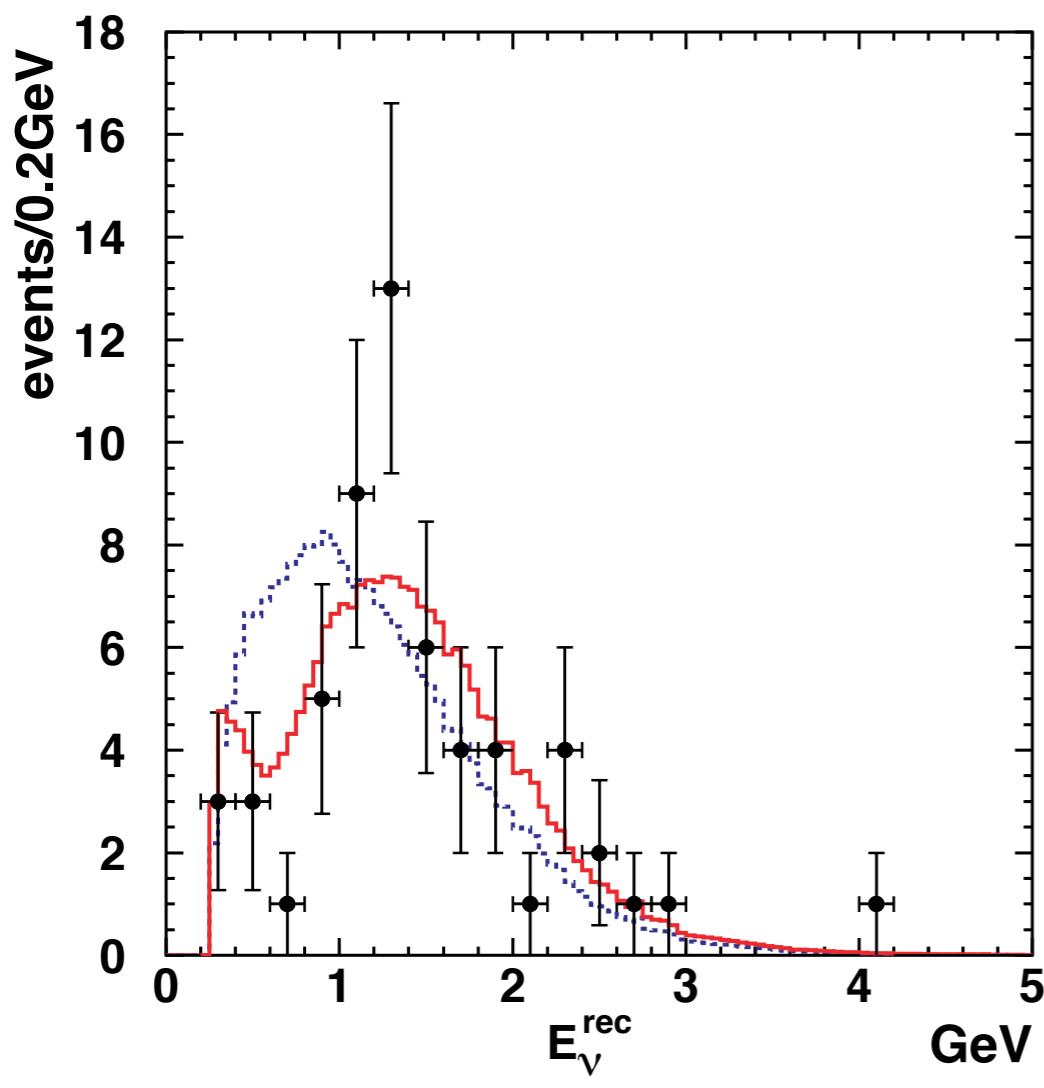
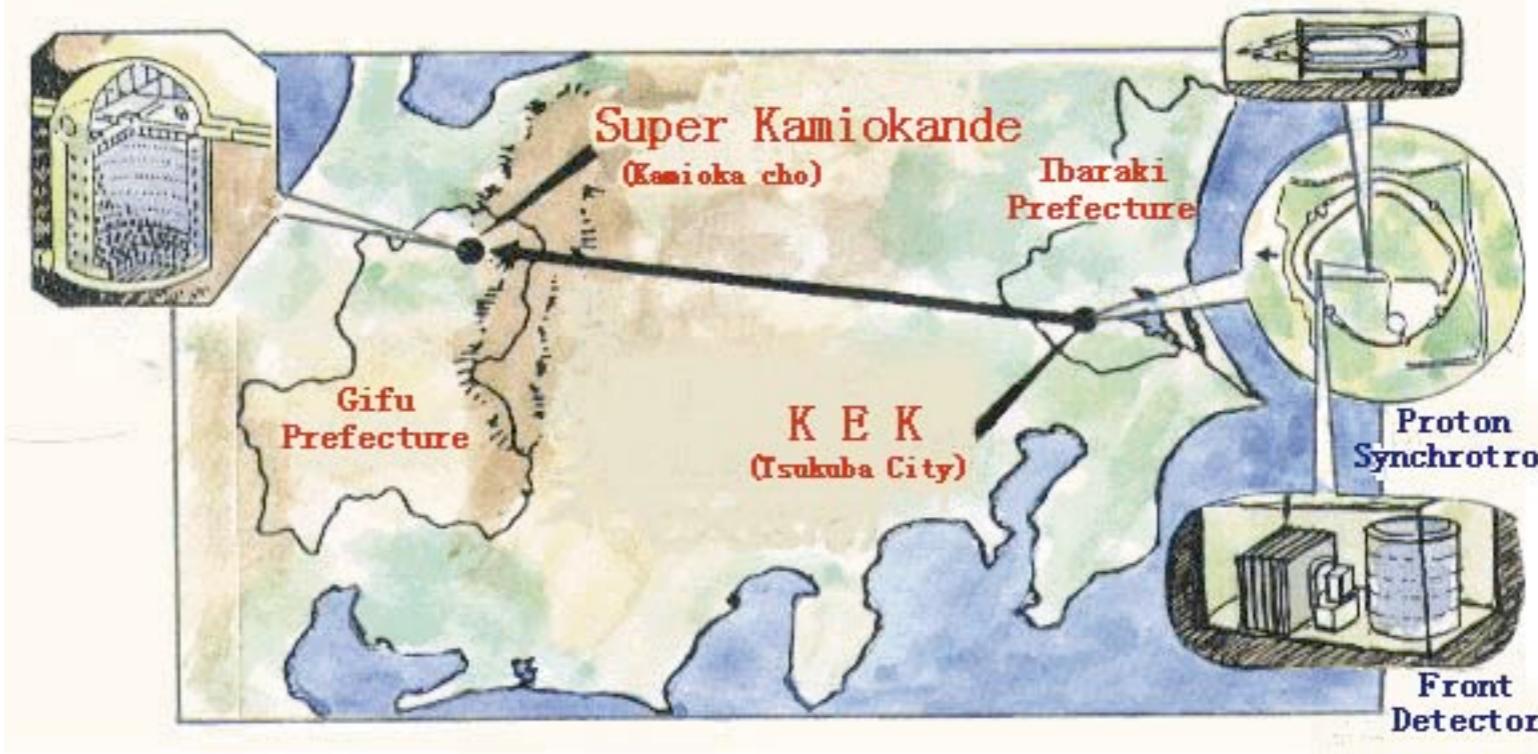
$$\chi^2_{\text{osc}} = 83.9/83$$

$$\chi^2_{\text{dcy}} = 107.1/83, \Delta\chi^2 = 23.2(4.8\sigma)$$

$$\chi^2_{\text{dec}} = 112.5/83, \Delta\chi^2 = 27.6(5.3\sigma)$$

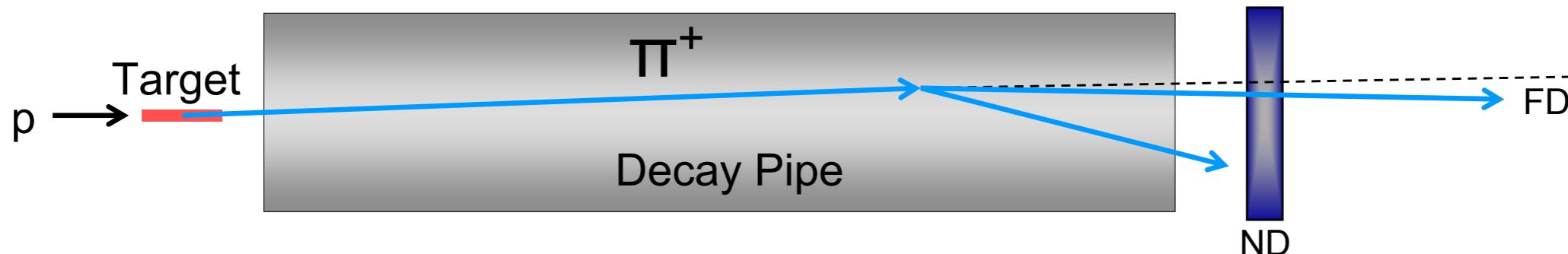


K2K





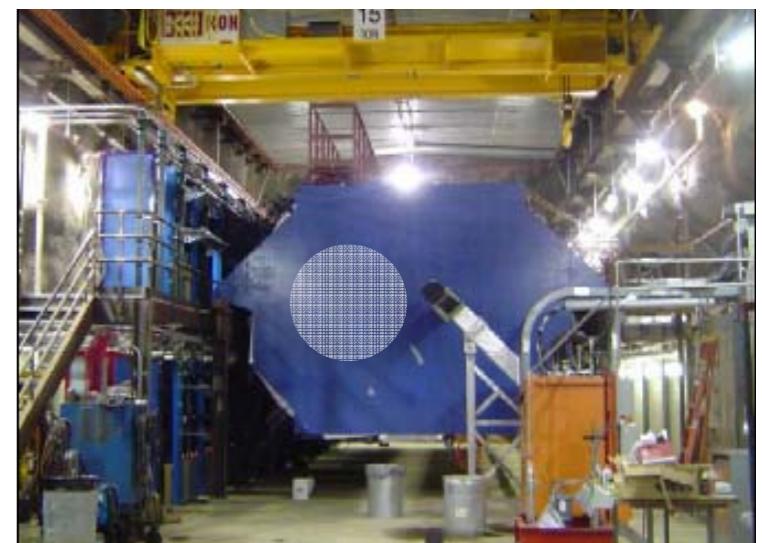
The MINOS Experiment



Fermilab Soudan
↓ 10 km
735 km

Near Detector

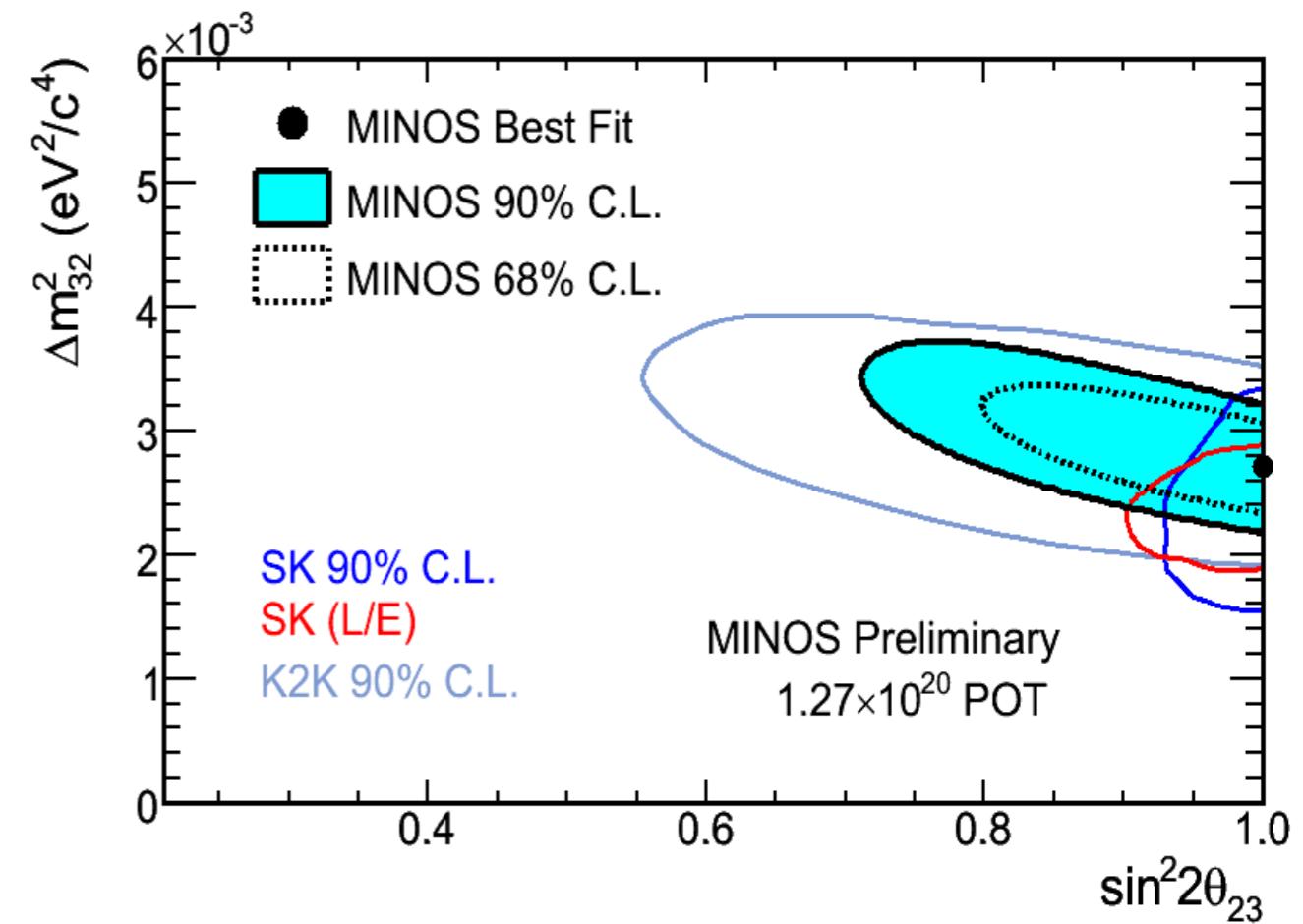
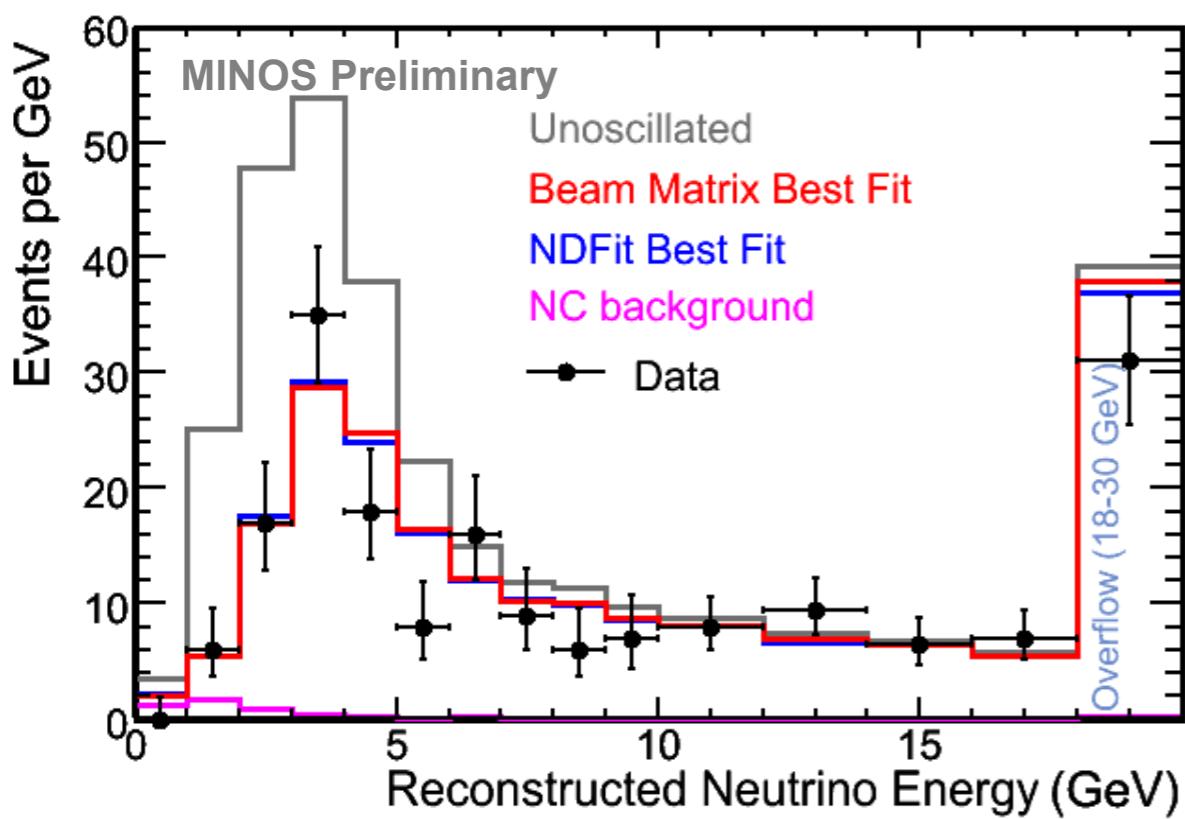
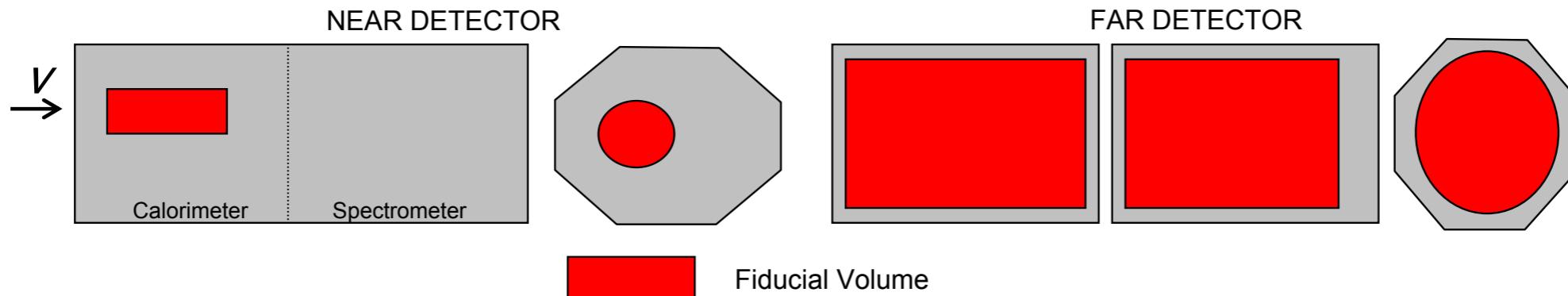
1 kton
 $3.8 \times 4.8 \times 15 \text{ m}^3$
282 steel planes
153 scintillator planes



Far Detector

5.4 kton
 $8 \times 8 \times 30 \text{ m}^3$
484 planes





$$|\Delta m_{32}^2| = 2.72^{+0.38}_{-0.25} (\text{stat}) \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{23} = 1.00_{-0.13} (\text{stat})$$

Normalization = 0.98

$$|\Delta m_{32}^2| = 2.72^{+0.38}_{-0.25} (\text{stat}) \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{23} = 1.00_{-0.13} (\text{stat})$$

Constrained to $\sin^2(2\theta_{23}) \leq 1$
Statistical errors

“Atmospheric” Neutrino Summary

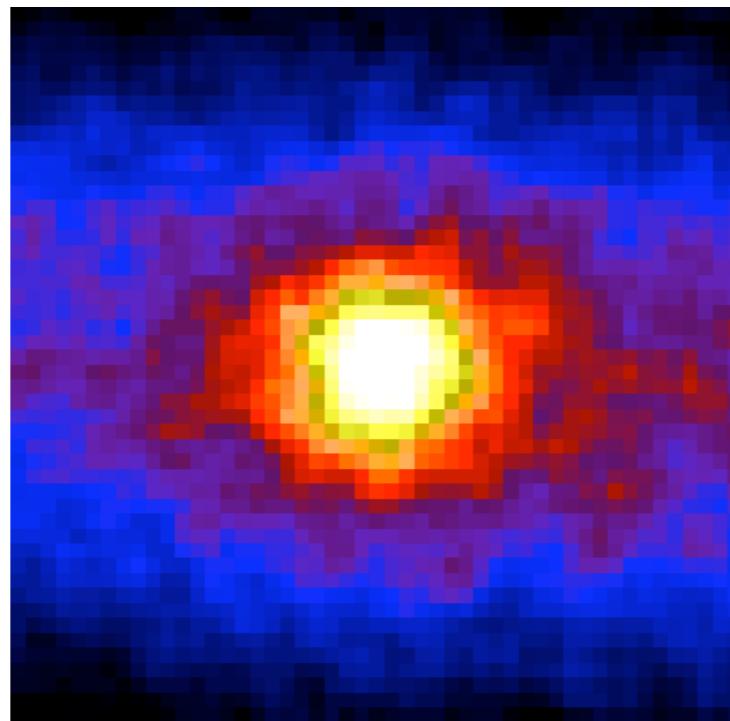
$$\nu_\mu \rightarrow \nu_\tau$$

no evidence of ν_e involvement:

$$\delta m_{atm}^2 = 2.7^{+0.4}_{-0.3} \times 10^{-3} eV^2 \quad L/E = 500 \text{ km/GeV}$$

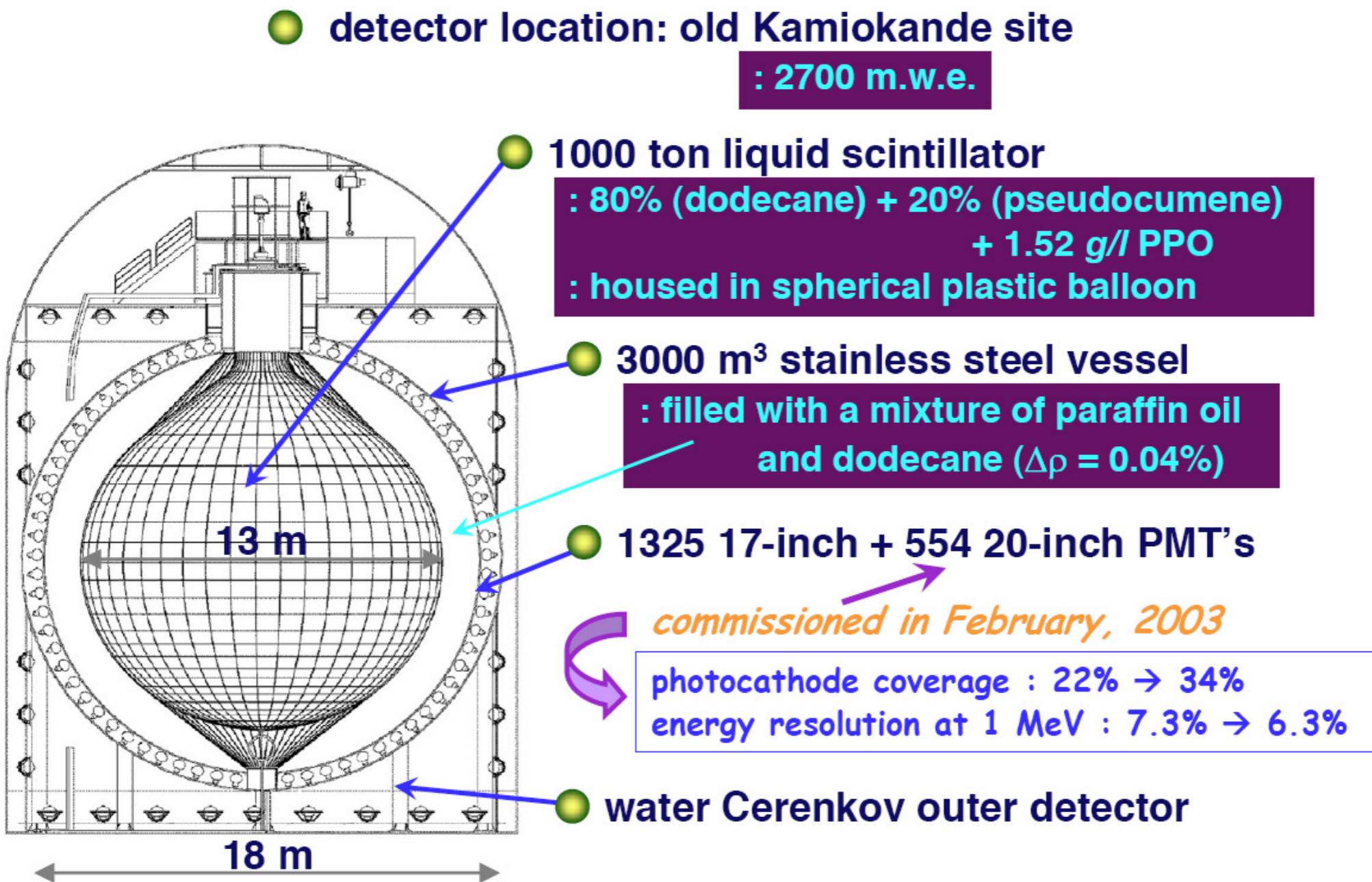
$$\sin^2 2\theta_{atm} > 0.92 \quad \Rightarrow 0.35 < \sin^2 \theta_{atm} < 0.65$$

Solar δm^2

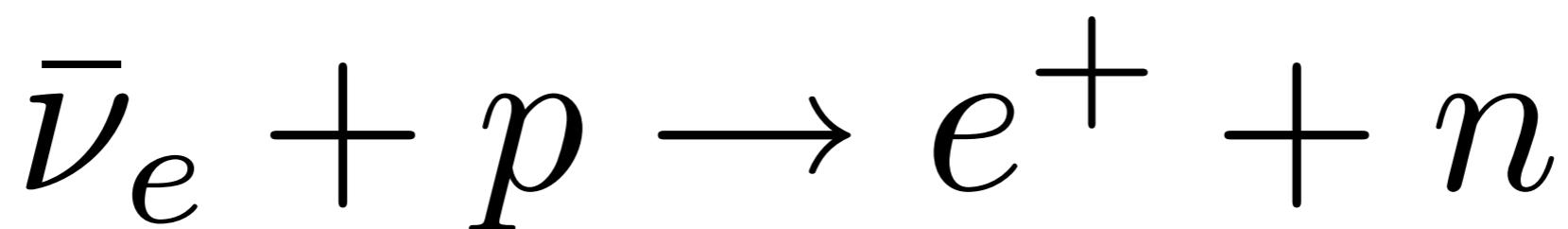
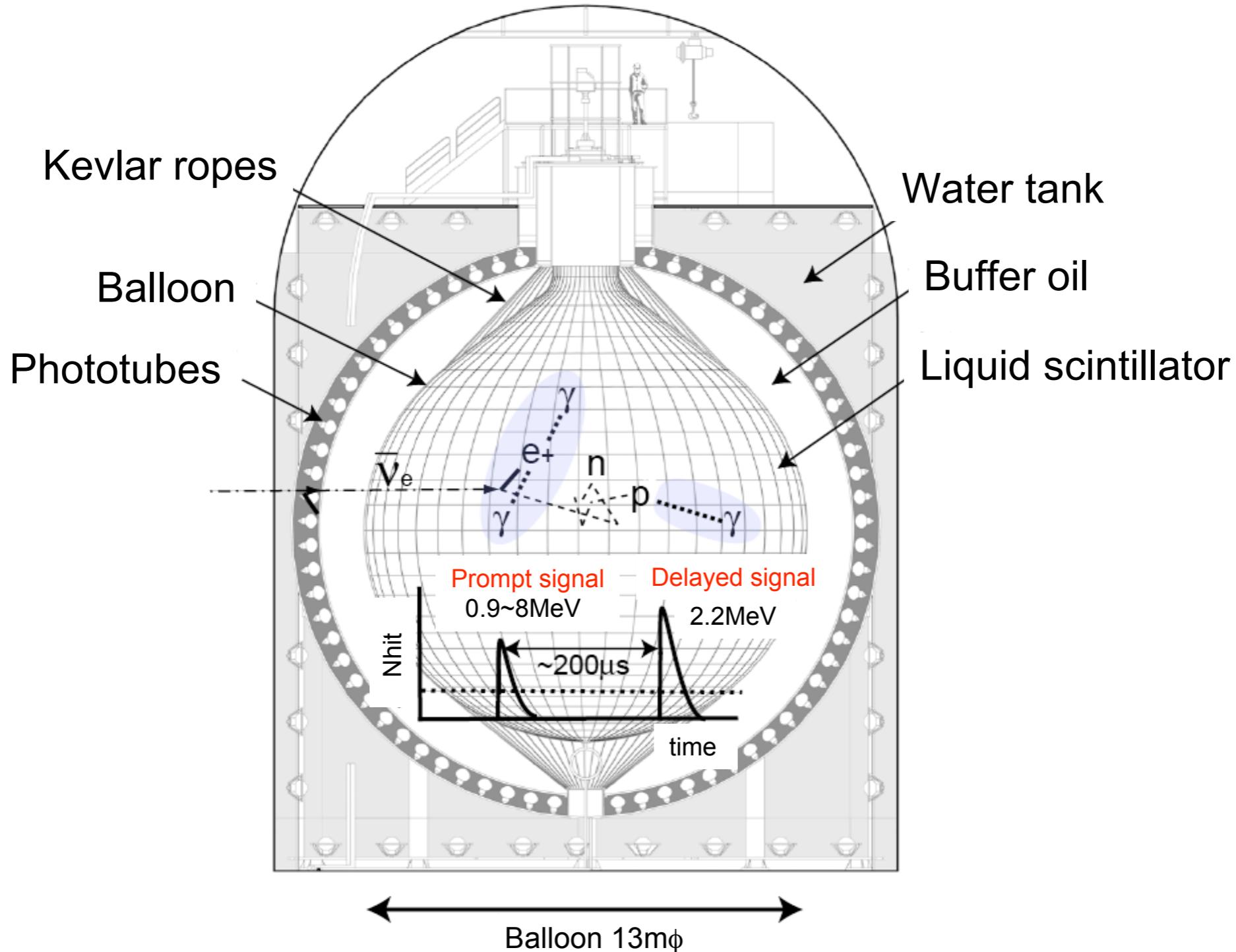


Reactor Neutrinos

KamLAND Detector

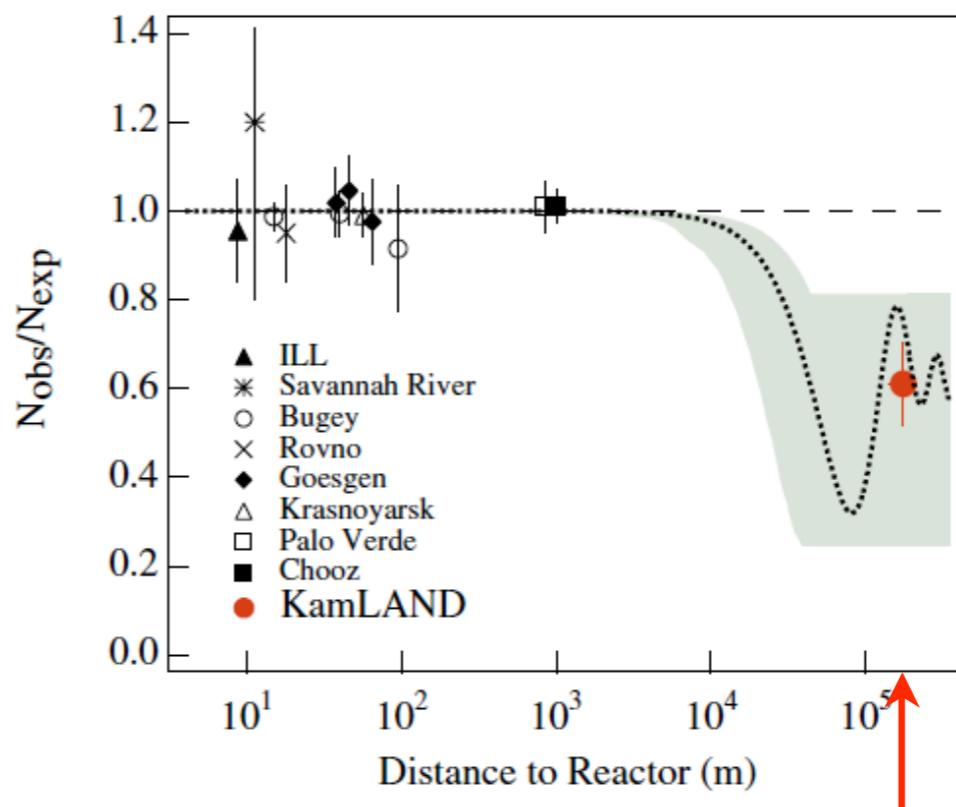


Kamioka Liquid Antineutrino Detector



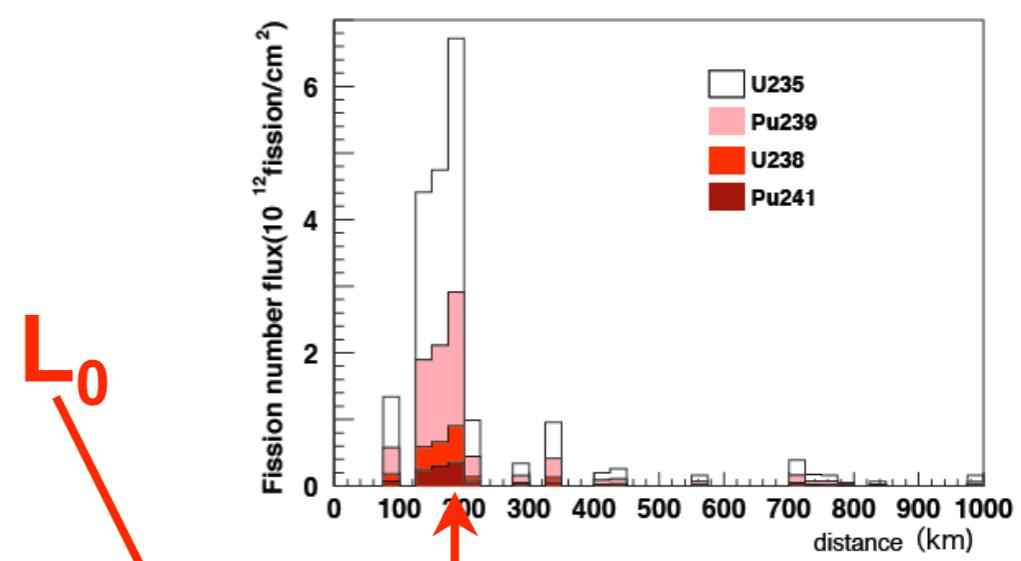
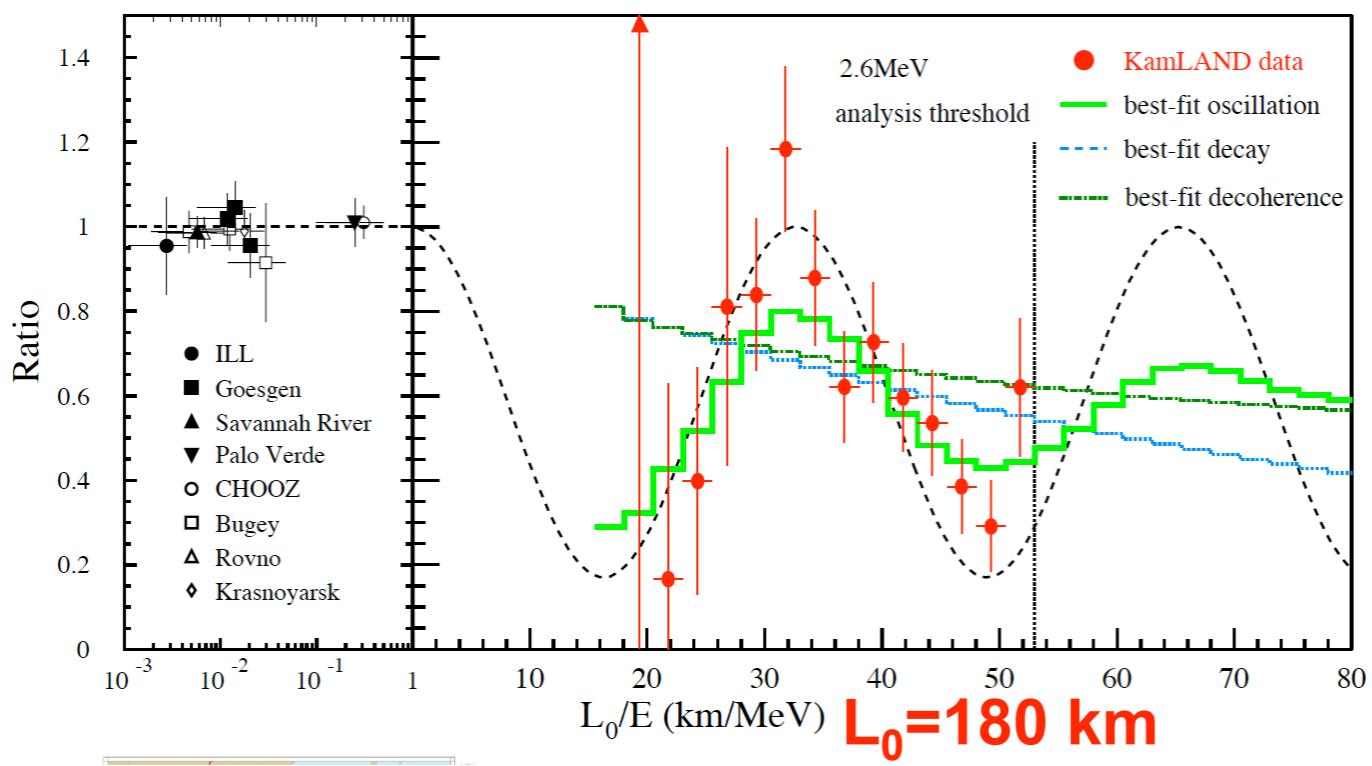


180 km

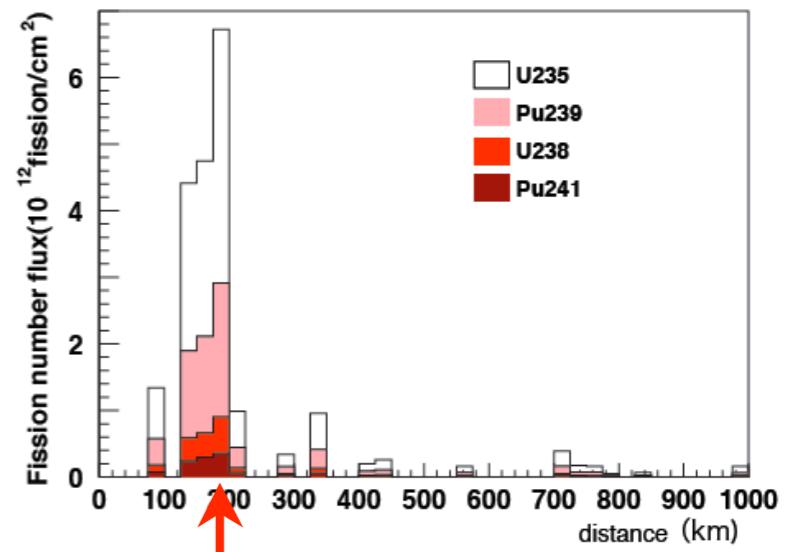


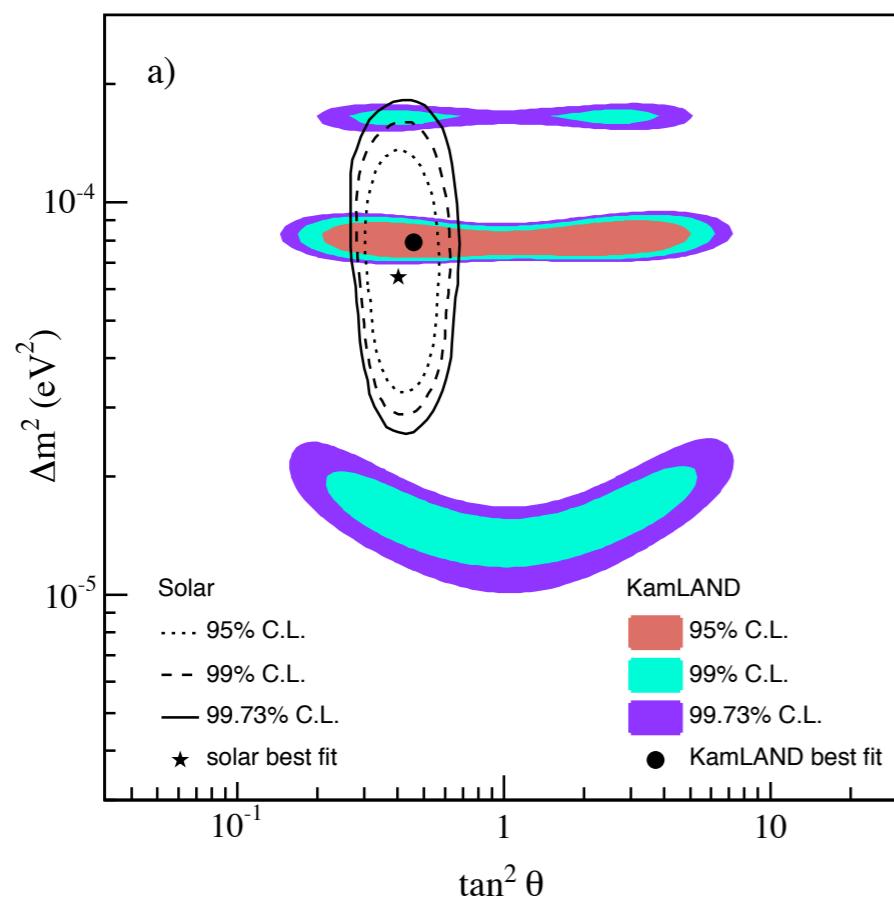
180 km

Disappearance: 99.95% C.L.

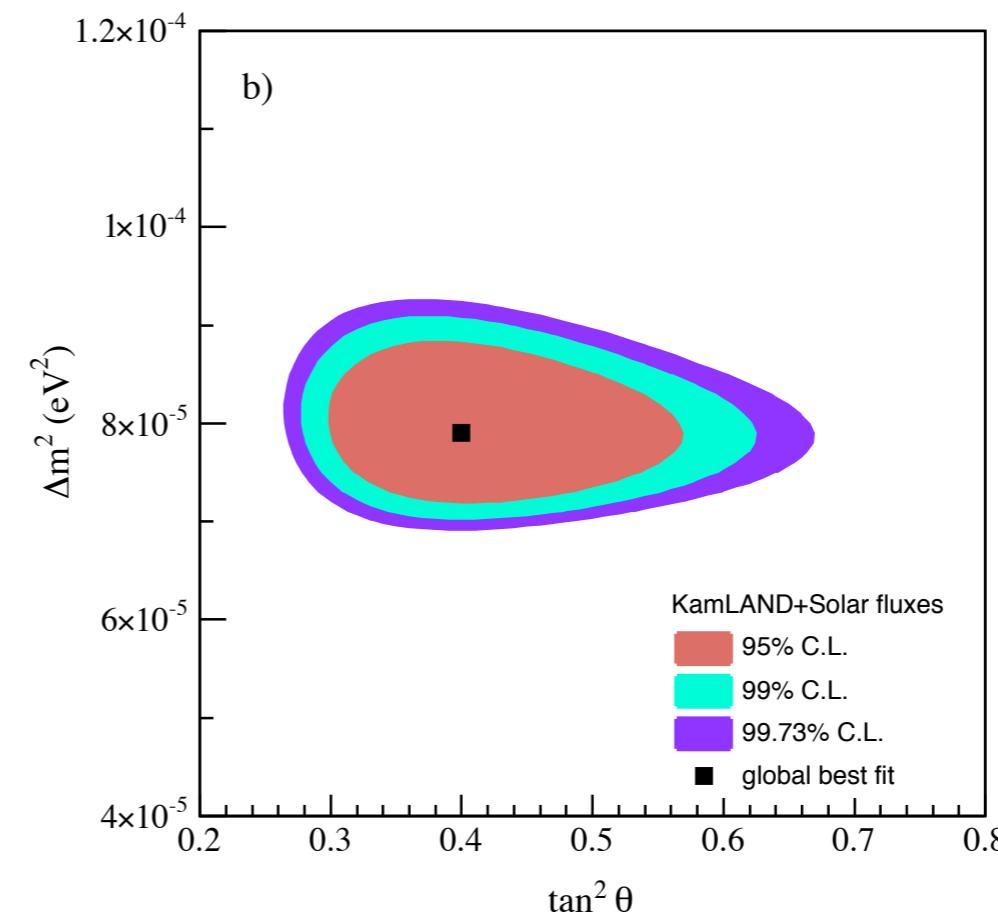


L_0





KamLAND Only

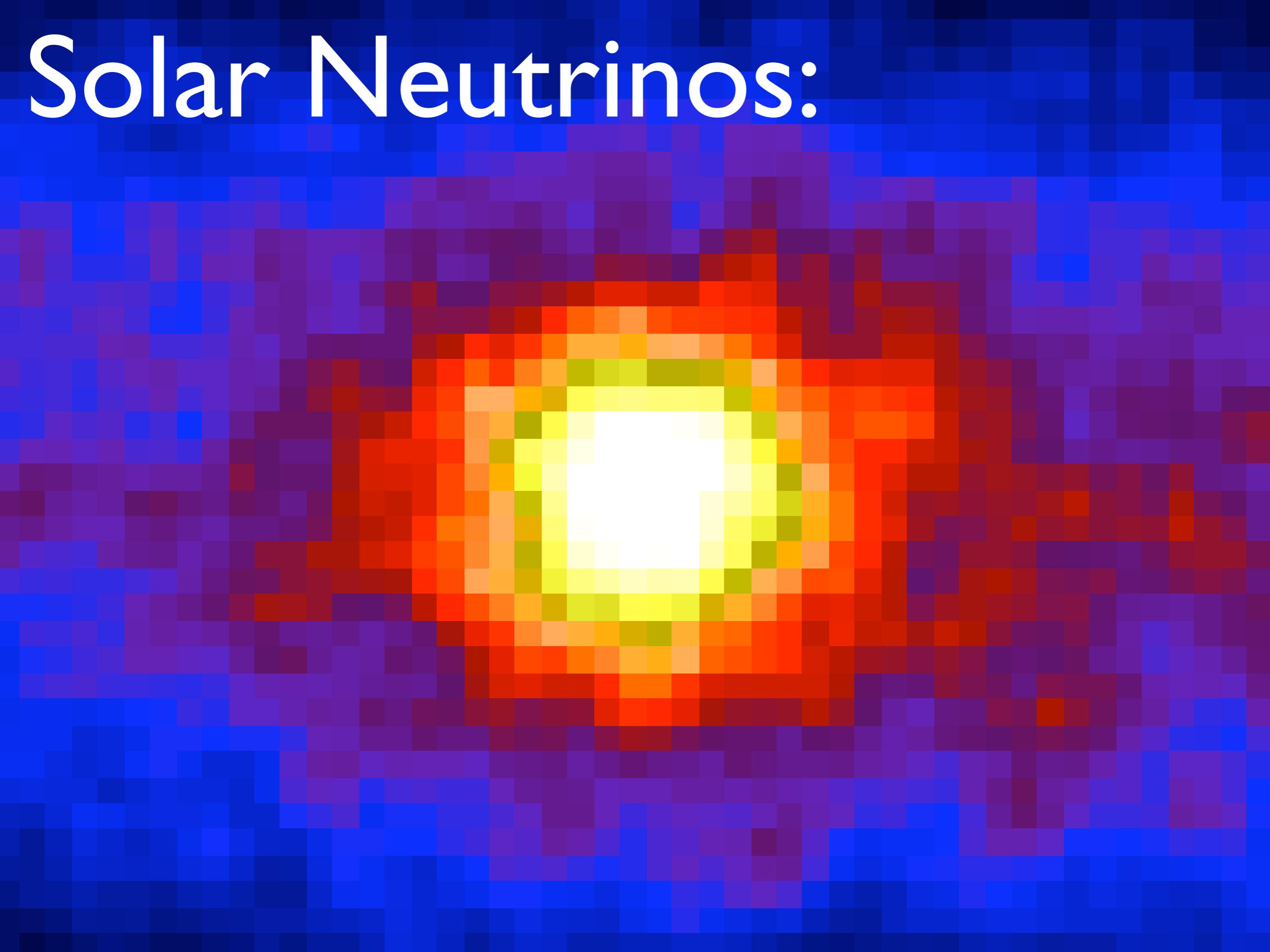


Solar + KamLAND

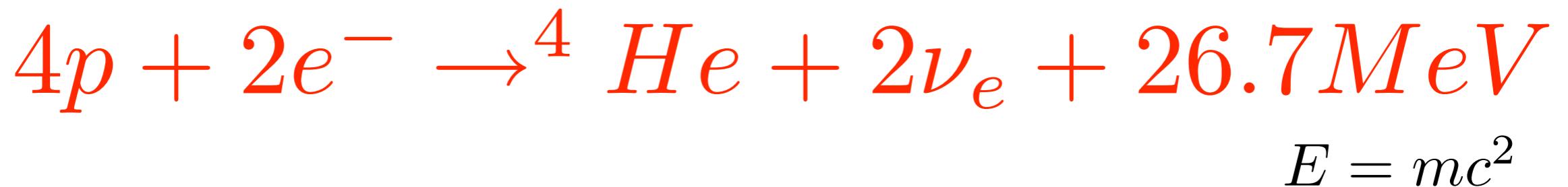
$$\delta m_{\odot}^2 = 8.0^{+0.4}_{-0.3} \times 10^{-5} \text{ eV}^2,$$

$$\sin^2 \theta_{\odot} = 0.310 \pm 0.026,$$

Solar Neutrinos:



Solar Engine:



1 ν_e for every 13.4 MeV ($=2.1 \times 10^{-12} \text{ J}$)

\mathcal{L}_\odot at earth's surface 0.13 watts/cm²

$$\phi_\nu = \frac{0.13}{2.1 \times 10^{-12}} = 6 \times 10^{10} / \text{cm}^2 / \text{sec}$$

This corresponds to an average of 2 ν 's per cm³
since they are going at speed c.

Solar Spectrum:

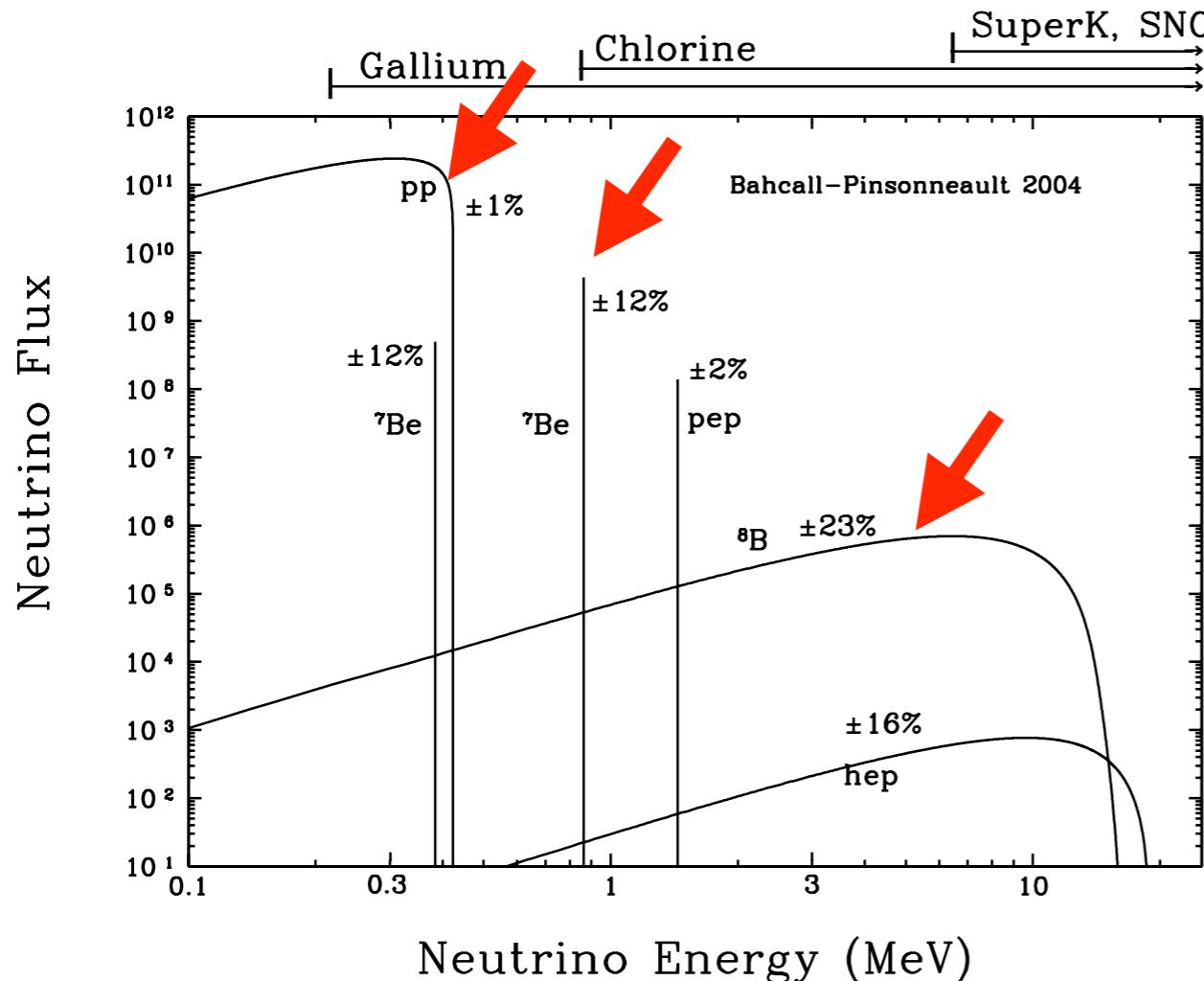
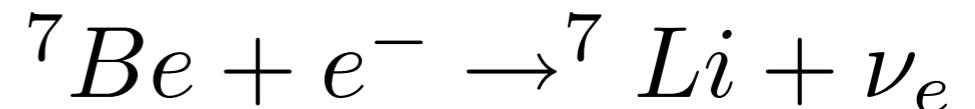


Figure 1. The predicted solar neutrino energy spectrum. The figure shows the energy spectrum of solar neutrinos predicted by the BP04 solar model [22]. For continuum sources, the neutrino fluxes are given in number of neutrinos $\text{cm}^{-2} \text{s}^{-1} \text{MeV}^{-1}$ at the Earth's surface. For line sources, the units are number of neutrinos $\text{cm}^{-2} \text{s}^{-1}$. Total theoretical uncertainties taken from column 2 of table 1 are shown for each source. To avoid complication in the figure, we have omitted the difficult-to-detect CNO neutrino fluxes (see table 1).



$$\phi_{pp} = 5.94(1 \pm 0.01) \times 10^{10} \text{ cm}^{-2} \text{ sec}^{-1}$$



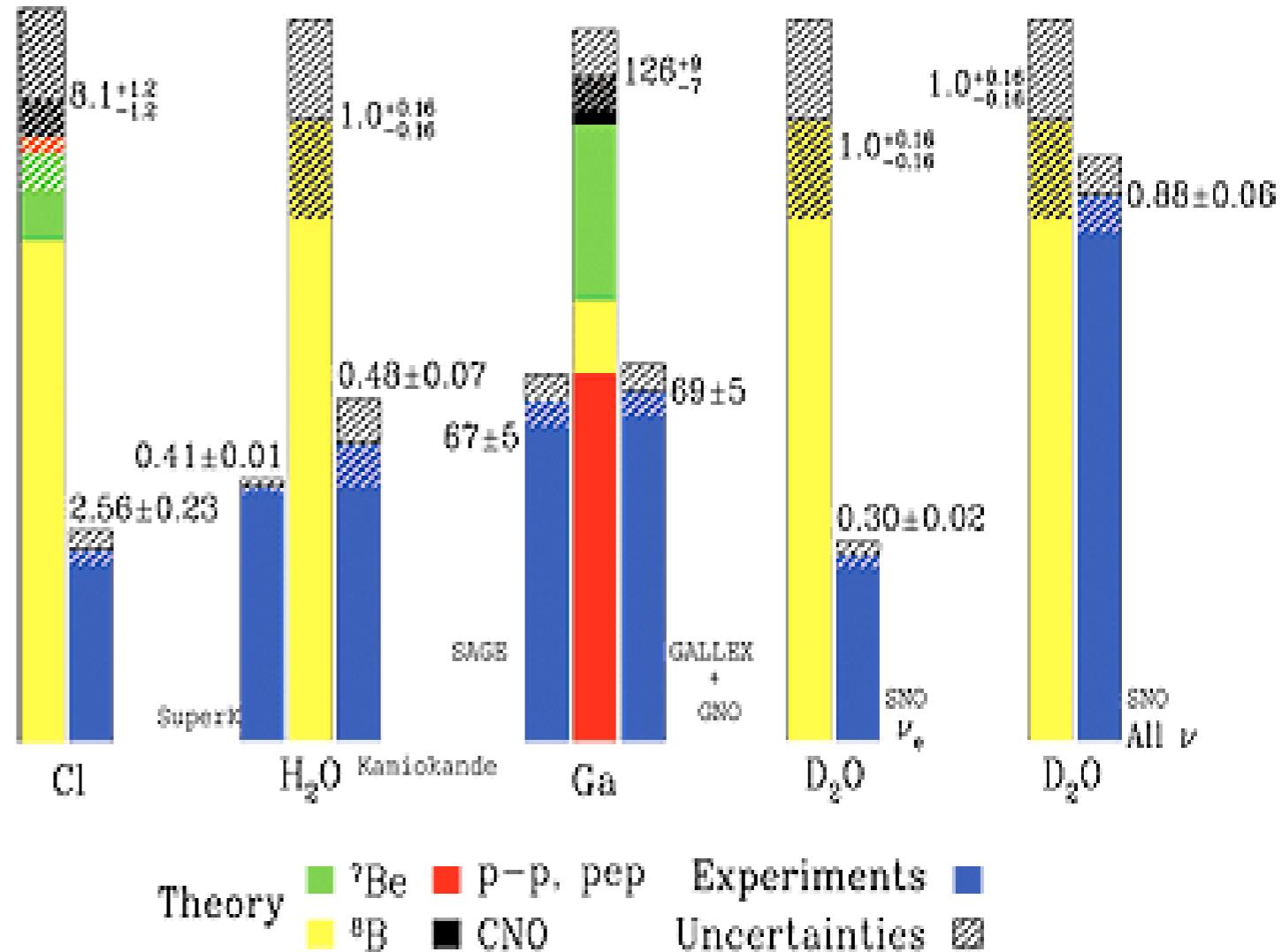
$$\phi_{^7Be} = 4.86(1 \pm 0.12) \times 10^9 \text{ cm}^{-2} \text{ sec}^{-1}$$



$$\phi_{^8B} = 5.82(1 \pm 0.23) \times 10^6 \text{ cm}^{-2} \text{ sec}^{-1}$$



Total Rates: Standard Model vs. Experiment
Bahcall–Serenelli 2005 [BS05(OP)]

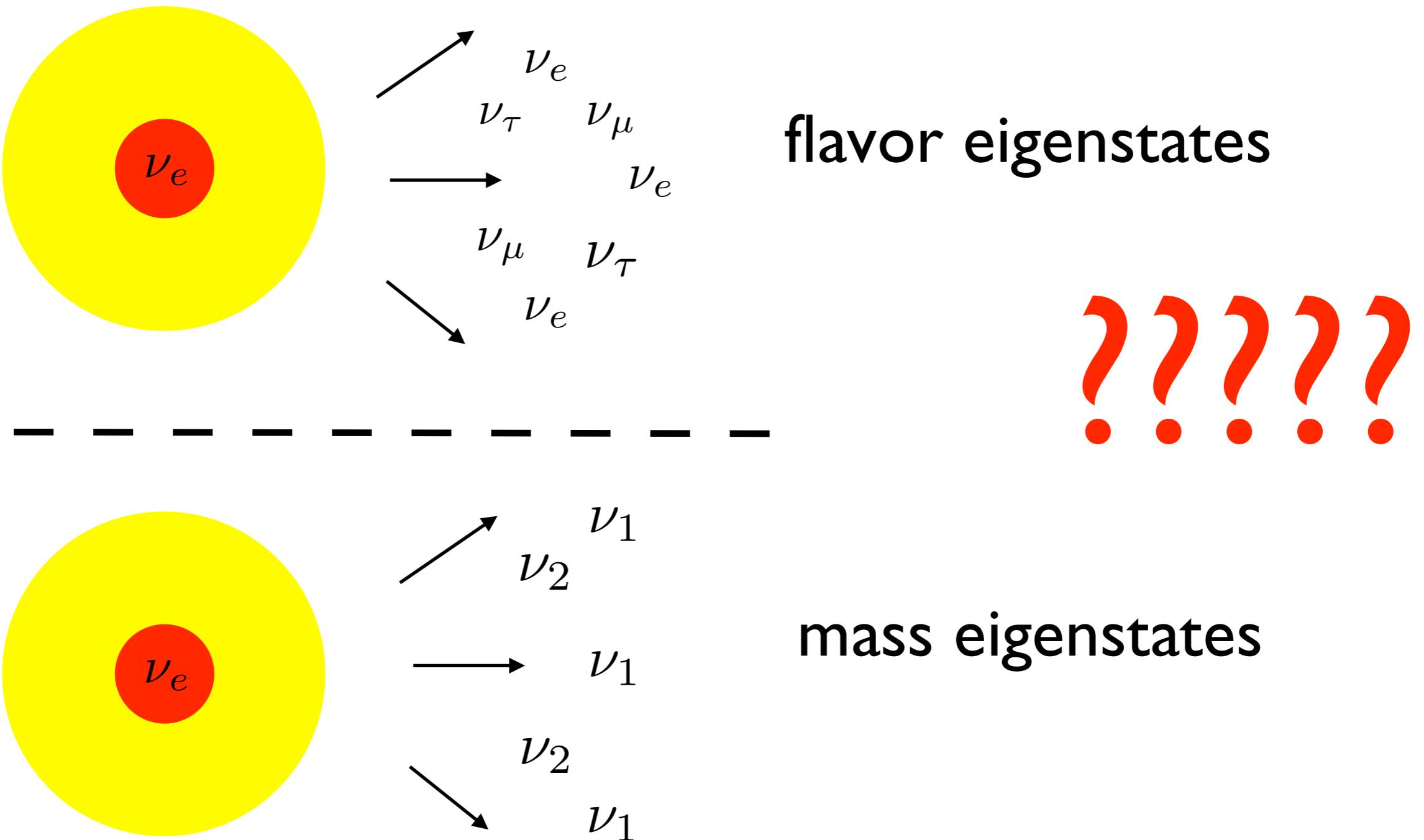


Ray Davis & John Bahcall

Theory v Exp.

Neutrino Flavor Transitions!!!

Identical Solar Twins:



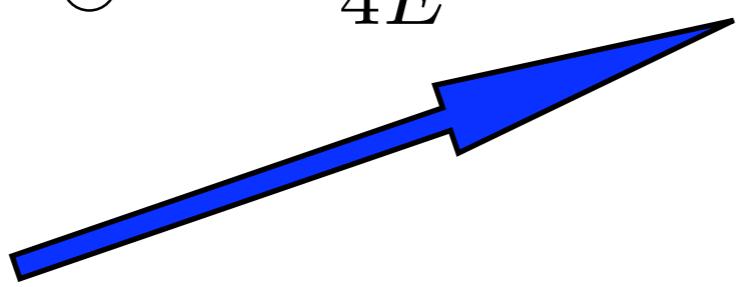
Kinematical Phase:

$$\delta m_{\odot}^2 = 8.0 \times 10^{-5} eV^2$$

$$\sin^2 \theta_{\odot} = 0.31$$

$$\Delta_{\odot} = \frac{\delta m_{\odot}^2 L}{4E} = 1.27 \quad \frac{8 \times 10^{-5} \text{ } eV^2 \cdot 1.5 \times 10^{11} \text{ } m}{0.1-10 \text{ } MeV}$$

???



$$\Delta_{\odot} \approx 10^{7 \pm 1}$$

Effectively Incoherent !!!

Vacuum ν_e Survival Probability:

$$\langle P_{ee} \rangle = f_1 \cos^2 \theta_\odot + f_2 \sin^2 \theta_\odot$$

where f_1 and f_2 are the fraction of ν_1 and ν_2 at production.

In vacuum $f_1 = \cos^2 \theta_\odot$ and $f_2 = \sin^2 \theta_\odot$.

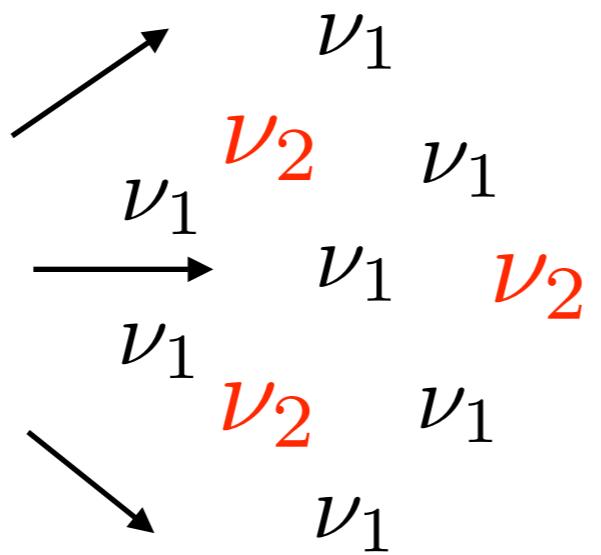
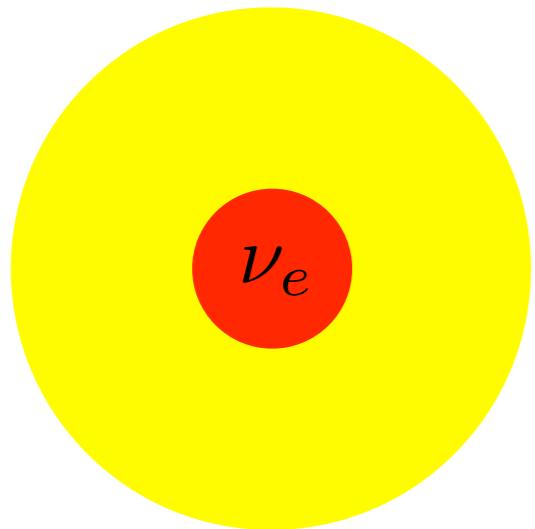
Note energy independence.

$$\langle P_{ee} \rangle = \cos^4 \theta_\odot + \sin^4 \theta_\odot = 1 - \frac{1}{2} \sin^2 2\theta_\odot$$

for pp and ${}^7\text{Be}$ this is approximately THE ANSWER.

$f_1 \sim 69\%$ and $f_2 \sim 31\%$ and $\langle P_{ee} \rangle \approx 0.6$

pp and ${}^7\text{Be}$



$$f_1 \sim 69\%$$

$$f_2 \sim 31\%$$

$$\langle P_{ee} \rangle \approx 0.6$$

$$f_3 = \sin^2 \theta_{13} < 4\%$$

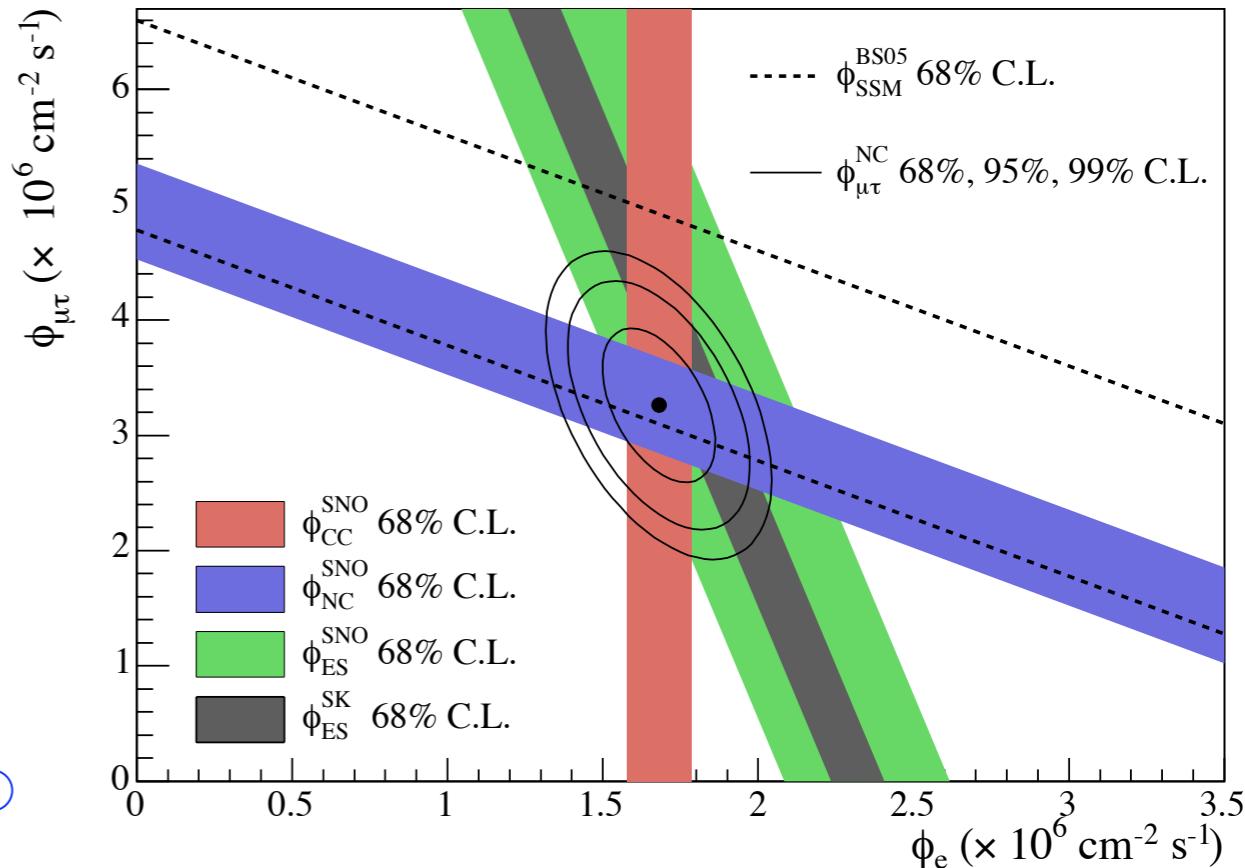
What about 8B ?

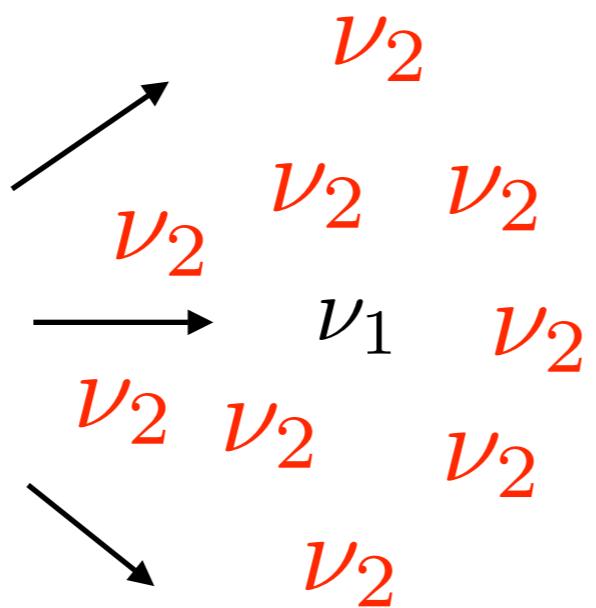
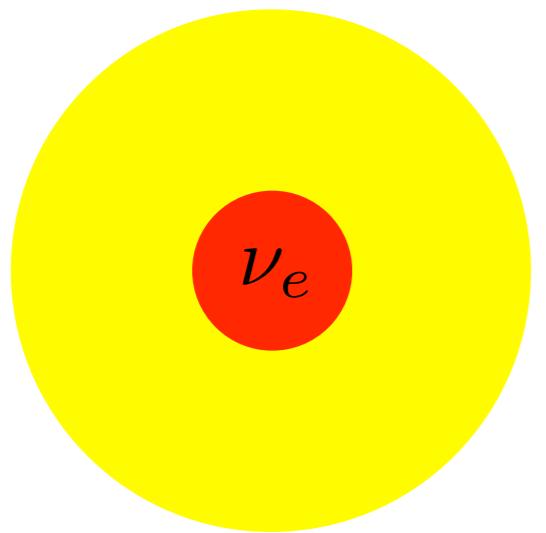
SNO's CC/NC

$$\frac{CC}{NC} = \langle P_{ee} \rangle = f_1 \cos^2 \theta_\odot + f_2 \sin^2 \theta_\odot$$

$$f_1 = \left(\frac{CC}{NC} - \sin^2 \theta_\odot \right) / \cos 2\theta_\odot$$

$$= (0.35 - 0.31)/0.4 \approx 10 \pm ???\%$$



8B 

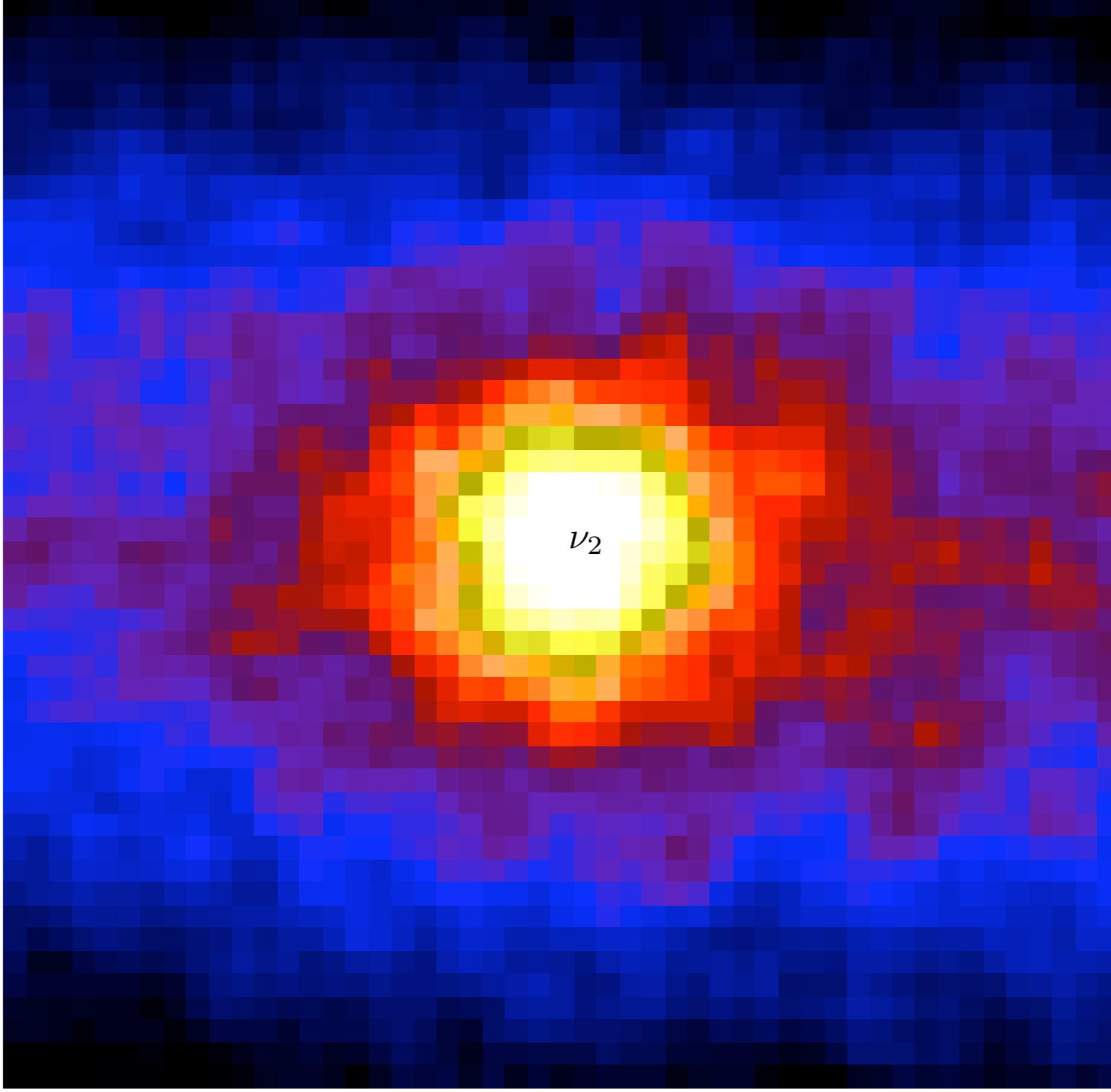
$$f_2 \sim 90\%$$

$$f_1 \sim 10\%$$

$$\langle P_{ee} \rangle = \sin^2 \theta + f_1 \cos 2\theta_\odot \approx \sin^2 \theta_\odot = 0.31$$

Wow!!! How did that happen???

energy dependence!!!



These are ν_2 Neutrinos !!!