

Mass Hierarchy via Mossbauer Neutrinos and Reactor Neutrinos

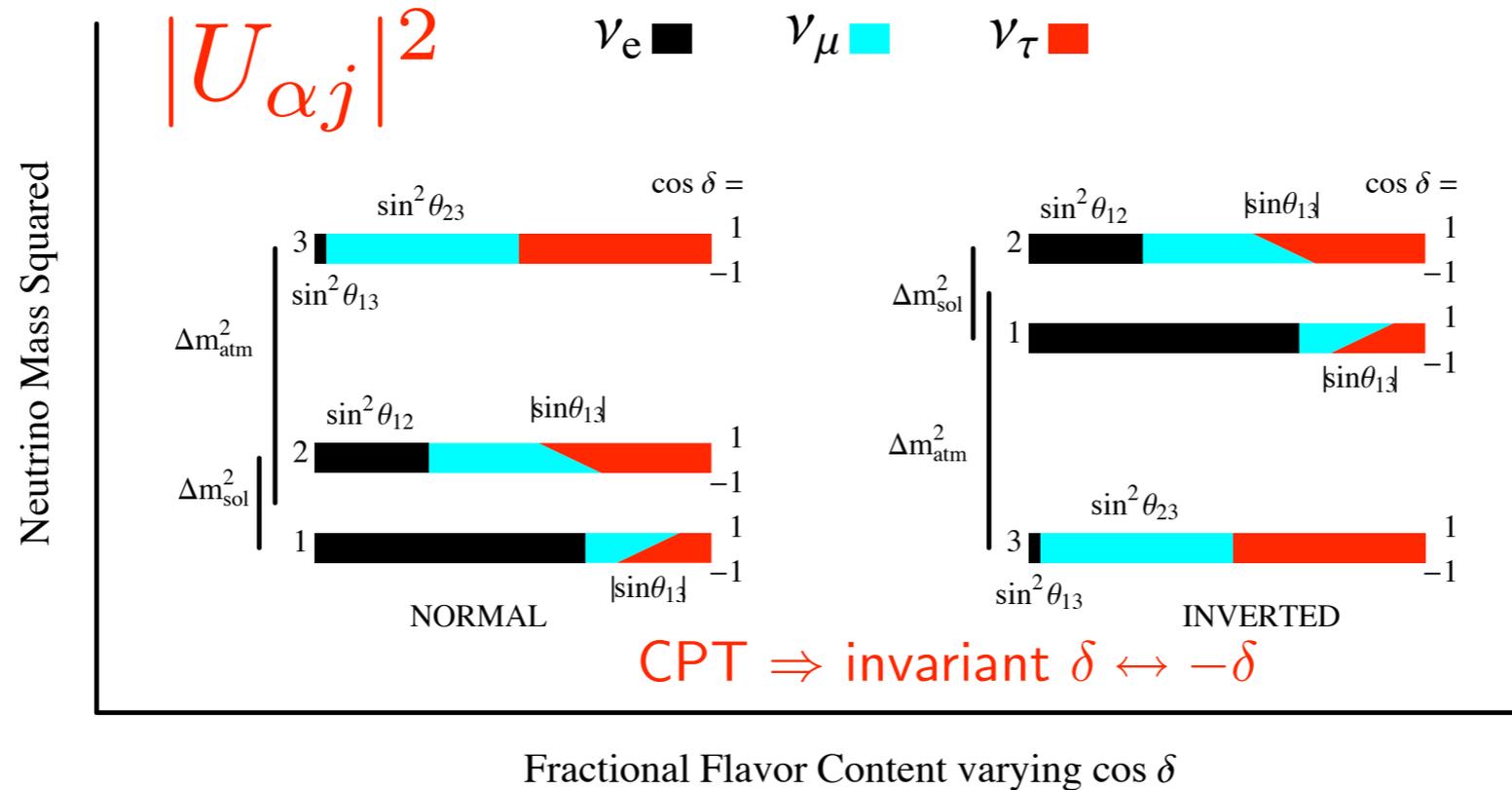
Stephen Parke - Fermilab

hep-ph/0701151

Minakata, Nunokawa, SP & Zukanovich Funchal

Atmospheric Neutrino Mass Hierarchy:

Mena + SP
hep-ph/0312131



defn: $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$

Solar neutrino mass hierarchy (mass ordering of ν_1 & ν_2)
was determined by SNO !

Mossbauer Neutrinos:

Mossbauer effect with Neutrinos in the ${}^3H - {}^3He$ system:



$$Q = 18.6 \text{ keV and } \Gamma_{{}^3H} = 1.2 \times 10^{-24} \text{ eV}$$

Various line broadening effects which significantly increase Γ_{eff}

Serious technical difficulties exist but it is not impossible (Raghaven, Potzel)

For $\Gamma_{eff} \sim 10^{-11} \text{ eV}$ ($\Delta E/E \sim 10^{-15}$) then $\sigma \sim 10^{-33} \text{ cm}^2$!!!

Do Mossbauer Neutrinos Oscillate? YES

(Akhmedov, Kopp, Lindner 0802.2513, 0803.1424)

(see also Bilenky, Feilitzsch, Potzel)

ν_e Disappearance

solar osc. (first min 270m)

atm osc. (first min 9m)

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} [\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}]$$

$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E}$ (kinematic phase).

$$\Delta_{21} = \Delta_{31} - \Delta_{32}$$

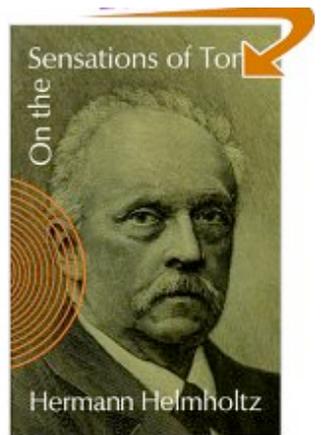
$$\cos^2 \theta_{12} > \sin^2 \theta_{12}$$

- for **Normal Hierarchy (NH)**: $|\Delta_{31}| > |\Delta_{32}|$

phase of atmospheric oscillation **ADVANCES** by $2\pi \sin^2 \theta_{12}$ for every solar osc.

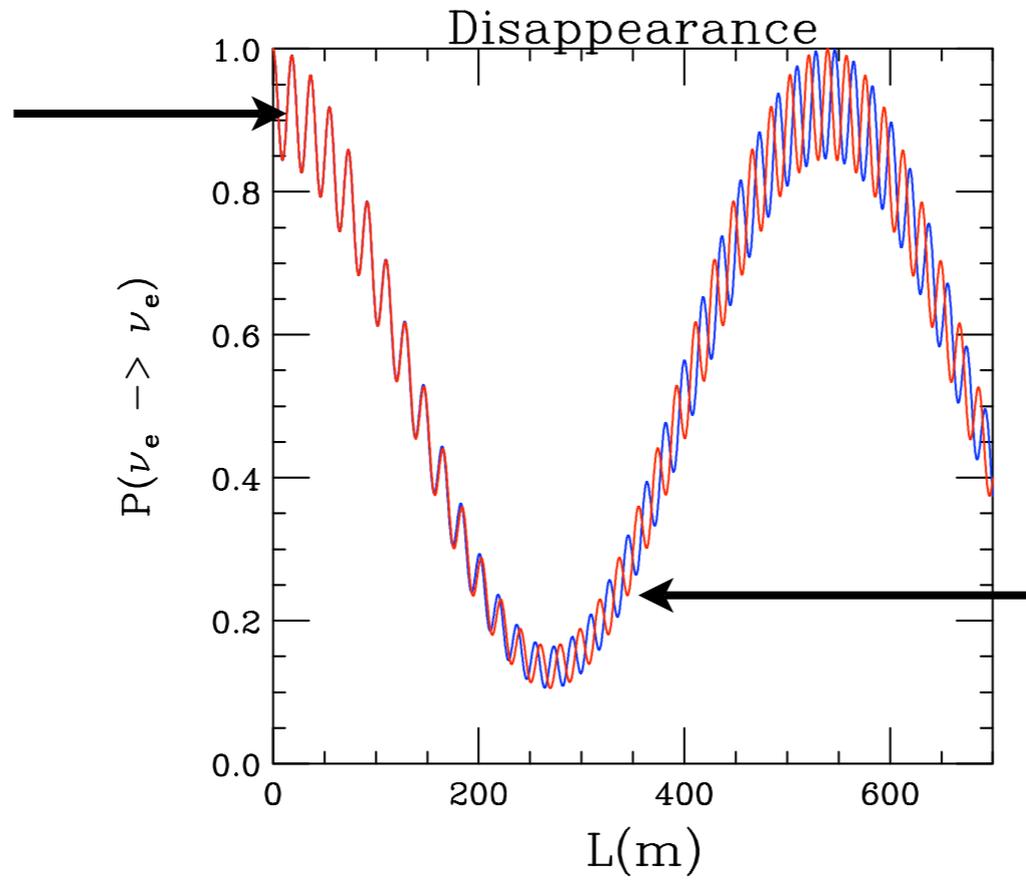
- for **Inverted Hierarchy (IH)**: $|\Delta_{31}| < |\Delta_{32}|$

phase of atmospheric oscillation **RETARDED** by $2\pi \sin^2 \theta_{12}$ for every solar osc.



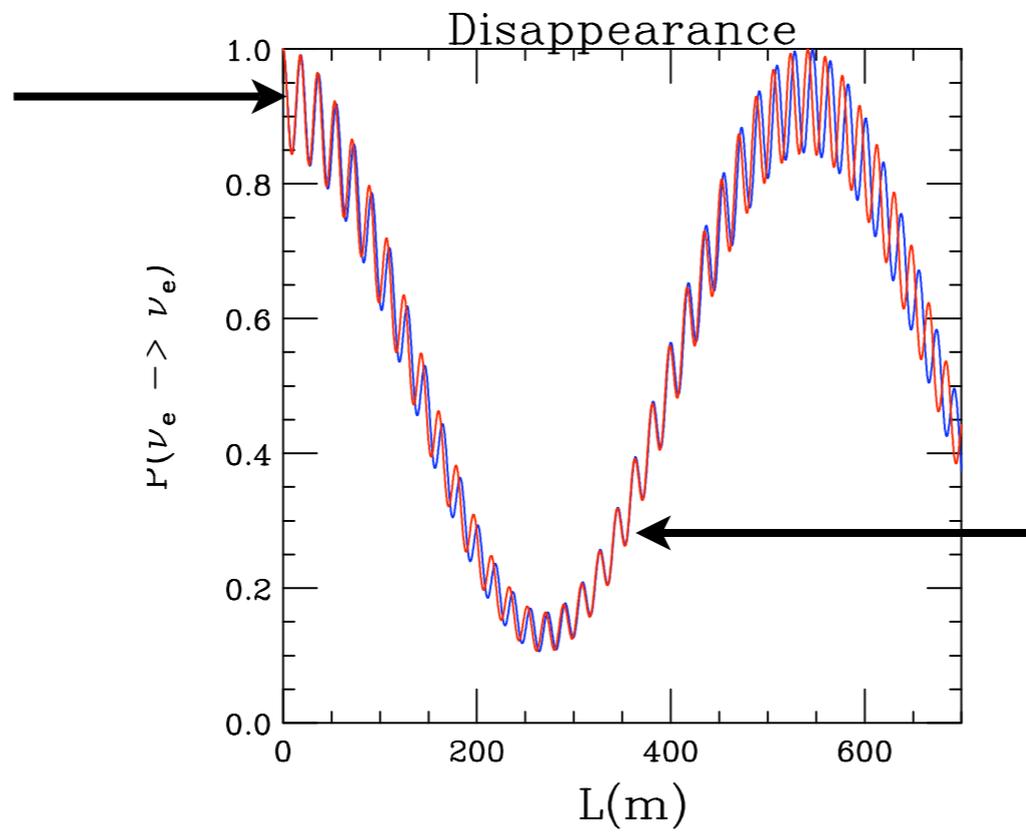
1875

in phase



out of phase by $\pi/2$

$$\delta m_{IH}^2 = 1.03 \times \delta m_{NH}^2$$



in phase

Combining the Atm Osc:

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \frac{1}{2} \sin^2 2\theta_{13} \left\{ 1 + \sqrt{(1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21}) \cos(2\Delta_{ee} \pm \phi)} \right\}$$

$$\Delta_{ee} \equiv \Delta m_{ee}^2 L / 4E$$

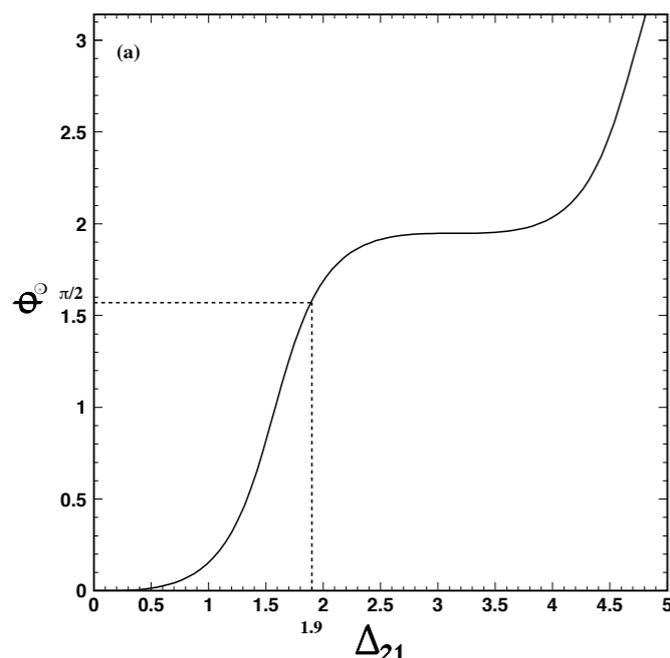
NH (+) and IH (-):

$$\Delta m_{ee}^2 = c_{12}^2 |\Delta m_{31}^2| + s_{12}^2 |\Delta m_{32}^2| = |m_3^2 - (c_{12}^2 m_1^2 + s_{12}^2 m_2^2)|$$

← ν_e weighted average of m_1^2 and m_2^2

everything else:

$$\phi_{\odot} \equiv \arctan(\cos 2\theta_{12} \tan \Delta_{21}) - \Delta_{21} \cos 2\theta_{12}$$

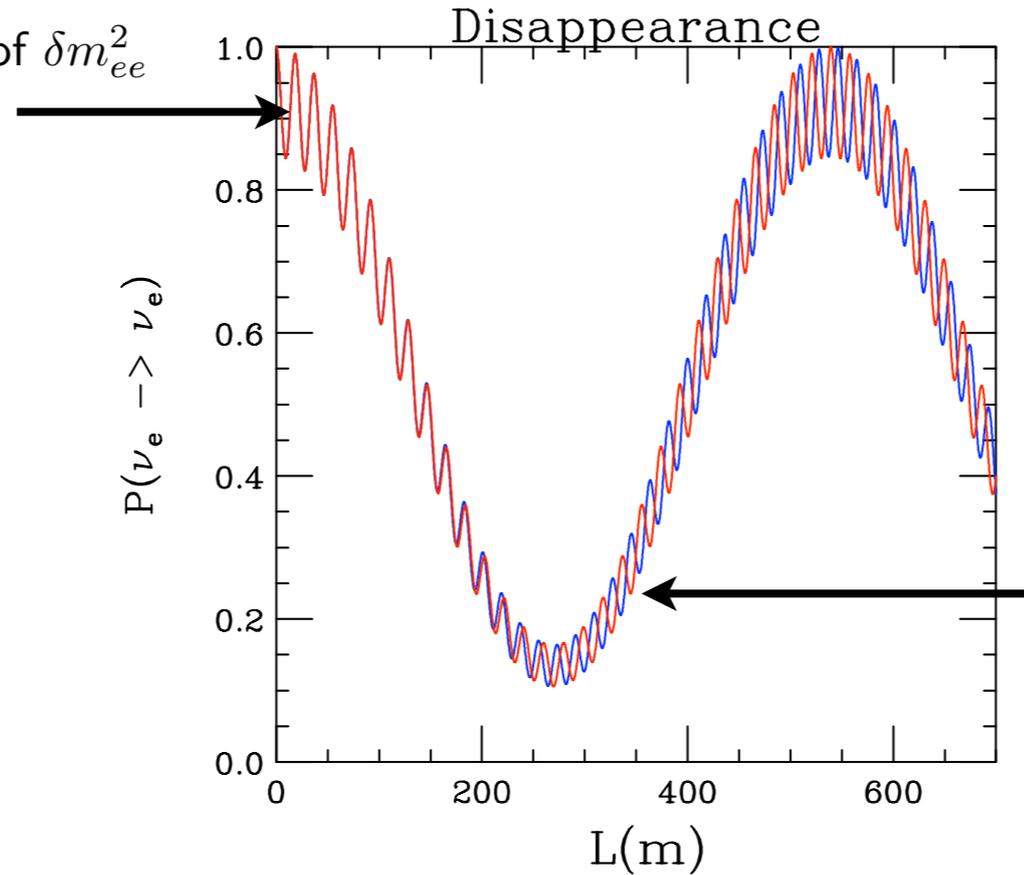


$$\phi_{\odot}(\Delta_{21} + \pi) = \phi_{\odot}(\Delta_{21}) + 2\pi \sin^2 \theta_{12},$$

$$\text{then } \frac{d\phi}{dL} \Big|_{L=0} = 0$$

Strategy:

(I) Precision ($<1\%$) measurement of δm_{ee}^2 at L around 10 m

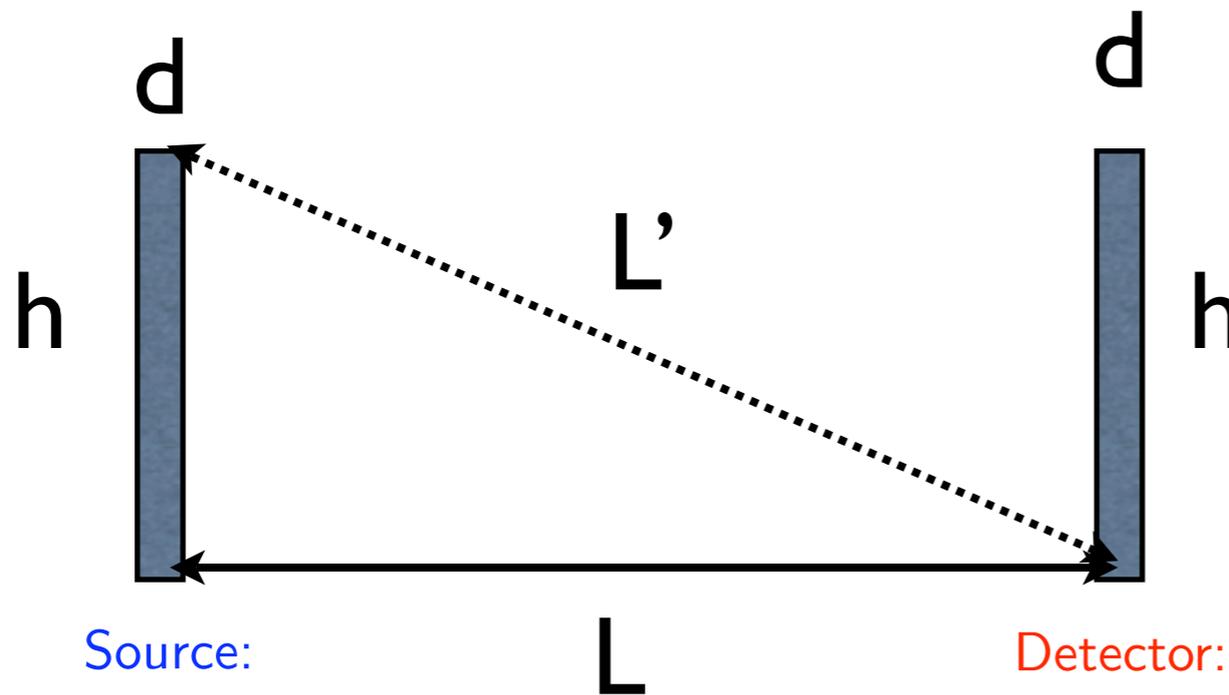
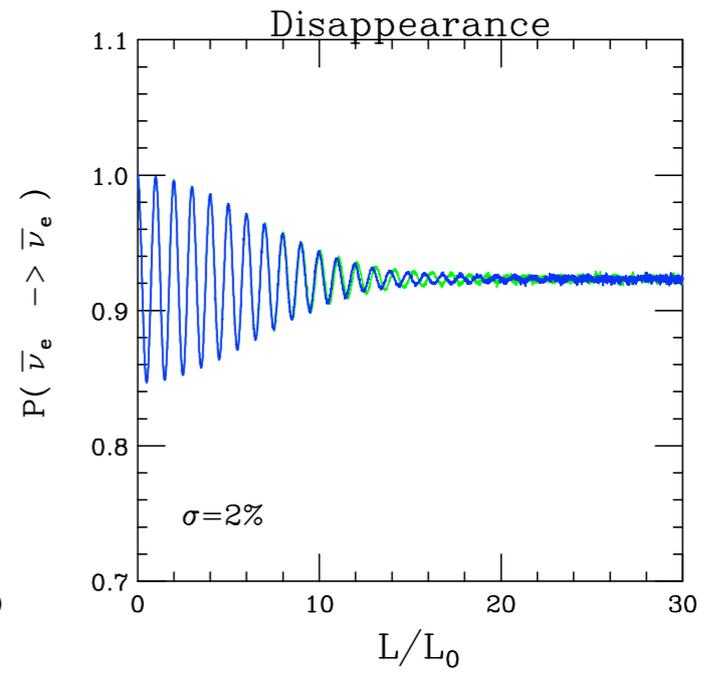
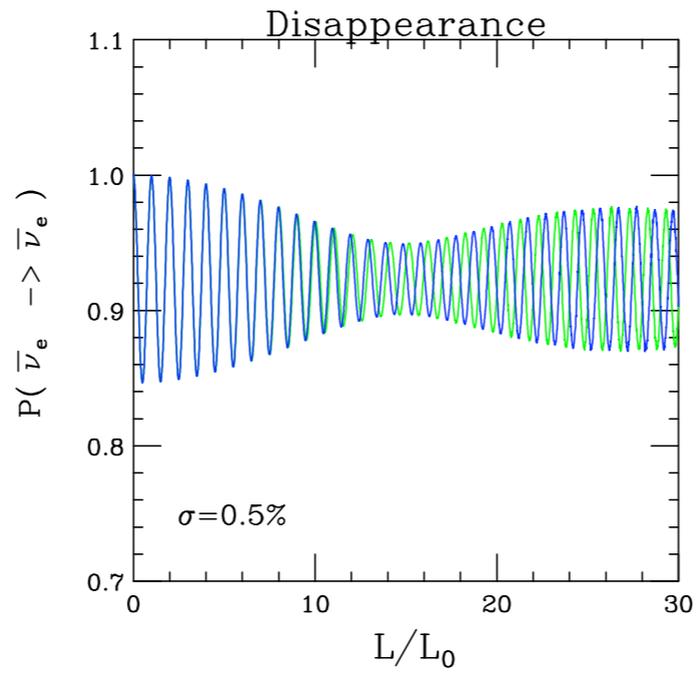
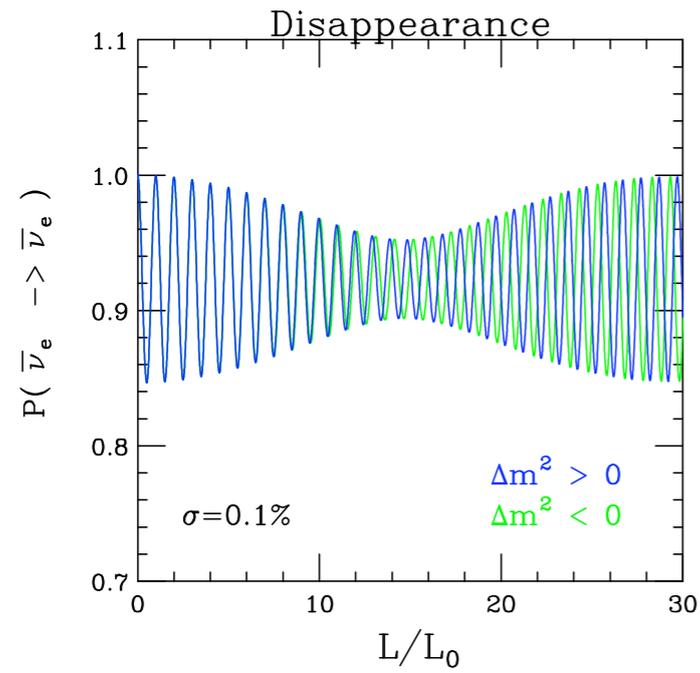
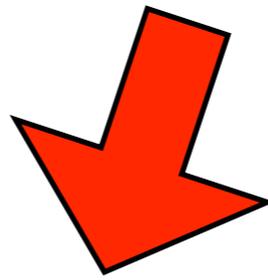


(II) determination of phase at $L=350$ m

But this is after 20 or so oscillation !!!
What about smearing in the L/E ?

E ok, as $\Delta E/E \sim 10^{-15}$

Smearing L:



$$d < L/200$$

$$L' \approx L(1 + \frac{1}{2} \frac{h^2}{L^2}) \text{ so } h < L/10$$

OK

Phase I: Measurement of δm_{ee}^2

(the atm δm^2 near the first osc. minima for a $\bar{\nu}_e$ disapp. exp.)

Event Rate:

$$R_{ench} = 3 \times 10^5 \left(\frac{S}{1MCi} \right) \left(\frac{M_T}{100g} \right) \left(\frac{L}{10m} \right)^{-2} \text{day}^{-1}$$

Minakata and Uchinami: [hep/0602046](#)

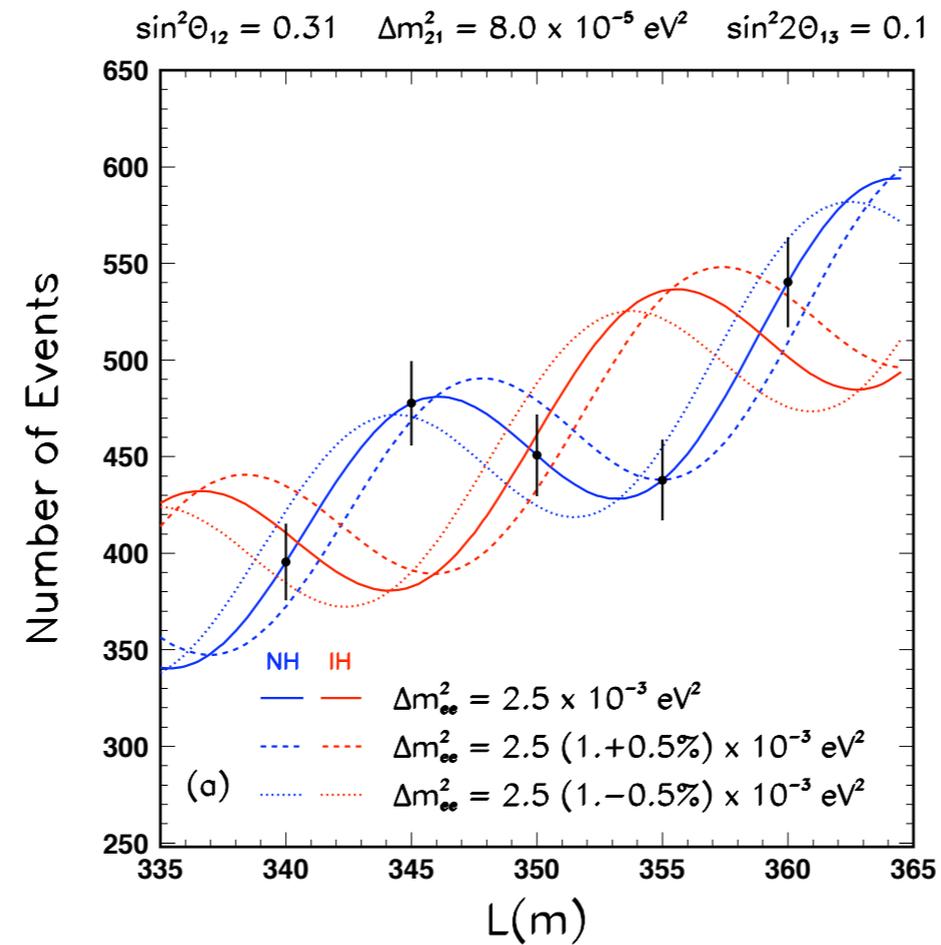
- Run IIB = 10 point measurement at $(1/5, 3/5, \dots, 19/5)L_{OM}$
- 10^6 events each, $\sigma_{sys} = 0.2\%$, $\sigma_c = 10\%$
- Sensitivity in $\delta m_{ee}^2 \approx 0.3 \left(\frac{\sin^2 2\theta_{13}}{0.1} \right)^{-1} \%$

Phase II: phase at 350 m

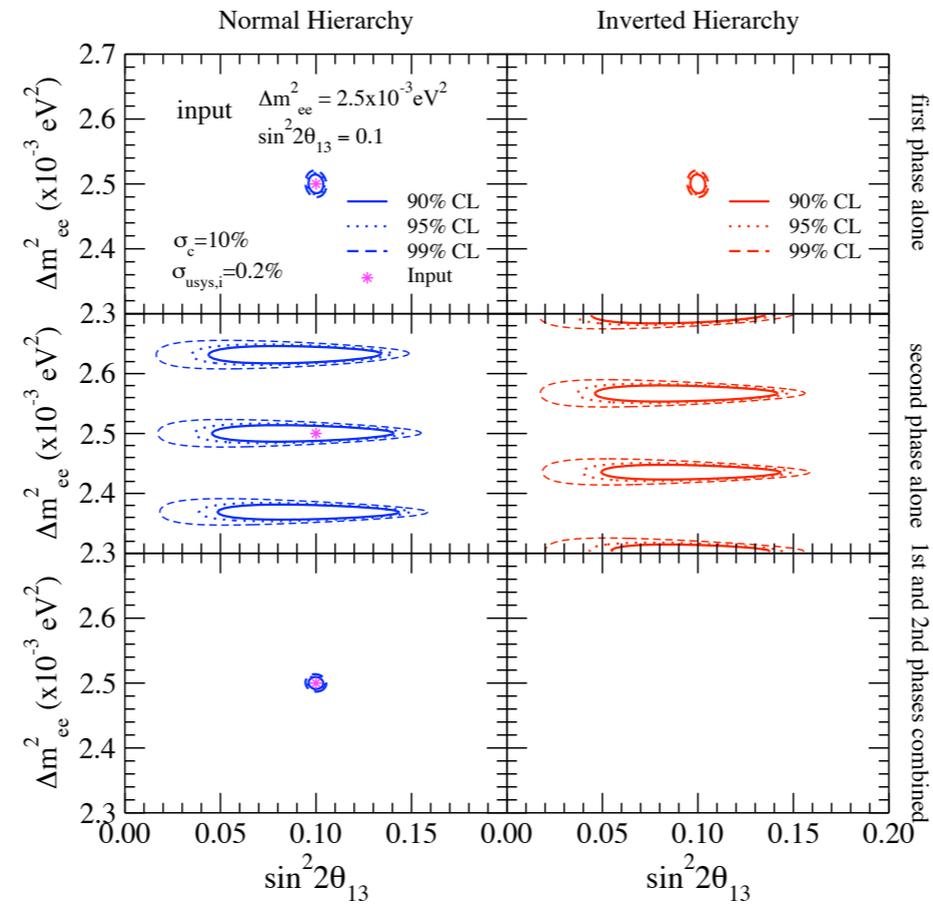
Event Rate:

$$R_{ench} = 2 \times 10^2 \left(\frac{S}{1MCi} \right) \left(\frac{M_T}{100g} \right) \left(\frac{L}{350m} \right)^{-2} \text{day}^{-1}$$

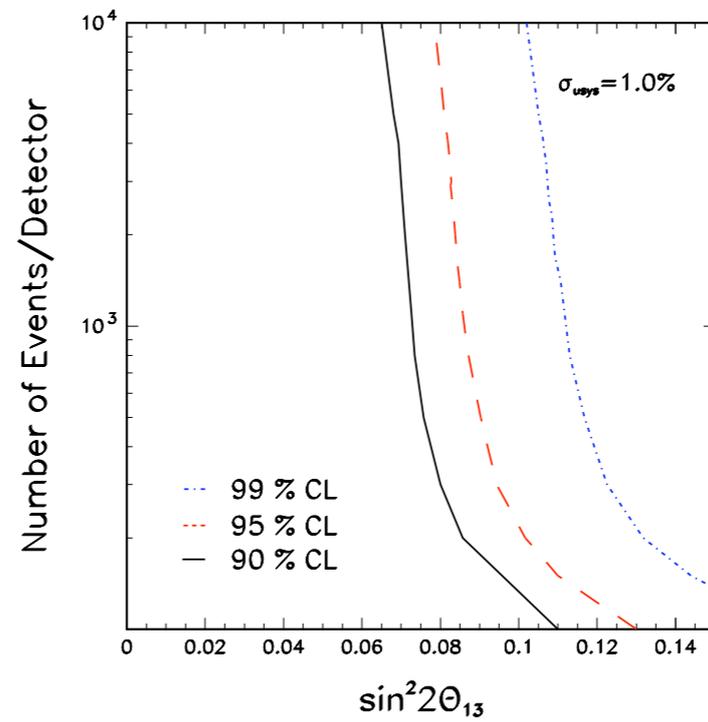
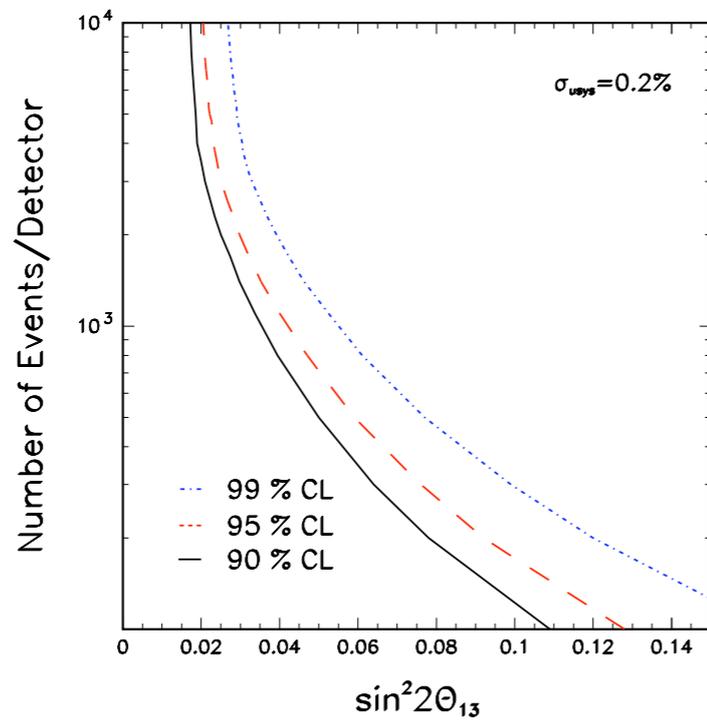
5 Baselines: $L = 350 \pm 5 \pm 10$ m



Phase I
Phase II
Phase I+II



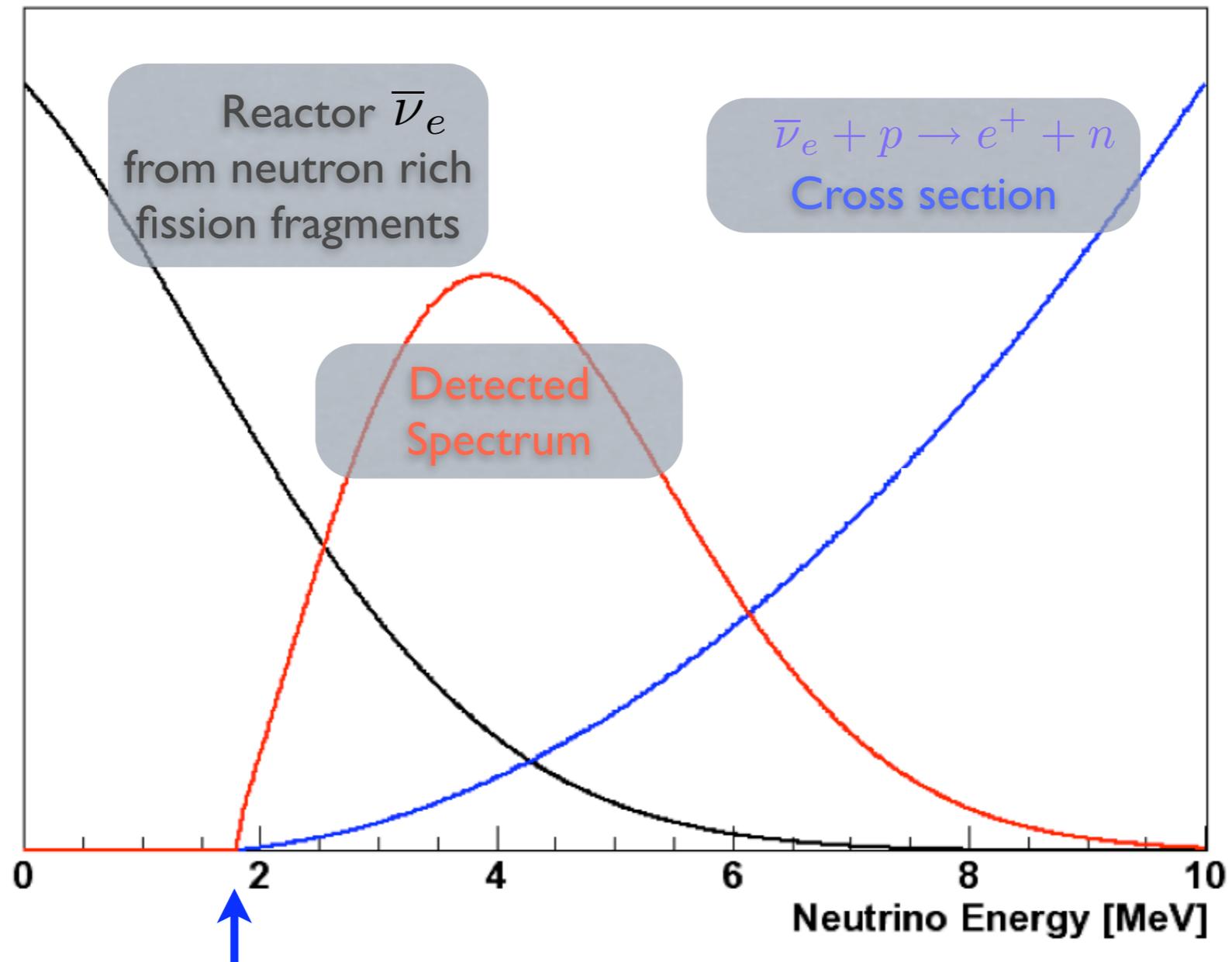
Sensitivity:



Reactor Neutrinos:

Reactor Neutrinos: Mass Hierarchy

Detected Spectrum



Hawaii Antineutrino Observatory Hanohano

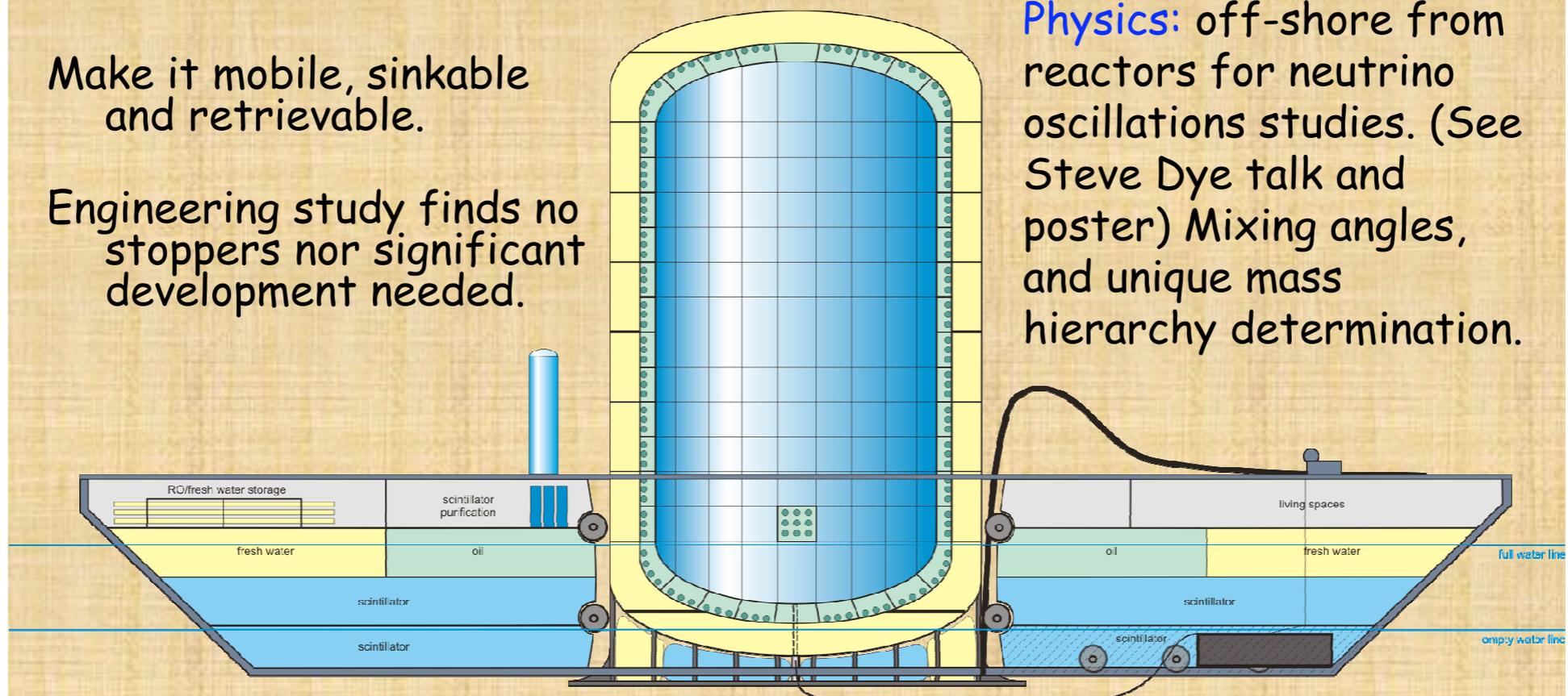
Idea: detector based on KamLAND technology adapted for deep ocean, but >10 x larger (for good counting rate)

Make it mobile, sinkable and retrievable.

Engineering study finds no stoppers nor significant development needed.

Geology: mid-Pacific and elsewhere for geo-neutrinos from mantle.

Physics: off-shore from reactors for neutrino oscillations studies. (See Steve Dye talk and poster) Mixing angles, and unique mass hierarchy determination.



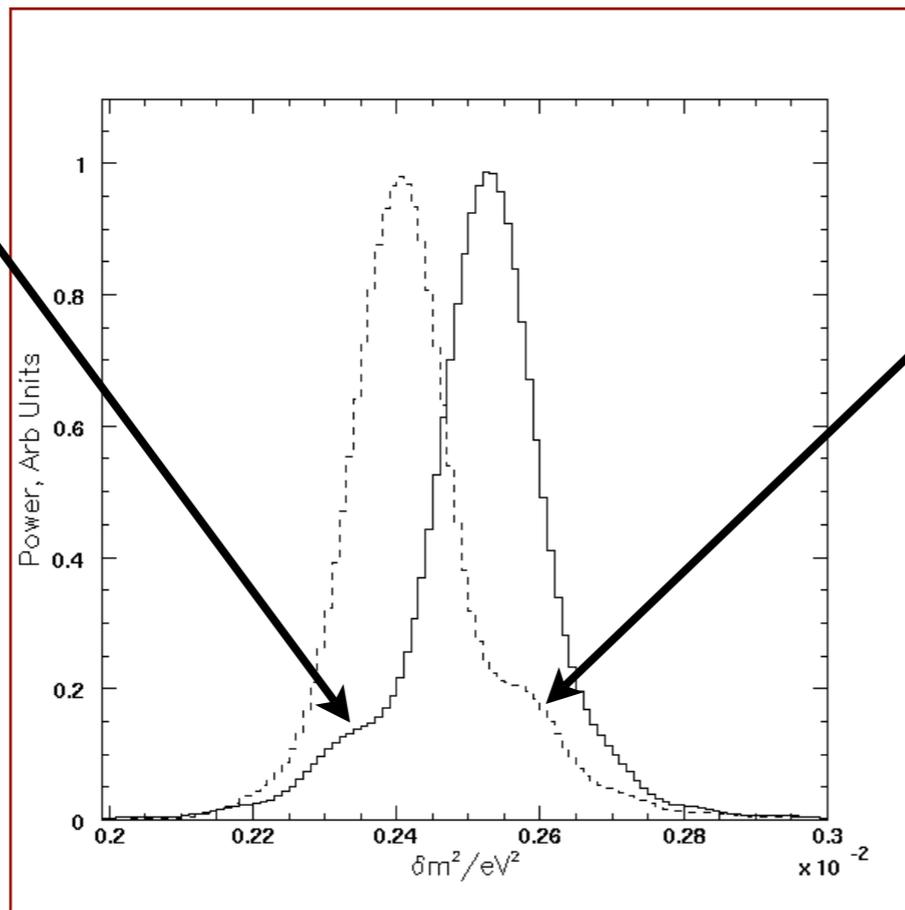
Fourier Transforms: Hanohano

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} [\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32}]$$

dominant frequency

sub-dominant frequency
(1/5 the power)

NH:
shoulder at
smaller freq.



IH:
shoulder at
higher freq.

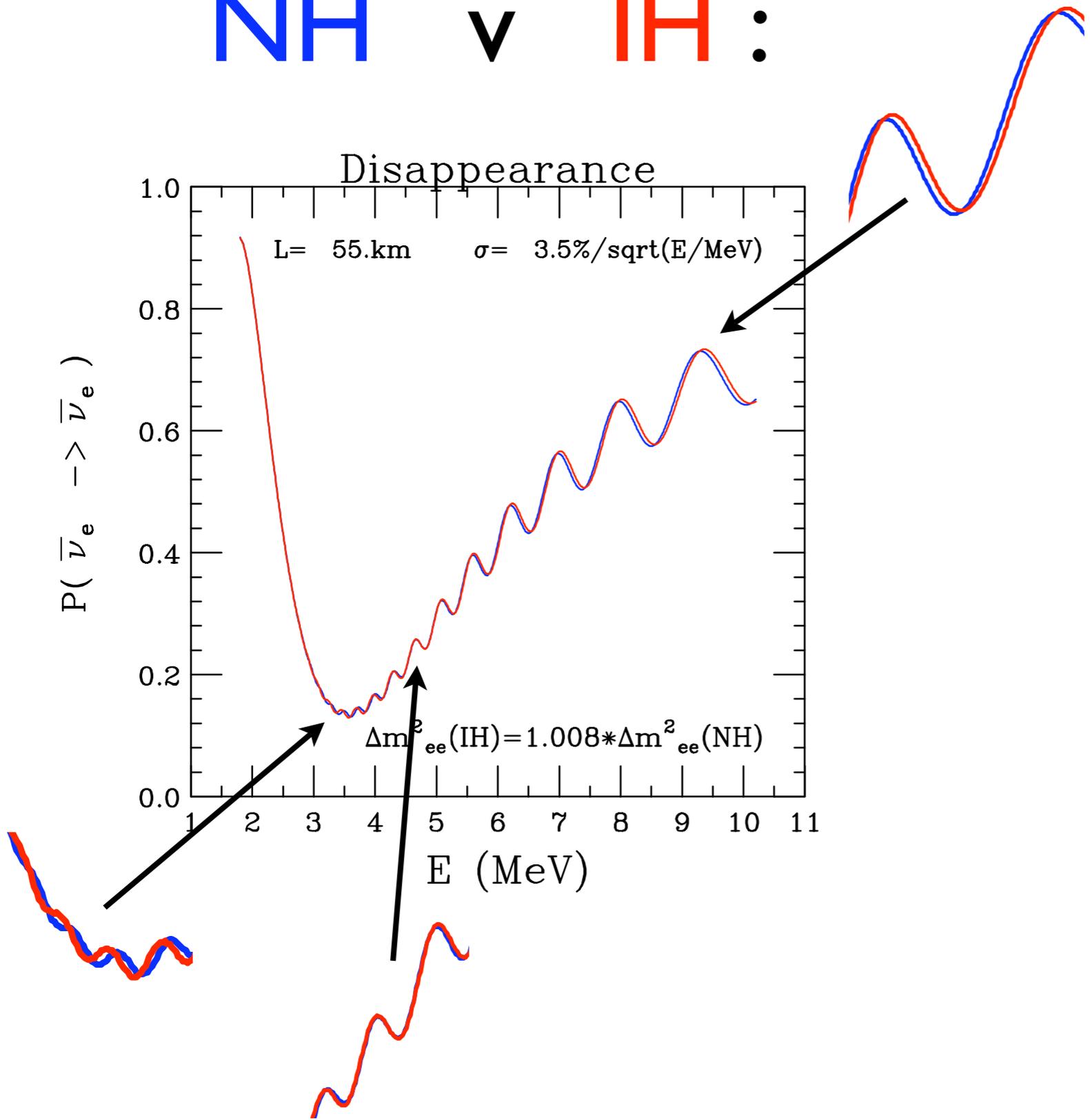
$$\sin^2 2\theta_{13} > 0.05 \text{ for } 10 \text{ Kton-yr}$$

$$\sin^2 2\theta_{13} > 0.02 \text{ for } 100 \text{ Kton-yr}$$

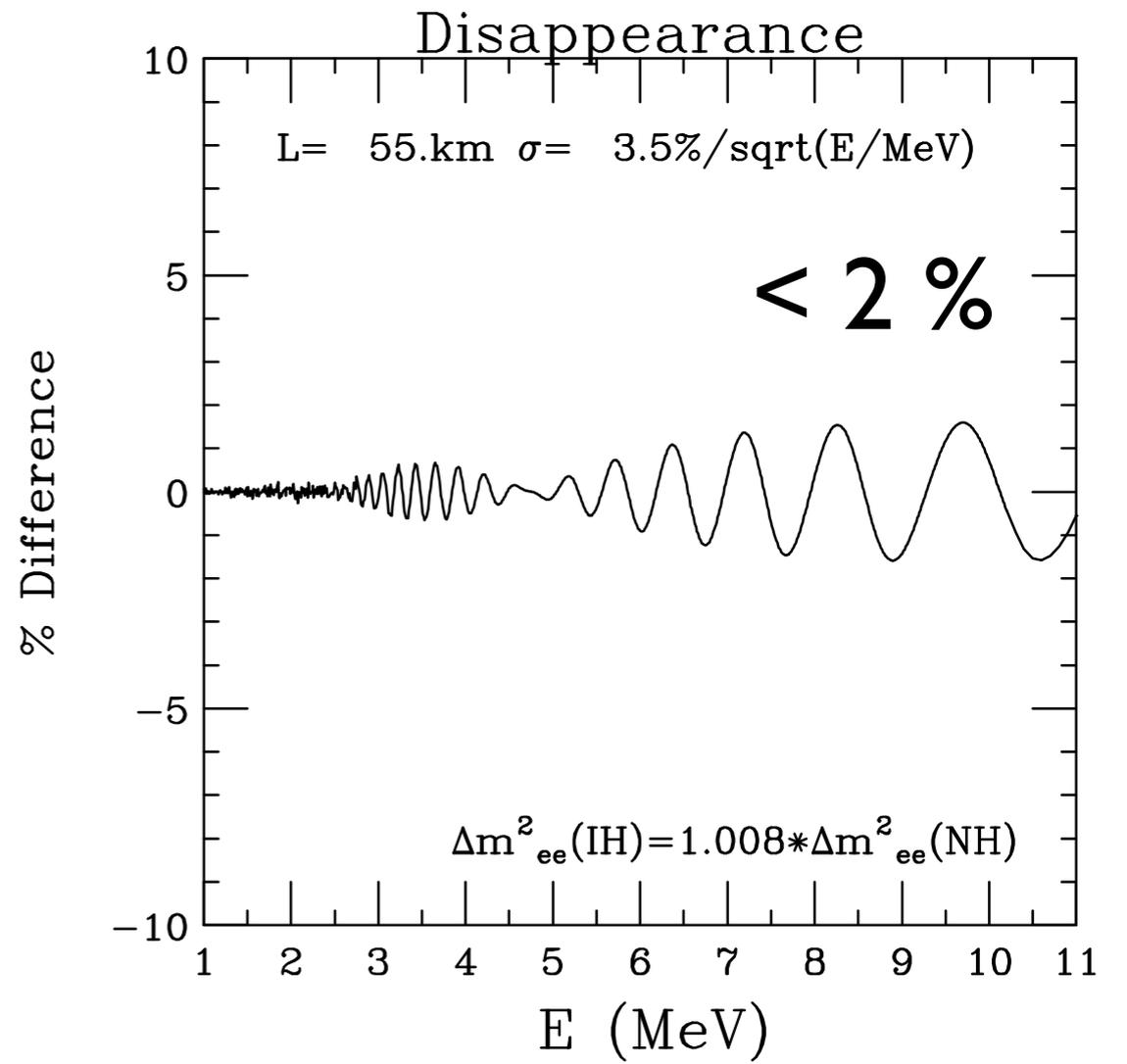
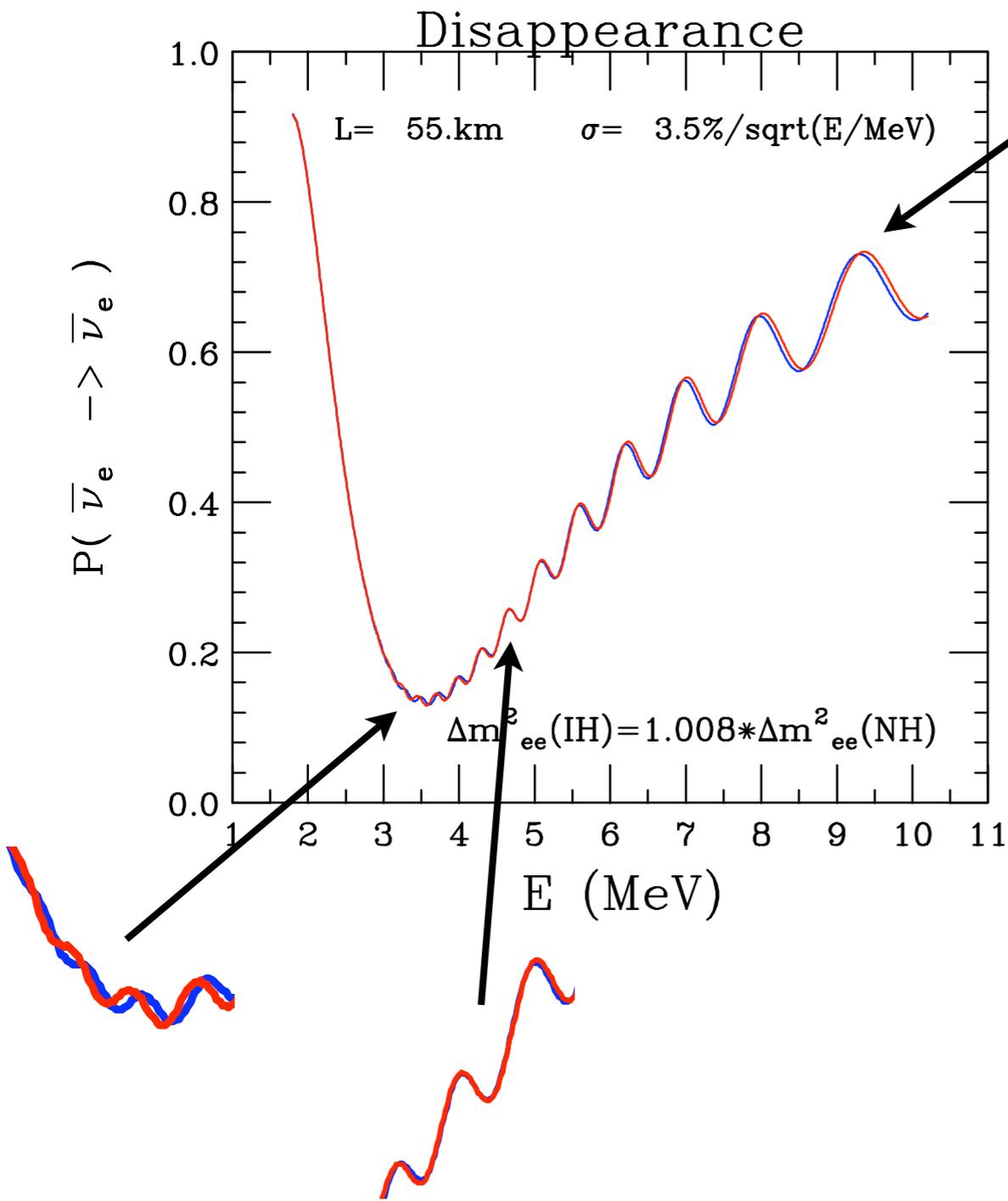
Learned, Dye, Pakvasa, and
Svoboda, *hep-ex/0612022*

also L. Zhan, Y. Wang, J. Cao and L. Wen, arXiv:0807.3203

NH ν IH :

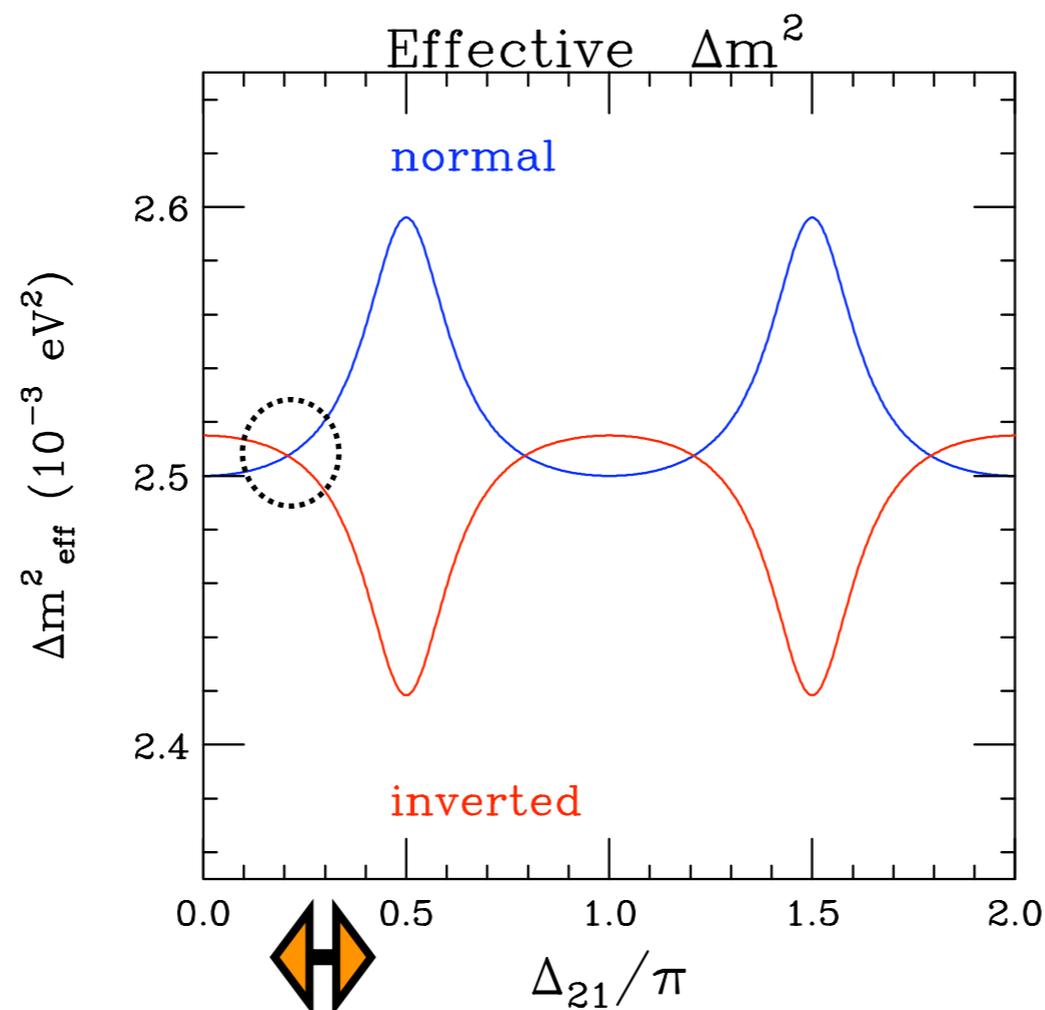


NH ν IH :



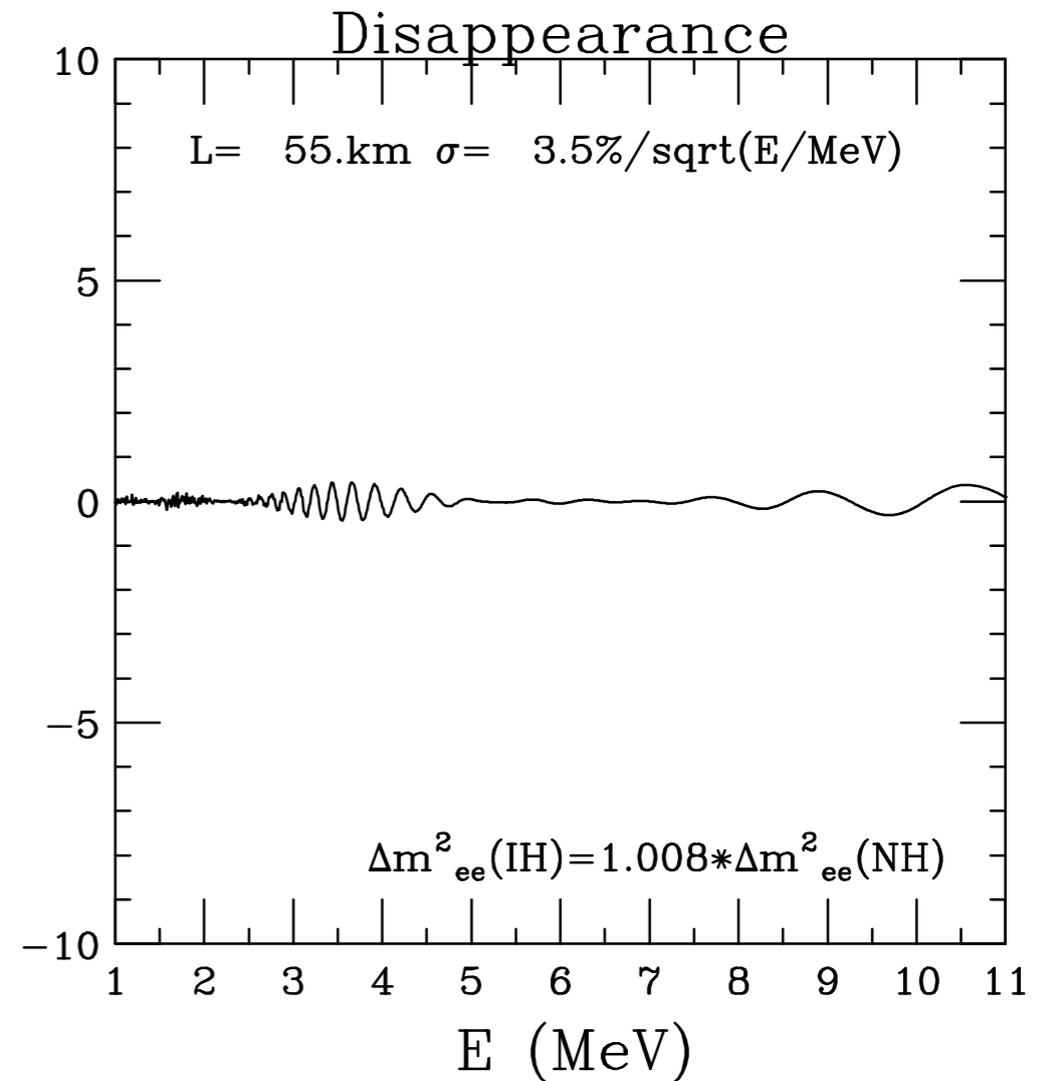
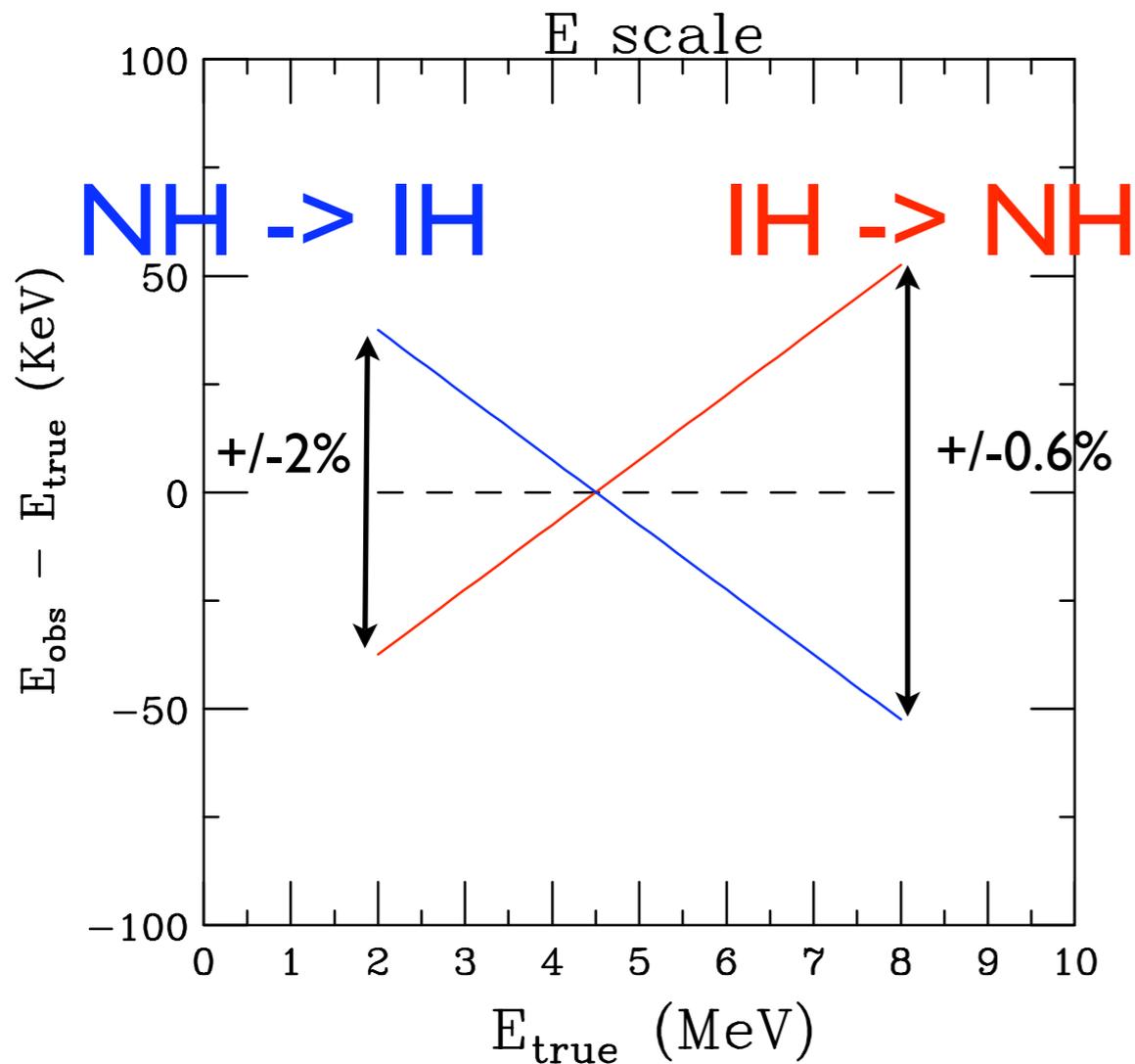
argument of the atm cosine term is $2\Delta_{ee} \pm \phi_{\odot} \equiv \frac{1}{2} \int_0^{L/E} d\rho \delta m_{eff}^2(\rho)$

$$\delta m_{eff}^2(L/E) = \delta m_{ee}^2 \pm \frac{1}{2} \delta m_{21}^2 \cos 2\theta_{12} \frac{\sin^2 2\theta_{12} \sin^2 \Delta_{21}}{(1 - \sin^2 2\theta_{12} \sin^2 \Delta_{21})}$$



Uncertainty in E scale ??? between 2 and 8 MeV !!!

$$\frac{P_{IH}(E_{obs}) - P_{NH}(E_{true})}{P_{NH}(E_{true})} \%$$



$$E_{obs} = E_{true} + 0.015 \times (E_{true} - 4.5)$$

$$E_{obs} = E_{true} - 0.015 \times (E_{true} - 4.5)$$

Summary & Conclusions

The phase advancement or retardation of the atmospheric oscillation allows for the possibly determination of the neutrino mass hierarchy in $\bar{\nu}_e$ disappearance experiments:

- For monochromatic $\bar{\nu}_e$ beams this would require a high precision measurement of δm_{atm}^2 around the first oscillation minimum as well as a determination of the phase 20 or so oscillations out ! Challenging, but the high event rate that maybe possible with Mossbauer neutrinos could make this possible with modest size detectors.
- Reactor neutrinos using multi-cycle analyses (Fourier) requires high precision relative determination of the neutrino energy from 2 to 8 MeV. What you call a 6 MeV neutrino must have twice the energy of what you call a 3 MeV to about 1%, otherwise the hierarchies can be confused. This requirement is very challenging for a large detector.